

# FRM financialriskmeter

Andrija Mihoci

Cathy Yi-Hsuan Chen

Wolfgang Karl Härdle

Michael Althof

Ladislaus von Bortkiewicz Chair of Statistics

Humboldt-Universität zu Berlin

[lvb.wiwi.hu-berlin.de](http://lvb.wiwi.hu-berlin.de)

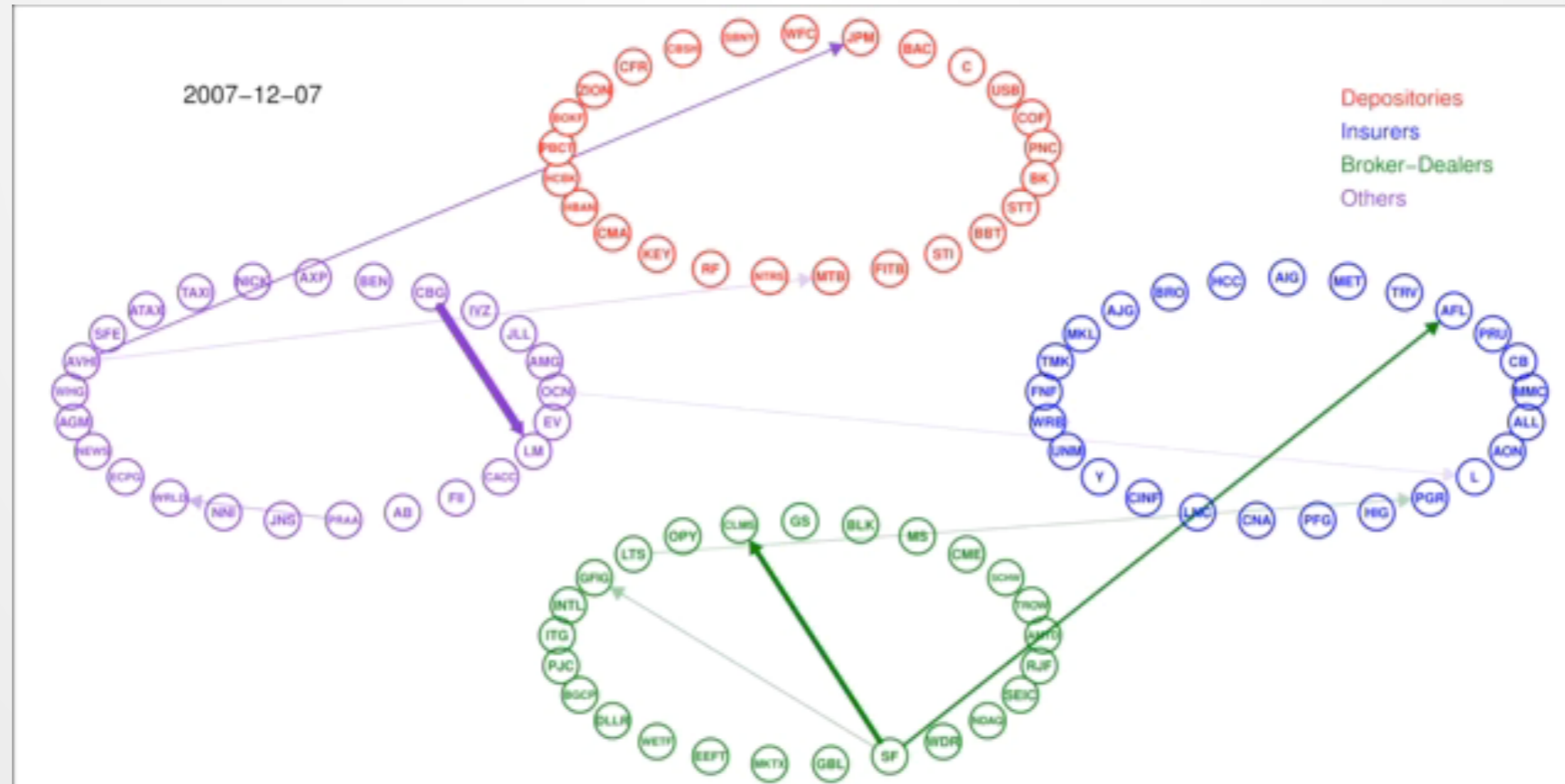
Brandenburg University of Technology

University of Glasgow

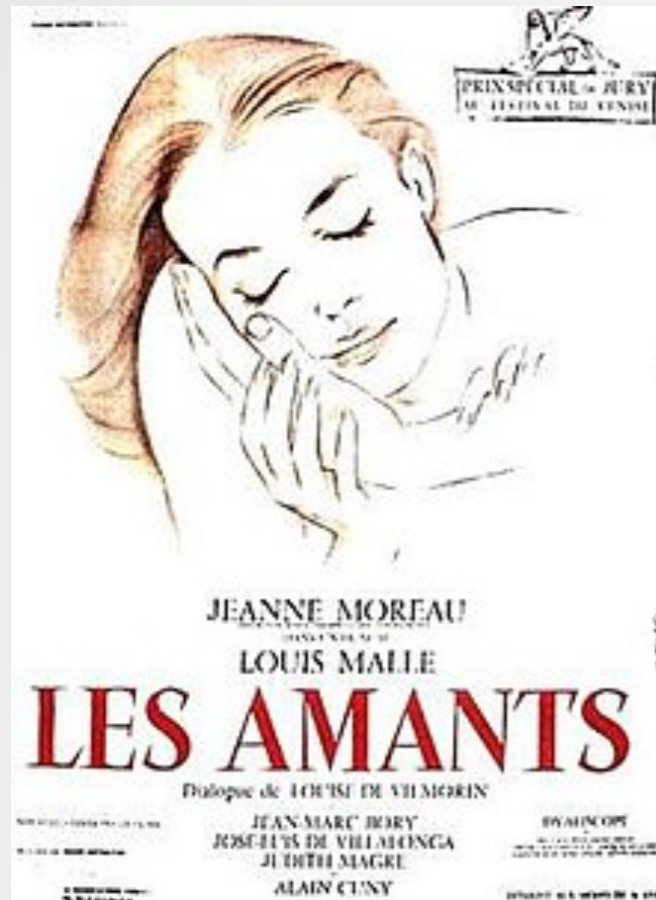


## Tail Events (TE)

- TEs across companies indicate increased risk
- CoVaR measures joint TEs between 2 risk factors
- CoVaR and other risk factors?
- TENET Tail Event NETwork risk, Härdle Wang Yu (2017) J E'trics
- FRM Financial Risk Meter for joint TEs



# Risk, Model Risk, Systemic Risk



The financial cycle and the business cycle are not synchronised, implying that risks can emerge especially in the periods of „disconnect” between the two cycles.”, Vítor Constâncio, VP ECB, 2015

“Broadly speaking, model risk can be attributed to either an incorrect model or to an incorrect implementation of a model” , Buraschi and Coriello (2005)

„I know it when I see it“, Justice Potter Stewart (1964)

- Tail Behaviour
- Ultra High Dimensions
- Nonlinear in Time and Space (=Network)

## Risk Measures

- ▣ VIX: IV based, does not reflect joint TEs
- ▣ CoVaR concentrates on a pair of risk factors
- ▣ NBER recession indicator, Google trends, SRISK, ...
- ▣ FRM employs the full picture of TE dependencies
- ▣ [HU.berlin/FRM](http://HU.berlin/FRM) **financialriskmeter**



# Outline

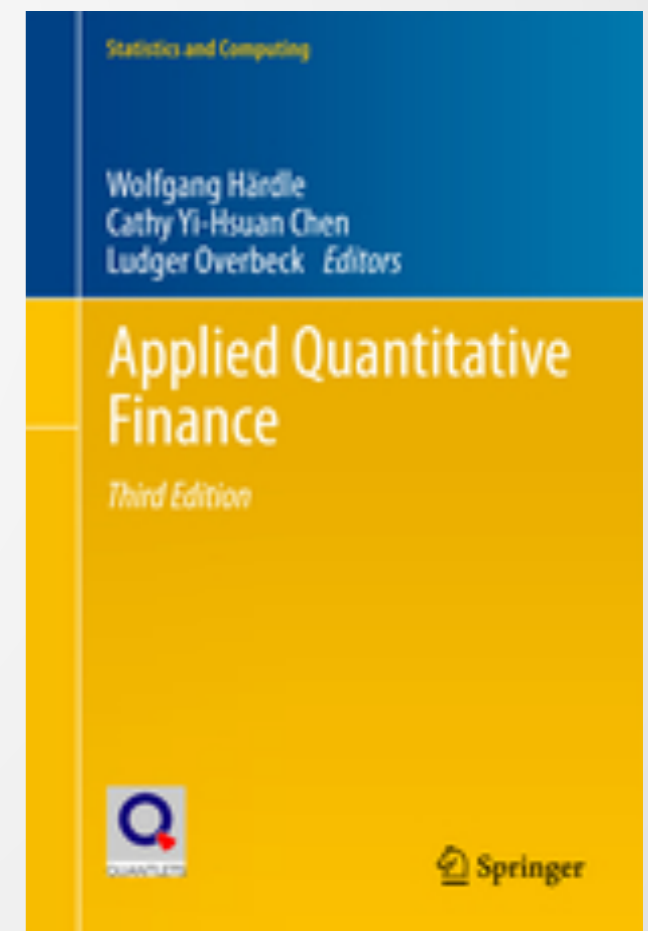
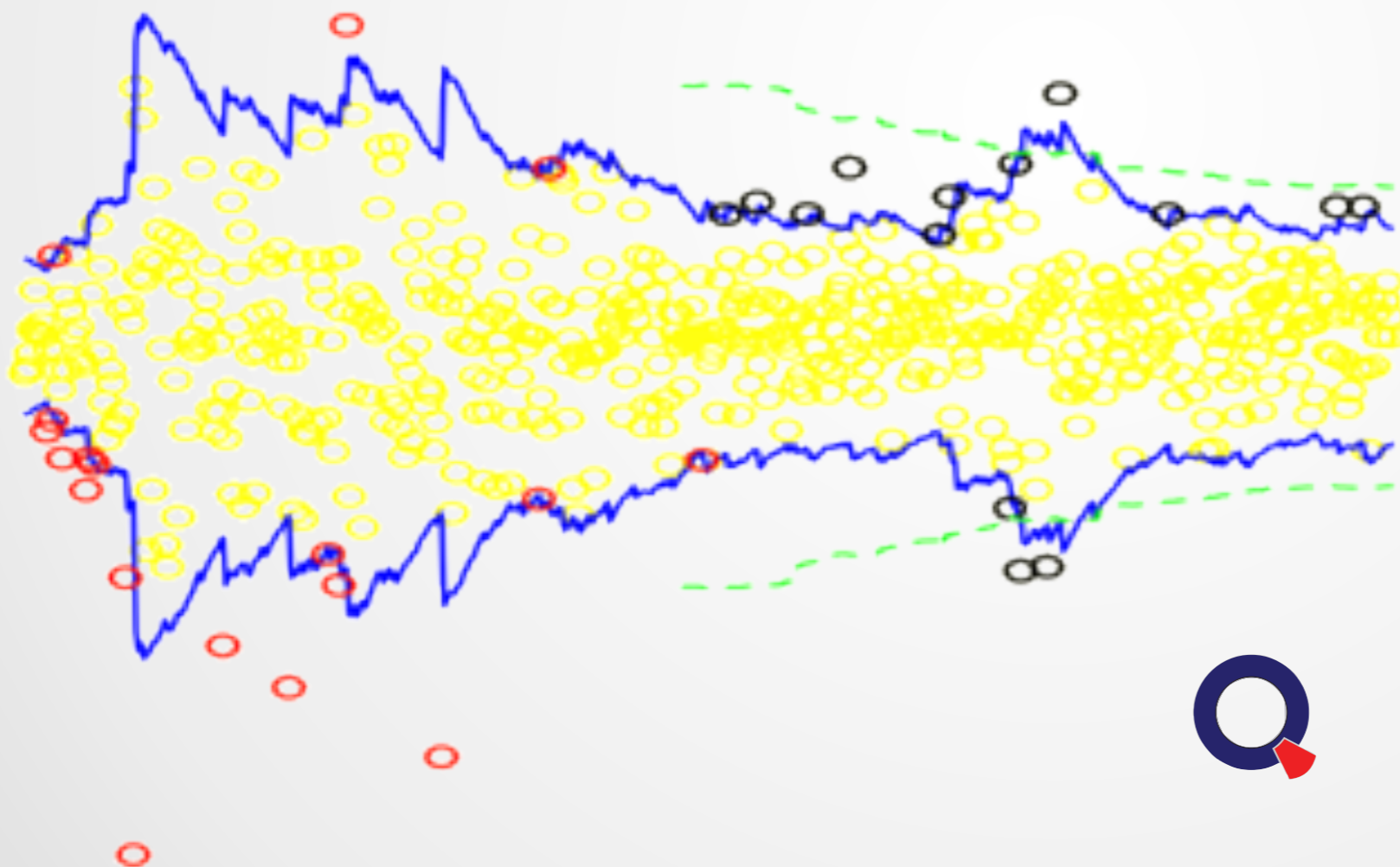
1. Motivation ✓
2. Genesis
3. FRM Framework
4. CoStress ID
5. FRM a predictor for recession
6. Conclusions

## VaR Value at Risk

- ▣ Probability measure based

$$P(X_{i,t} \leq VaR_{i,t}^{\tau}) \stackrel{def}{=} \tau, \quad \tau \in (0,1)$$

- ▣  $X_{i,t}$  log return of risk factor (company)  $i$  at  $t$
- ▣ VaRs (0.99, 0.01) based on **RMA**, **Delta Normal Method**



## Quantiles and Expectiles

For r.v.  $Y$  obtain tail event measure:

$$q^\tau = \arg \min_{\theta} E \{ \rho_\tau (Y - \theta) \}$$

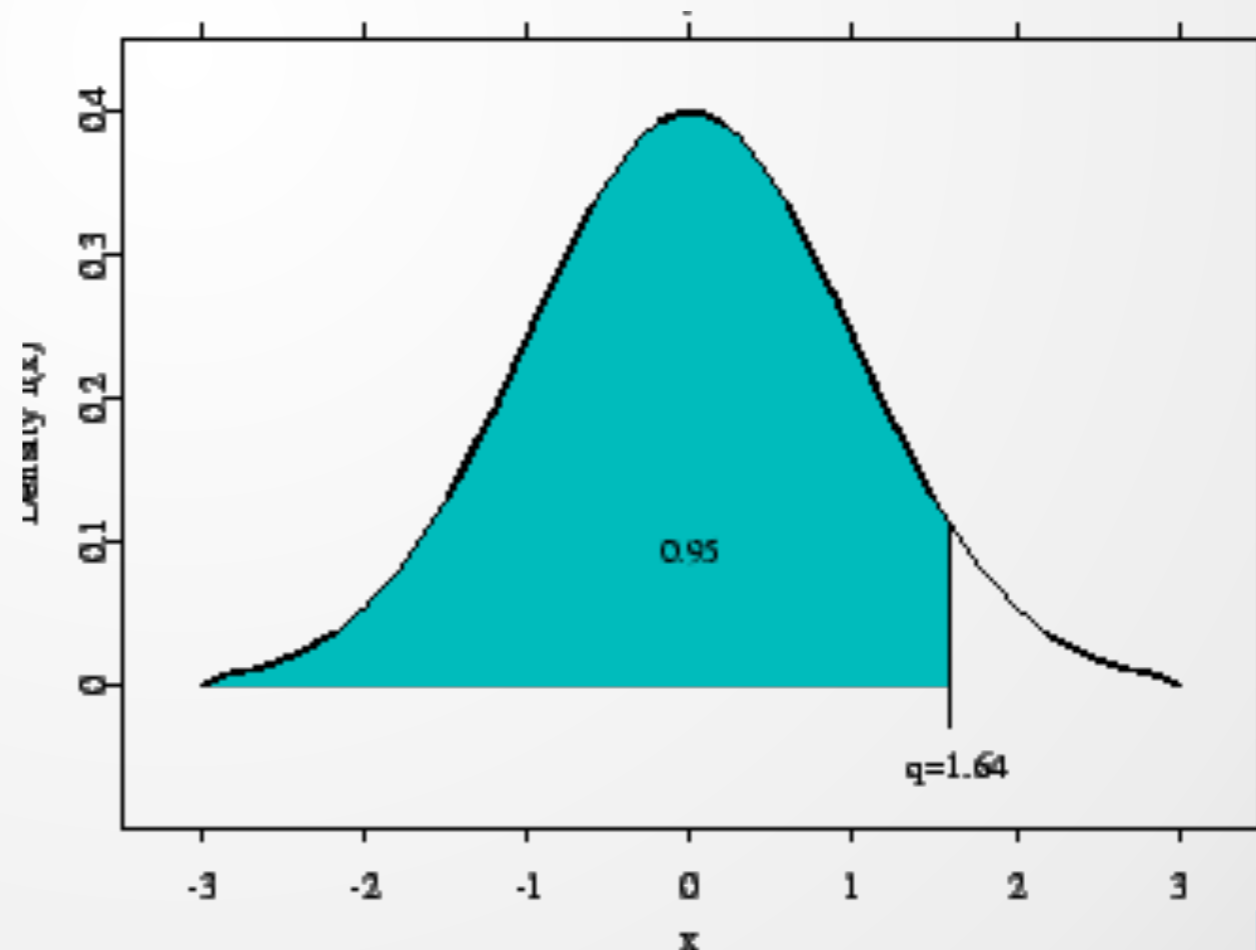
*log returns*

asymmetric loss function

$$\rho_\tau (u) = |u|^\alpha \left| \tau - \mathbf{I}_{\{u < 0\}} \right|$$

$\alpha = 1$  for quantiles,  
 $\alpha = 2$  for expectiles

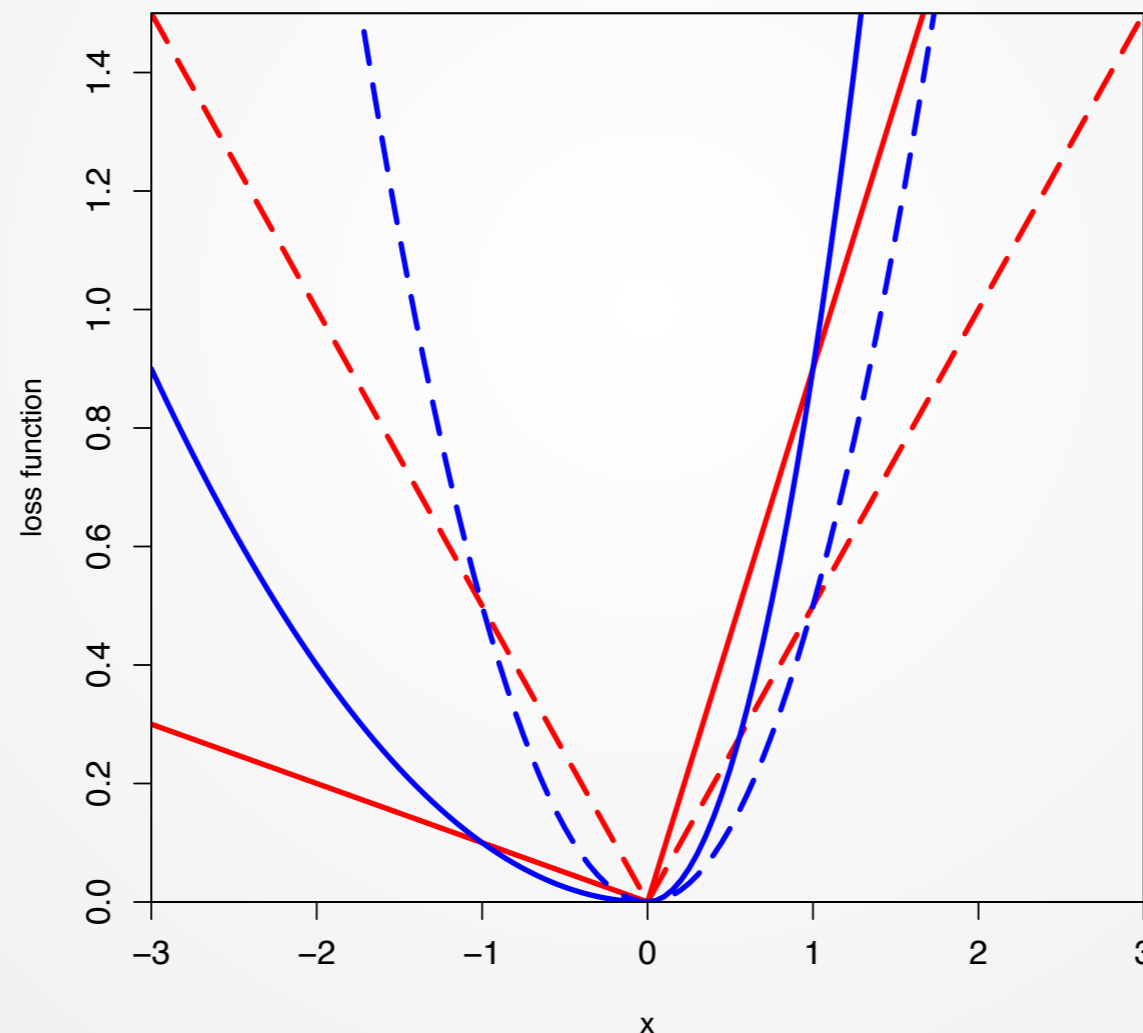
$\tau = 0.05$



Expectile as Quantile

# Quantiles and Expectiles

- Quantiles/Expectiles focus on TEs
- SRM Spectral Risk Measures
- LAWS algorithm fast and efficient



 LQRcheck

Figure: Loss function of **expectiles** and **quantiles** for  $\tau = 0.5$  (dashed) and  $\tau = 0.9$  (solid)

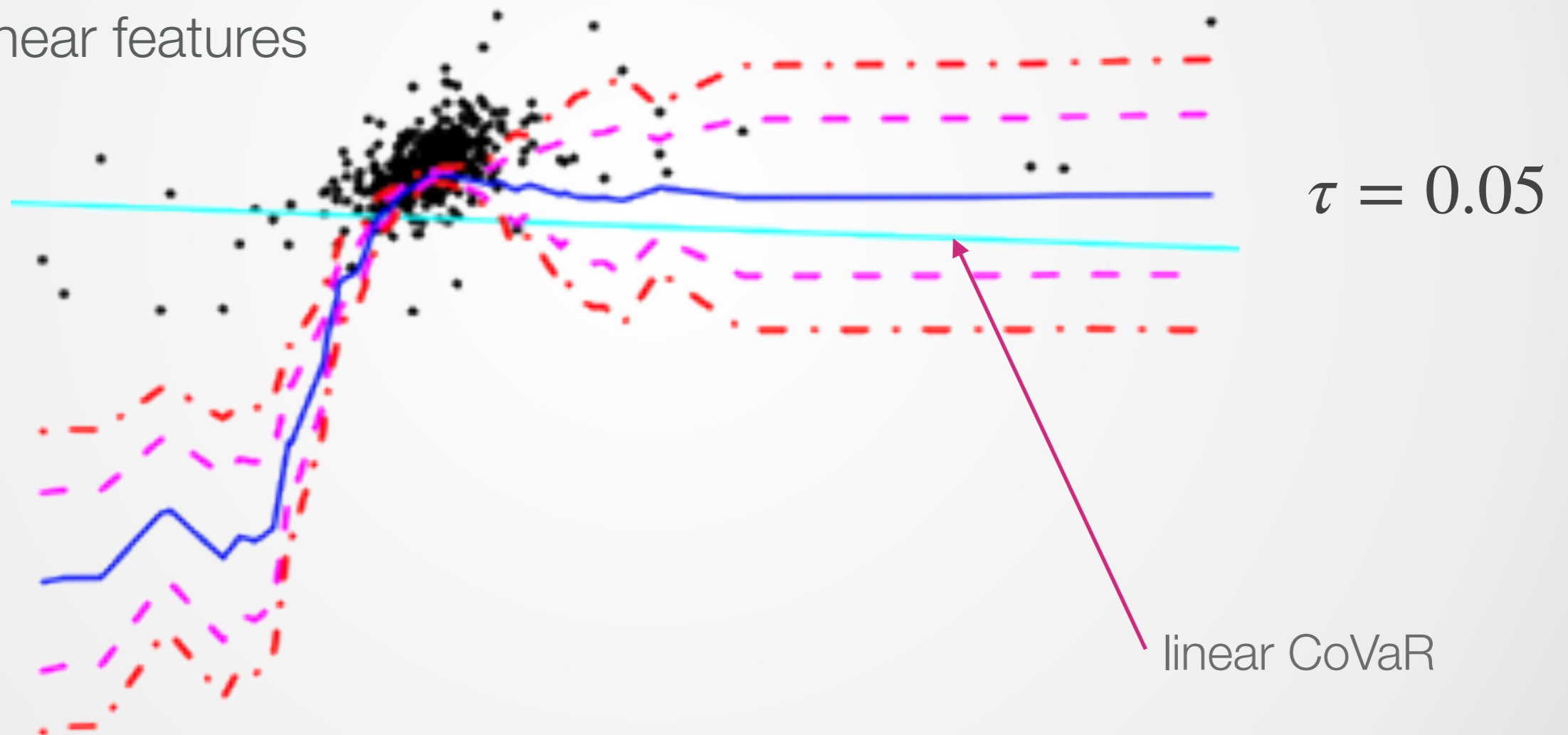


## Conditional Value at Risk

- Adrian and Brunnermeier (2016) introduced CoVaR

$$P\{X_{i,t} \leq CoVaR_{j|i,t}^\tau \mid X_{i,t} = VaR^\tau(X_{i,t}), M_{t-1}\} \stackrel{def}{=} \tau,$$

- $M_{t-1}$  vector of macro-related variables
- Nonlinear features



Goldman Sachs (Y), Citigroup (X), Conf Bands, Chao et al (2015)

## CoVaR and the magic of joint TEs

- CoVaR technique

$$X_{i,t} = \alpha_i + \gamma_i^\top M_{t-1} + \varepsilon_{i,t},$$

$$X_{j,t} = \alpha_{j|i} + \beta_{j|i} X_{i,t} + \gamma_{j|i}^\top M_{t-1} + \varepsilon_{j,t}.$$

- $F_{\varepsilon_{i,t}}^{-1}(\tau | M_{t-1}) = 0$  and  $F_{\varepsilon_{j,t}}^{-1}(\tau | M_{t-1}, X_{i,t}) = 0$

$$\widehat{VaR}_{i,t}^\tau = \hat{\alpha}_i + \hat{\gamma}_i^\top M_{t-1},$$

$$\widehat{CoVaR}_{j|i,t}^\tau = \hat{\alpha}_{j|i} + \hat{\beta}_{j|i} \widehat{VaR}_{i,t}^\tau + \hat{\gamma}_{j|i}^\top M_{t-1},$$

CoVaR: First calculate VaRs, then compute the TE given a stressed risk factor.

## Linear Quantile Lasso Regression

$$X_{j,t}^s = \alpha_{j,t}^s + A_{j,t}^{s\top} \beta_j^s + \varepsilon_{j,t}^s, \quad (1)$$

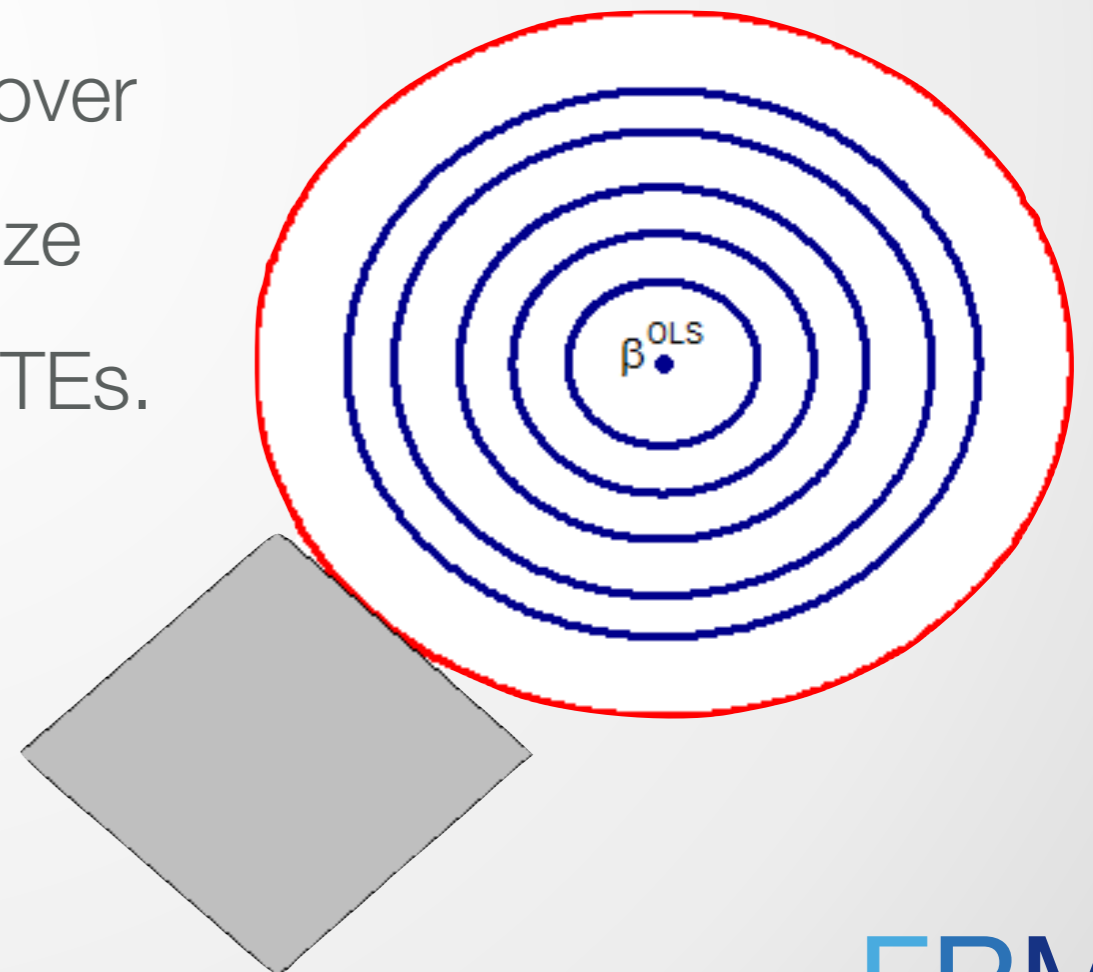
- Where  $A_{j,t}^{s\top} \stackrel{\text{def}}{=} [M_{t-1}^s, X_{-j,t}^s]$
- $X_{-j,t}^s$  log returns of all other firms except  $j$  at time  $t$
- $s$  length of moving window
- $M_{t-1}^s$  log return of macro prudential variable at time  $t - 1$
- Application  $j = 1, \dots, J, t = 2, \dots, T$   
 $J = 100, T = 2700, s = 63$

[Company List](#)[Macroprudentials](#)

# Lasso Quantile Regression

$$\min_{\alpha_j^s, \beta_j^s} \left\{ n^{-1} \sum_{t=s}^{s+(n-1)} \rho_{\tau}(X_{j,t}^s - \alpha_j^s - A_{j,t}^{s\top} \beta_j^s) + \lambda_j^s \|\beta_j^s\|_1 \right\}, \quad (2)$$


- ▣ Check function  $\rho_{\tau}(u) = |u|^c |1(u \leq 0) - \tau|$ ,
- ▣ here  $c = 1, 2$  correspond to quantile, expectile regression
- ▣  $\lambda$  creates size of „active set“, i.e. spillover
- ▣  $\lambda$  is sensitive to residual size, i.e. TE size
- ▣  $\lambda$  reacts to singularity issues, i.e. joint TEs.



## $\lambda$ Role in Linear Lasso Regression

- Penalisation (Lagrange) parameter  $\lambda$  , Osborne et al. (2000)
- Dependence, time-varying, company-specific
- Size of model coefficients depends on

$$\lambda = \frac{(Y - X\beta(\lambda))^T X\beta(\lambda)}{\|\beta\|_1}$$


  
Coeff's depend on  $\lambda$

- Penalty  $\lambda$  depends on:
- **residual size, condition of design matrix, active set**

## $\lambda$ Role in Linear Quantile Regression

- $\lambda$  size of estimated LQR coefficients

$$\lambda = \frac{(\alpha - \gamma)^\top X\beta(\lambda)}{\|\beta\|_1}$$


  
Coeff's ( $\lambda$ )

$$(\alpha - \gamma) = \tau I(Y - X\beta(\lambda) > 0) + (\tau - 1) I(Y - X\beta(\lambda) < 0)$$

- Penalty  $\lambda$  depends on:
- **residual size, condition of design matrix, active set**
- Average penalty: an indicator for tail risk

$$FRM_t \stackrel{def}{=} J^{-1} \sum_{j=1}^J \lambda_{jt}$$

- The **FRM** time series is ONE index for joint TEs!

## $\lambda$ Selection

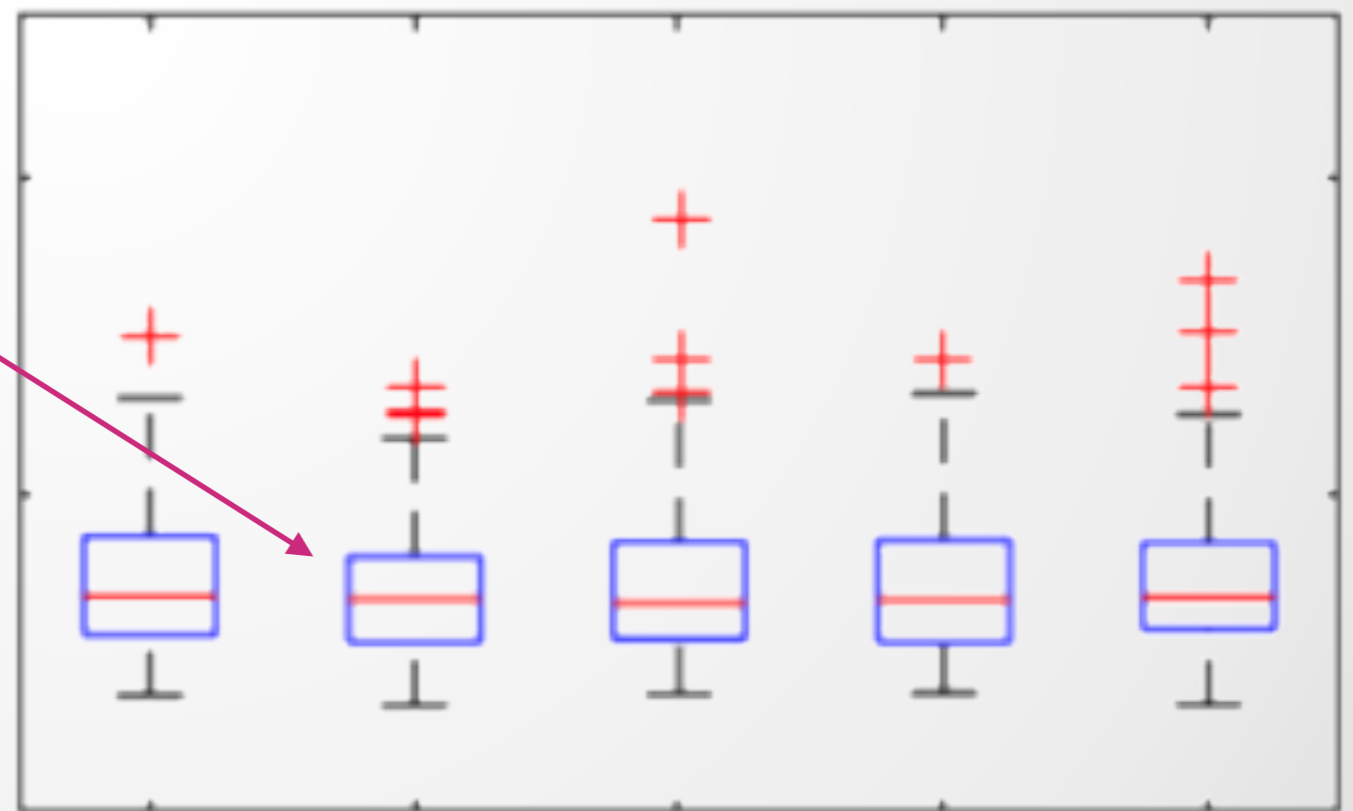
- Generalized approximate cross-validation (GACV)

$$\min GACV(\lambda_j^s) = \min \frac{\sum_{t=s}^{s+(n-1)} \rho_\tau(X_{j,t}^s - \alpha_j^s - A_{j,t}^{s,T} \beta_j^s)}{n - df}$$



Coeff's depend on  $\lambda$

- $df$  degrees of freedom
- $\lambda$  is a function of  $j, t$
- Distribution of  $\lambda_{j,t}$
- ID the TE drivers



# FRM codes

[hu.berlin/frm](http://hu.berlin/frm)



severe risk of crisis

high risk of crisis

elevated risk of crisis

general risk of crisis

X low risk of crisis

<b>Low Risk</b>	<b>&lt;20%</b>
<b>General Risk</b>	<b>20% - 40%</b>
<b>Elevated Risk</b>	<b>40% - 60%</b>
<b>High Risk</b>	<b>60% - 80%</b>
<b>Severe Risk</b>	<b>&gt;80%</b>



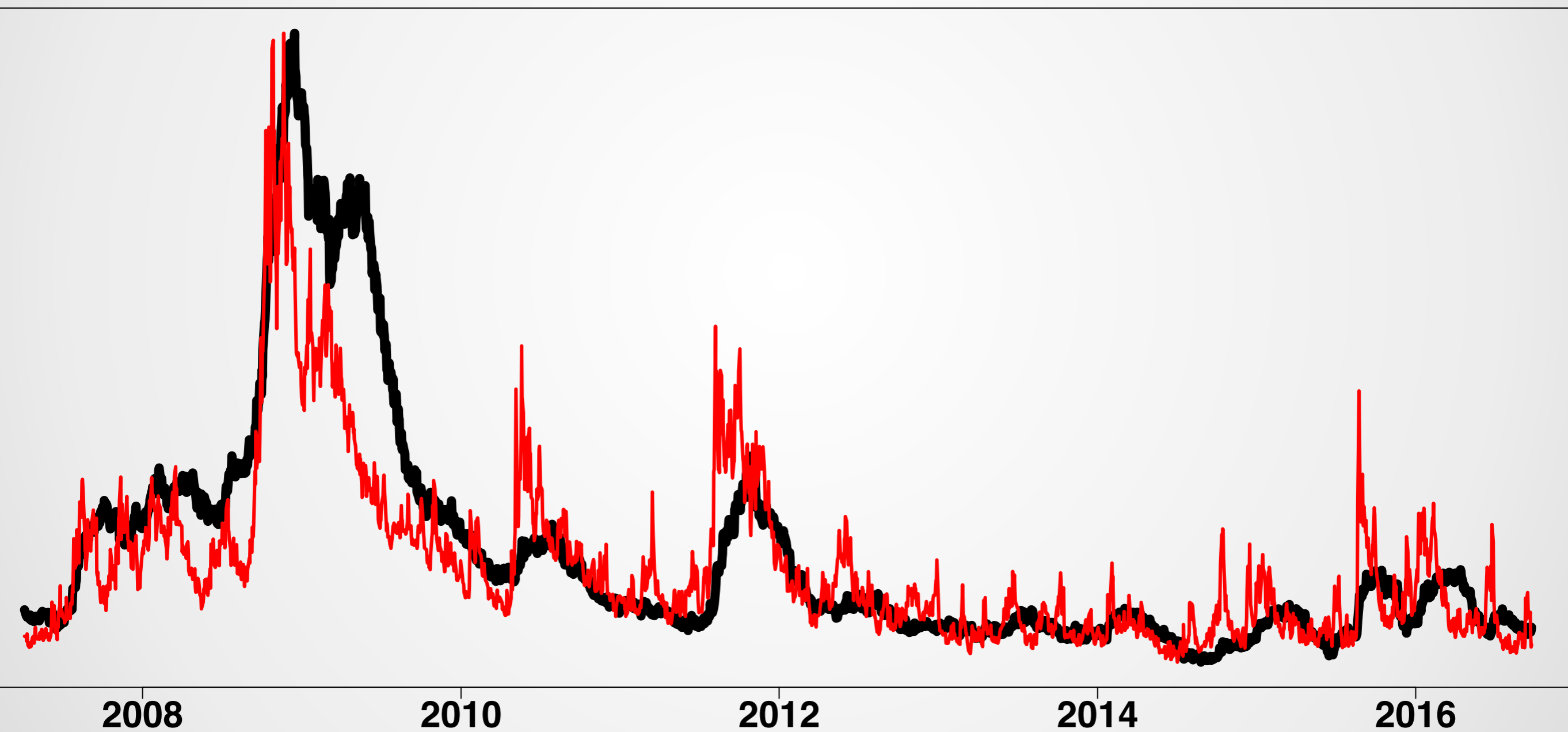
## Data

- ▣ 100 largest U.S. publicly traded financial institutions
- ▣ 6 macro related variables
- ▣ Quantile level  $\tau = 0.05, \tau = 0.01, \dots$
- ▣ Time frame: 01.04.2007 - 15.03.2019
- ▣ Macroeconomics CBOE Volatility Index,  $\wedge VIX$   
S&P 500,  $\wedge GSPC$   
iShares US Real Estate ETF, IYR  
3M Treasury Constant Maturity Rate, DGS3MO  
10Y Treasury Constant Maturity Rate, DGS10  
Moody's Seasoned Baa Corp Bond Yield, DBAA

LQ Lasso Regression

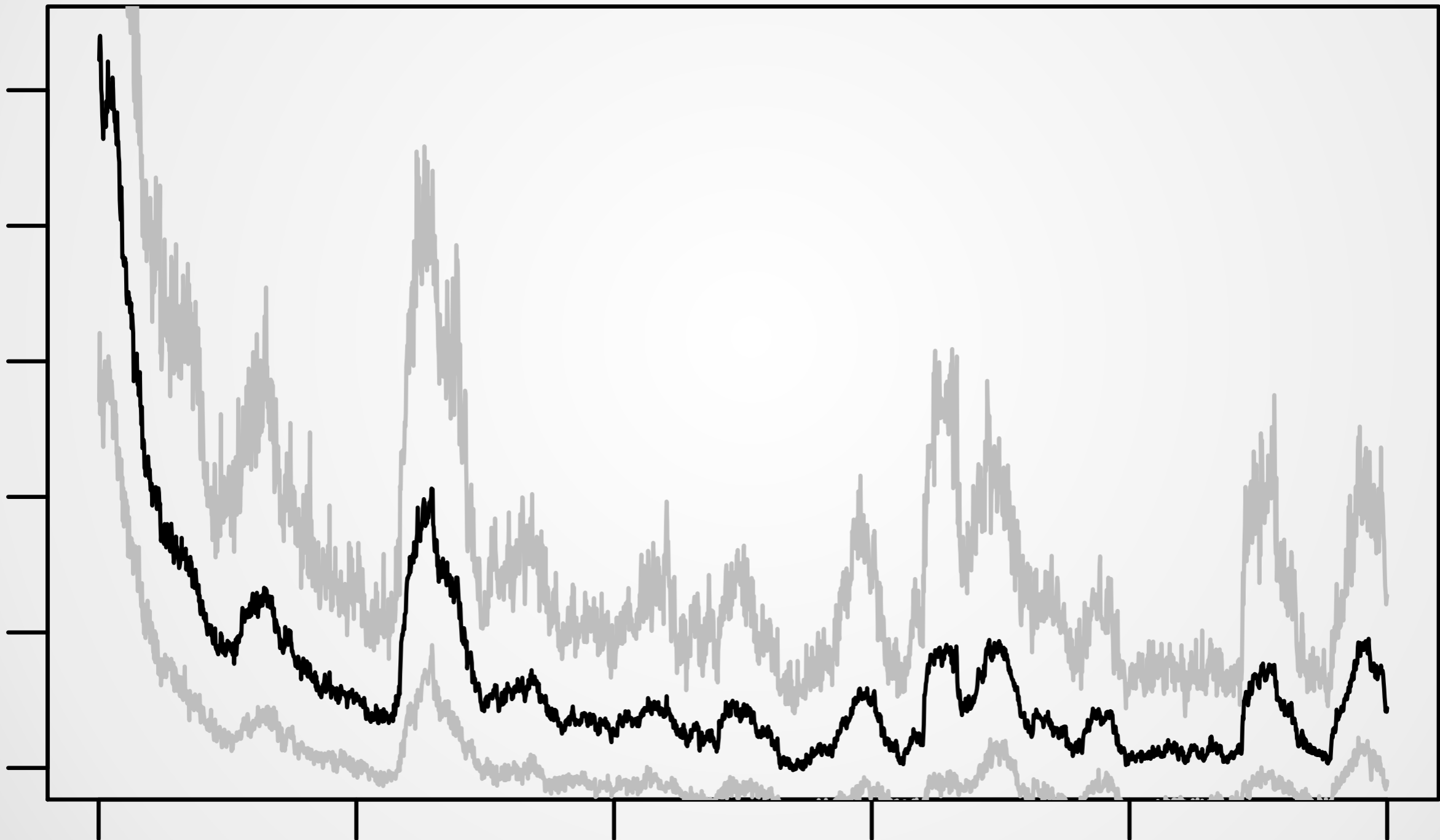
# FRM vs VIX

- The evolution of **FRM** relative to **VIX**



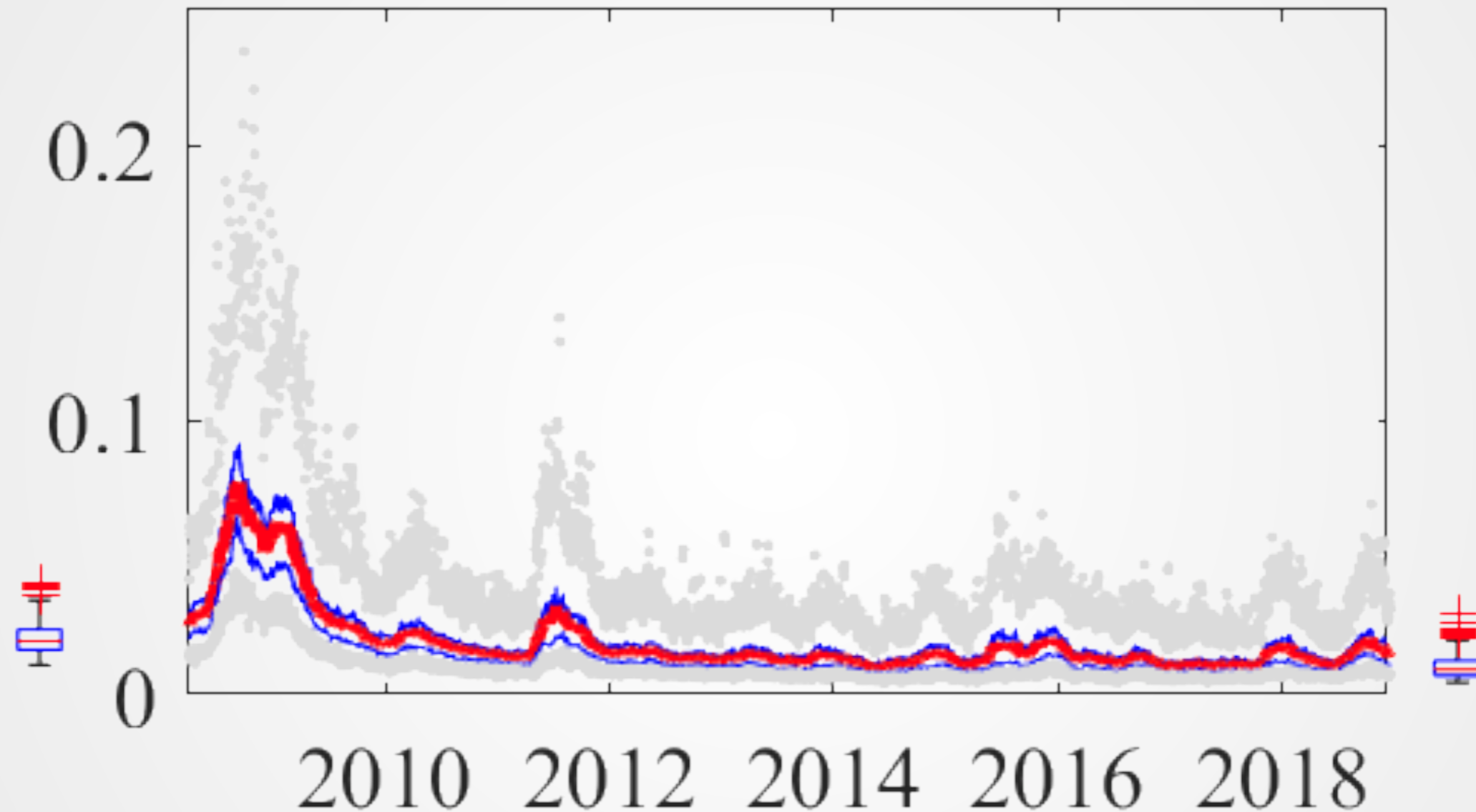
# Confidence band

- ▣ 95% and 5%



## Distributional characteristics

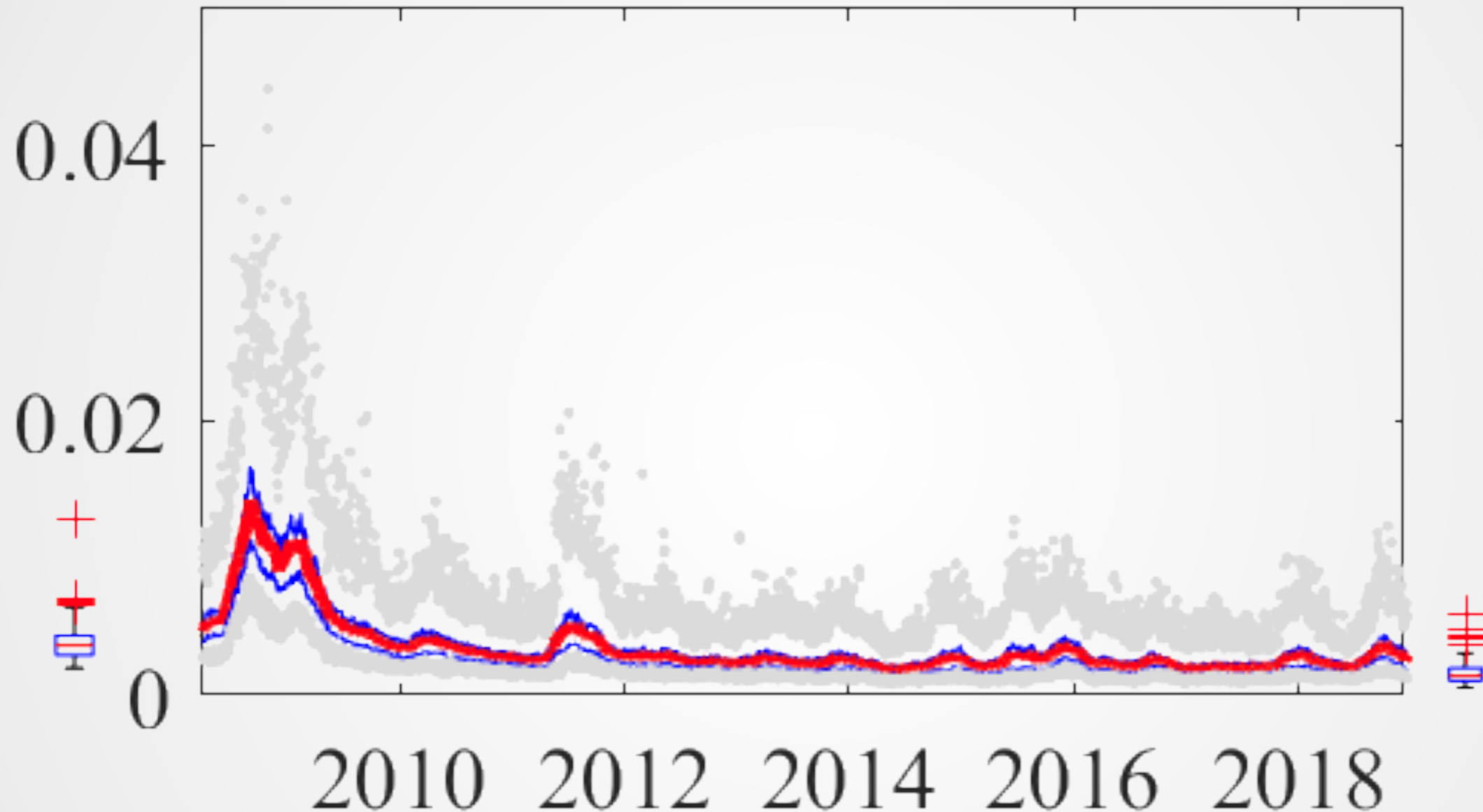
- Identifying companies CoStress  $\tau = 0.05$



Distributional characteristics of  $\lambda_j, j = 1, \dots, J$   
20080402 (left boxplot), 20190327 (right boxplot);  
FRM, quartiles and extremes.

## Distributional characteristics

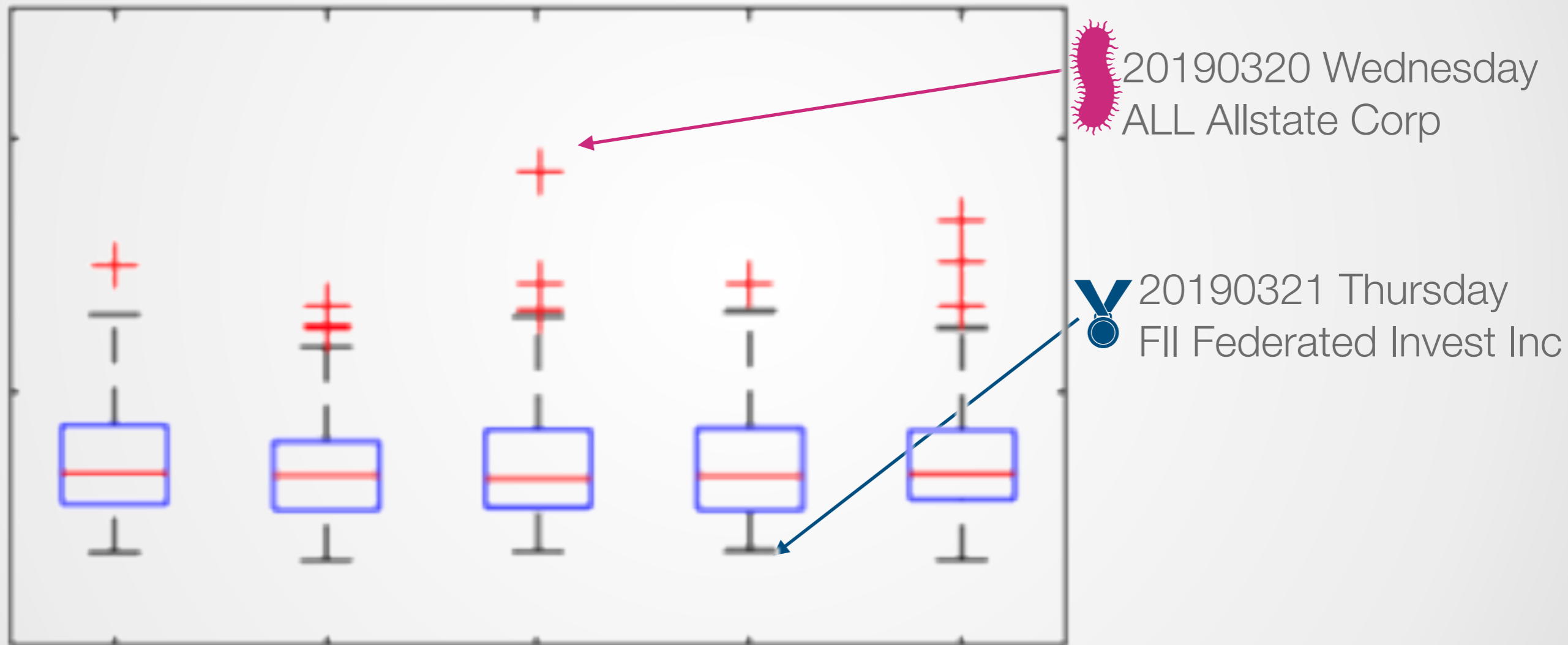
- Identifying companies CoStress  $\tau = 0.01$



Distributional characteristics of  $\lambda_j, j = 1, \dots, J$   
20080402 (left boxplot), 20190327 (right boxplot);  
FRM, quartiles and extremes.

## CoStress IDs

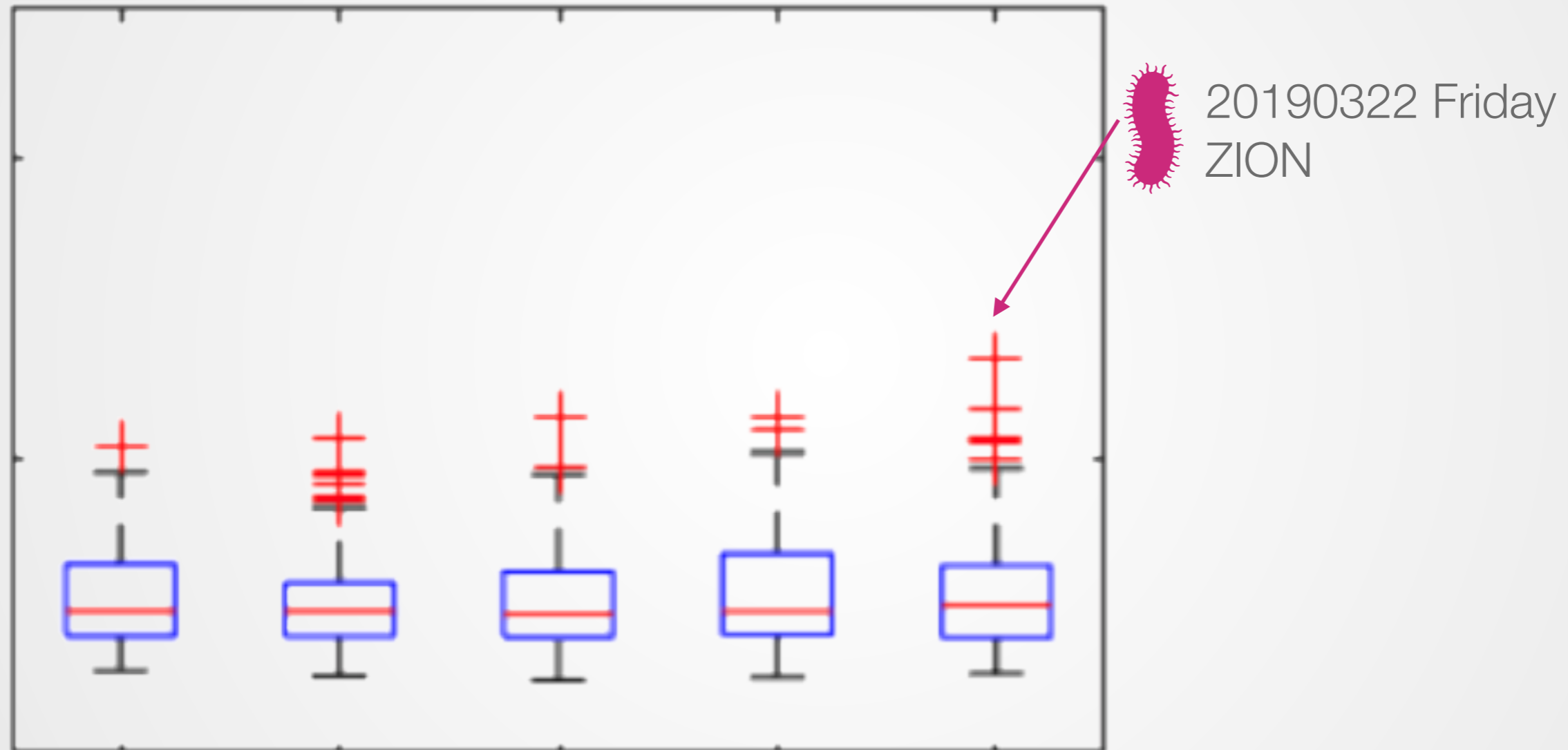
- ID CoStress via size of  $\lambda_j, j = 1, \dots, J$   $\tau = 0.05$



Boxplots from 20190318 to 20190322. Max CoStress: FITB, ZION, ALL, AFG, ZION. Min CoStress: LM, AMG, AMG, FII, FII

## CoStress IDs

- ID CoStress via size of  $\lambda_j, j = 1, \dots, J$   $\tau = 0.01$



Boxplots from 20190318 to 20190322. Max CoStress: ZION, ZION, UNM, AFG, ZION. Min CoStress: EFX, AMG, LM, MORN, LM.

## TOP Extreme CoStress

- TOP 5 companies exhibiting extreme CoStress  $\tau = 0.05$

Maximal		Minimal	
BBT	94	CACC	172
MS	86	SEB	159
RJF	83	MKTX	103
STI	75	WTM	99
AMP	68	OZM	97

TOP 5 companies: # days of CoStress all companies from 20080402 to 20190327 (2700 trading days)



## TOP Extreme CoStress

- TOP 5 companies exhibiting extreme CoStress  $\tau = 0.01$

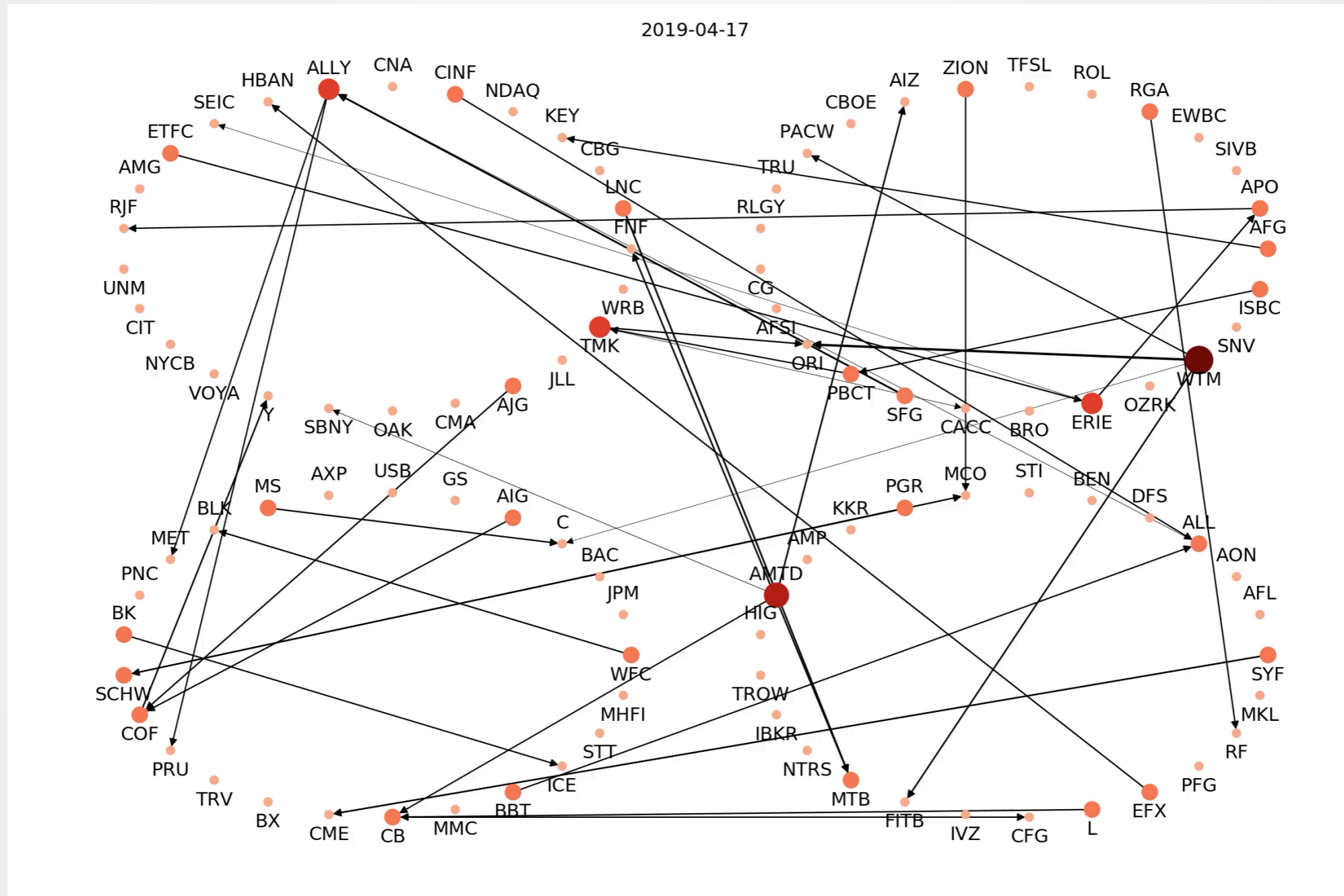
Maximal		Minimal	
STI	92	CACC	113
SNV	71	SEB	114
IVZ	69	OZM	111
BBT	67	MKTX	100
RJF	64	MORN	73

TOP 5 companies: # days of CoStress all companies from 20080402 to 20190327 (2700 trading days)

# Network Dynamics

▣ 100 risk factors

$\tau = 0.05$



Coeffs of all companies from 20190417 to 20190426

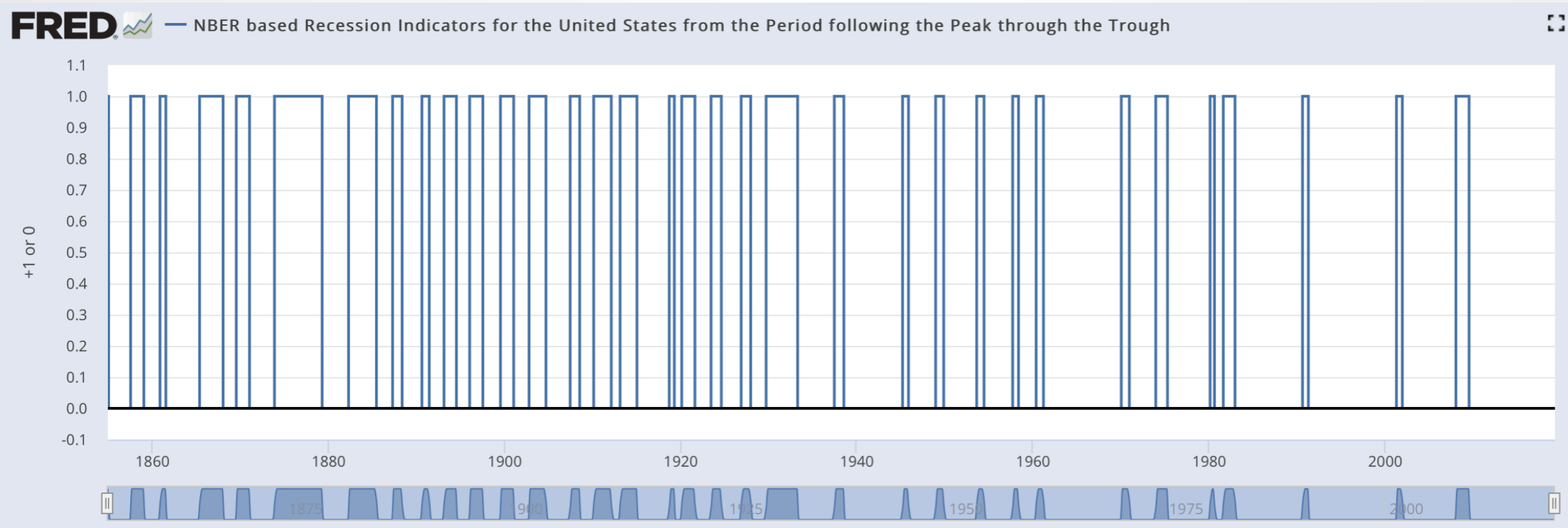
## FRED meets FRM

- Logistic linear regression

$$\log \frac{P(y = 1 | x; \beta)}{P(y = 0 | x; \beta)} = \beta_0 + \beta_1 x$$

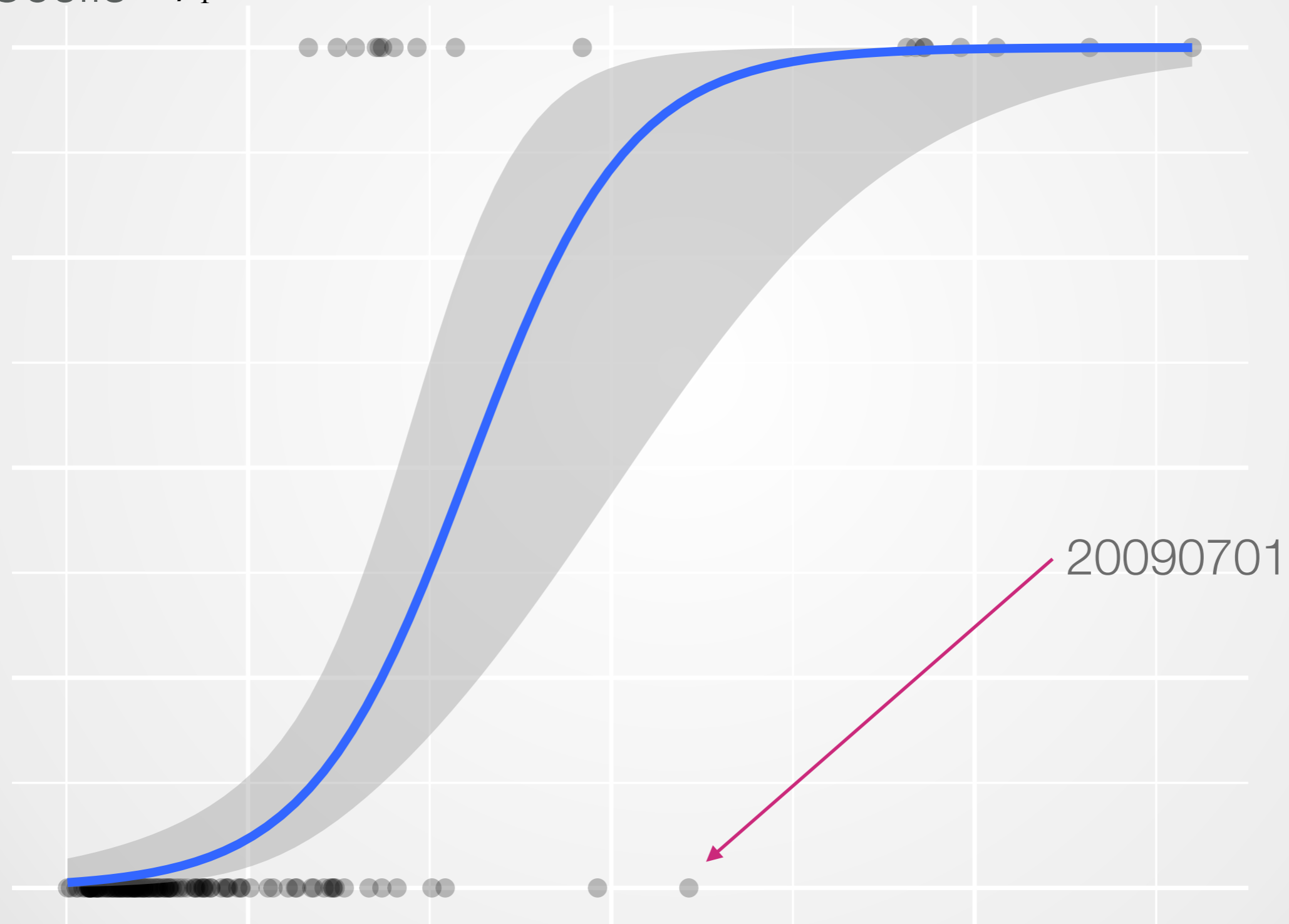
$y$  National Bureau of Economic Research (NBER) recession indicator

$x$  FRM



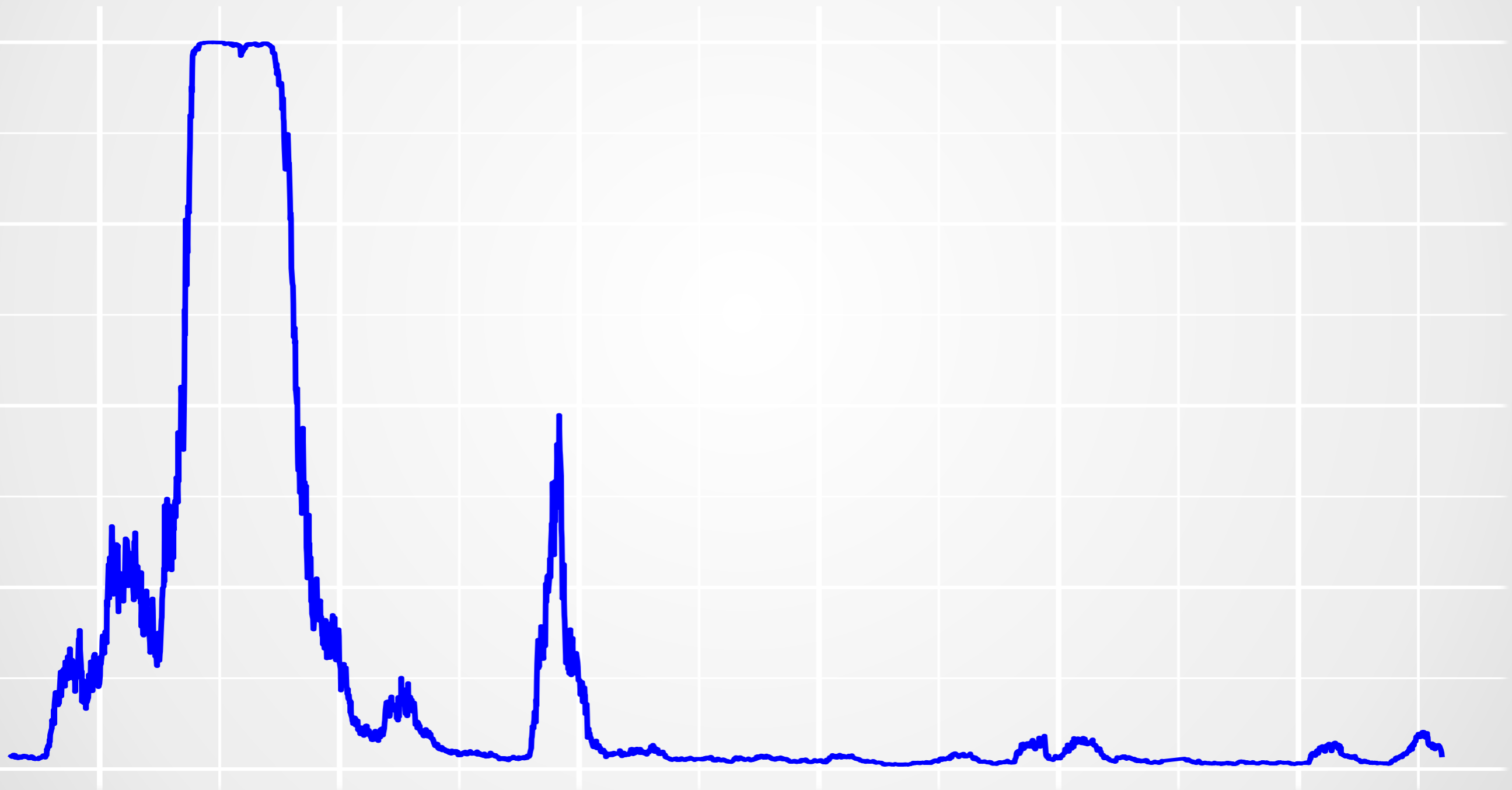
## Result

□ Coeffs  $\beta_1 = 215.5$   $\beta_0 = -5.8$   $\tau = 0.05$



# Implied recession probability

- FRM scales



## Extensions

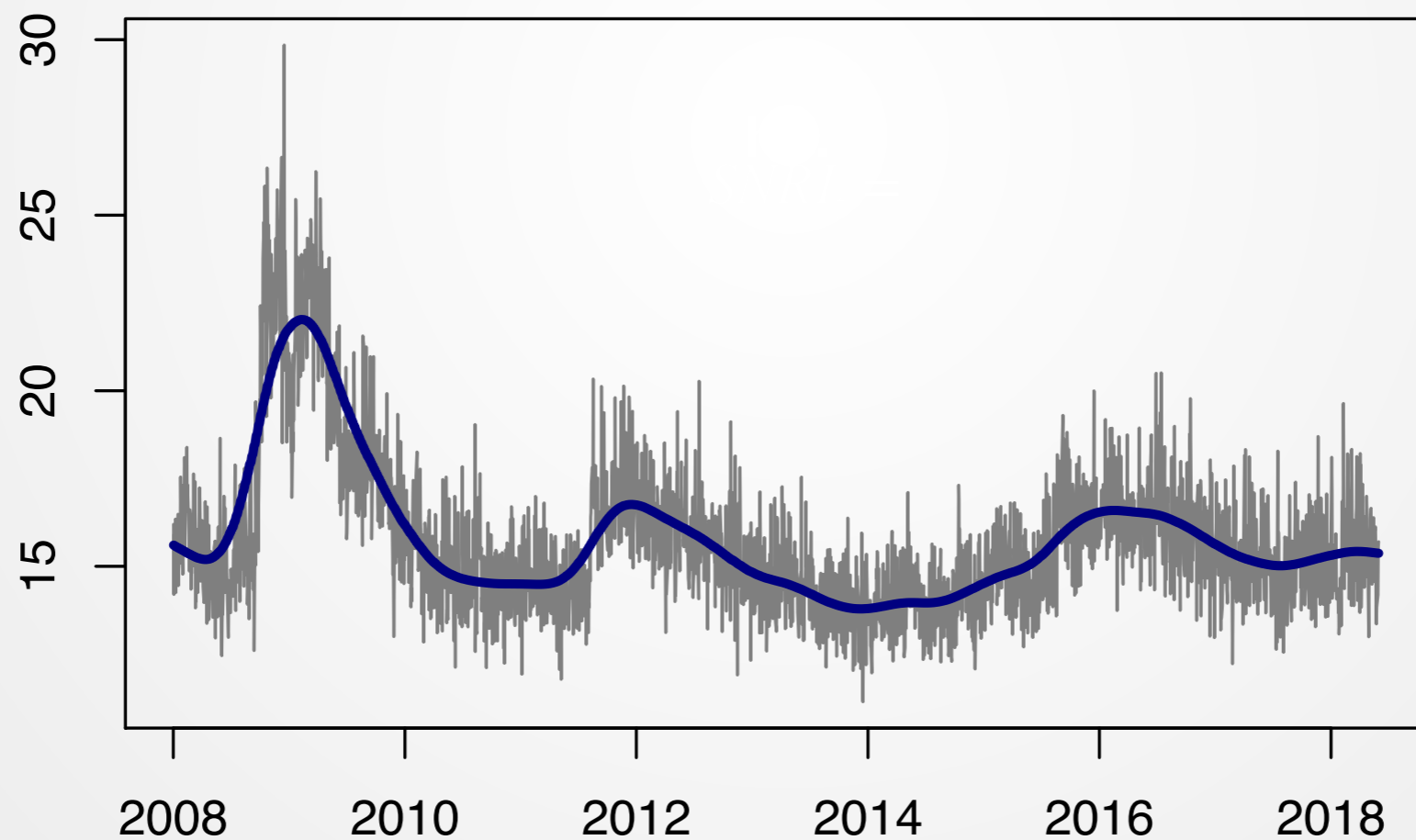
- Use national or EU data to construct localised **FRM**
- Adaptive LASSO
- Global contagion effect of FRMs
- Relate Network Centrality to Max/Min CoStress nodes
- Besides equal weights, weights by degree of centrality
- LASSO in Time and Space
- Aggregate global FRMs



## Extensions: Neural Network CoVaR (Keilbar, 2018)

- *Systemic Network Risk Index (SNRI)* measures total systemic risk
- Incorporates bivariate risk spillover effects  $a_{ji,t}$

$$SNRI_t = \sum_{j=1}^k \sum_{i=1}^k (1 + |\text{VaR}_{i,t}^\tau|)(1 + |\text{CoVaR}_{j,t}^\tau|) \cdot a_{ji,t}$$



## Extensions: Neural Network CoVaR (Keilbar, 2018)

- *Systemic Hazard Index (SHI)* measures the risk of bank  $i$  imposes to the financial system

$$SHI_{i,t} = \sum_{j=1}^k (1 + |\text{CoVaR}_{j,t}^{\tau}|) \cdot a_{ji,t}$$

- *Systemic Fragility Index (SFI)* measures the exposure of bank  $j$  to the financial system

$$SFI_{i,t} = \sum_{i=1}^k (1 + |\text{VaR}_{i,t}^{\tau}|) \cdot a_{ji,t}$$

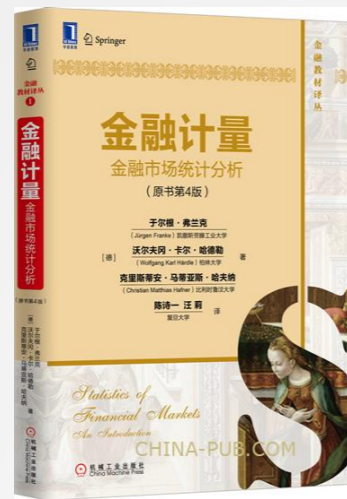
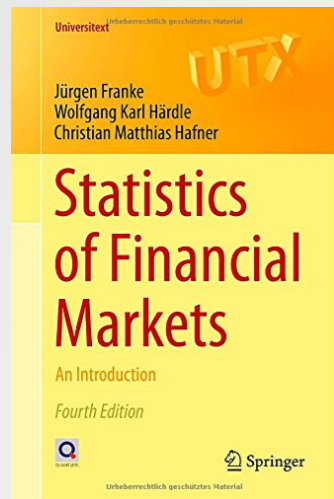




## Conclusions

- ▣ **FRM financialriskmeter** = Flexible Risk Meter
- ▣ **FRM** has systemic risk components
- ▣ **FRM** predicts recession periods
- ▣ **FRM** can be tuned to any TE risk
- ▣ **FRM** reacts to coagulation of risk emitters via active set

# FRMs in FinTech, Cryptos, ...



## Vol 1. 2019 on Crypto Currencies



Volume 1 • Number 1 • January 2019

42521 Digital Finance

EDITORS: Wolfgang Karl Härdle and Steven Kou

# Digital Finance

Smart Data Analytics, Investment Innovation, and Financial Technology

Volume 1 • Number 1 • January 2019 • pp. 1–xx



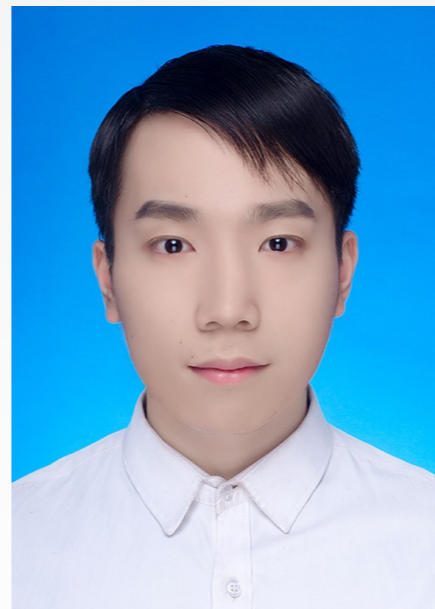
# Advisors



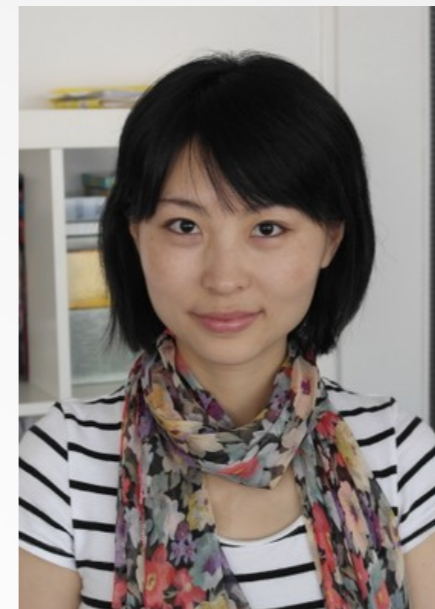
Georg Keilbar



Alla Petukhina



Keyan LIU



Lining YU



Weining WANG



Jochen Papenbrock

# FRM Team



Cathy YH CHEN



Wolfgang K Härdle



Andrija Mihoci



Michael Althof

# FRM financialriskmeter

Andrija Mihoci

Cathy Yi-Hsuan Chen

Wolfgang Karl Härdle

Michael Althof

# FRM

Ladislaus von Bortkiewicz Chair of Statistics  
Humboldt-Universität zu Berlin

[lvb.wiwi.hu-berlin.de](http://lvb.wiwi.hu-berlin.de)

Brandenburg University of Technology

University of Glasgow



## References

- ▣ Adrian J, Brunnermeier M (2016) CoVaR, *American Economic Review*, 106 (7): 1705-41, DOI: [10.1257/aer.20120555](https://doi.org/10.1257/aer.20120555)
- ▣ Buraschi A, Coriello F (2005). Risk management of time-inconsistency: Model updating and recalibration of no-arbitrage models. *J Banking and Finance* 29: 2883–907
- ▣ Chao SK, Härdle WK, Wang W (2015) Quantile Regression in Risk Calibration. in *Handbook for Financial Econometrics and Statistics*, Cheng-Few Lee, ed., Springer Verlag, DOI: [10.1007/978-1-4614-7750-1\\_54](https://doi.org/10.1007/978-1-4614-7750-1_54).
- ▣ Härdle WK, Wang W, Zbonakova L (2018) Time Varying Lasso, in *Applied Quantitative Finance* 3rd ed, (Chen, Härdle, Overbeck eds.) Springer Verlag, ISBN 978-3-662-54486-0
- ▣ Keilbar G (2018) Modeling systemic risk using Neural Network Quantile Regression, [MSc thesis](#)
- ▣ Osborne MR, Presnell B, Turlach BA (200) *J Comp Graphical Statistics* Vol. 9, 319-337
- ▣

## Expectile as Quantile

$e_\tau(Y)$  is the  $\tau$ -quantile of the cdf  $T$ , where

$$T(y) = \frac{G(y) - xF(y)}{2\{G(y) - yF(y)\} + \{y - \mu_Y\}}$$

and

$$G(y) = \int_{-\infty}^y u dF(u)$$

[Back to Expectiles](#)

# Company List



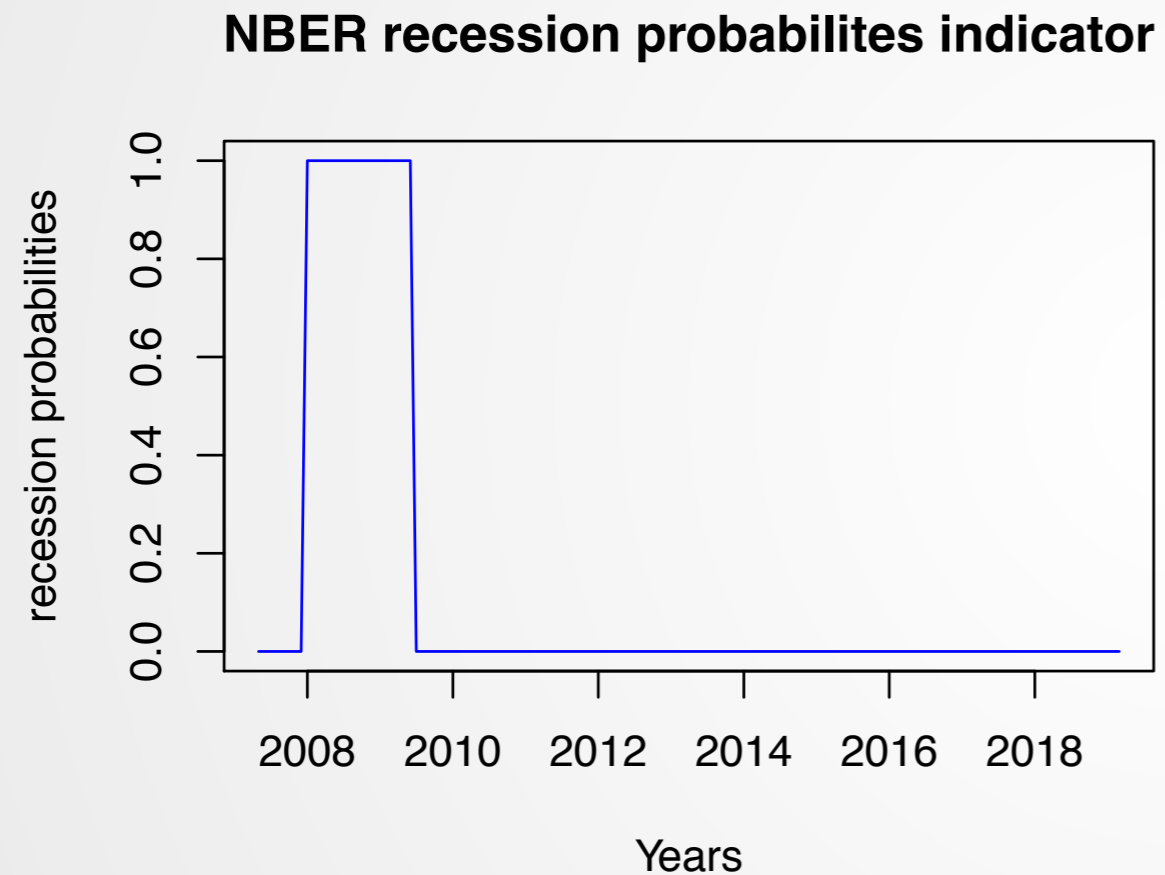
Symbol	Name	LastSale	MarketCap	ADR TSO	IPOyear	Sector	Industry	Summary Quote
<b>WFC</b>	Wells Fargo & Company	51.88	2.65E+11	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/wfc">http://www.nasdaq.com/symbol/wfc</a>
<b>JPM</b>	J P Morgan Chase & Co	62.81	2.31E+11	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/jpm">http://www.nasdaq.com/symbol/jpm</a>
<b>BAC</b>	Bank of America Corporation	16.08	1.67E+11	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/bac">http://www.nasdaq.com/symbol/bac</a>
<b>C</b>	Citigroup Inc.	50.12	1.49E+11	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/c">http://www.nasdaq.com/symbol/c</a>
<b>AIG</b>	American International Group, Inc.	59.75	73911497592	n/a	n/a	Finance	Property-Casualty Insurers	<a href="http://www.nasdaq.com/symbol/aig">http://www.nasdaq.com/symbol/aig</a>
<b>GS</b>	Goldman Sachs Group, Inc. (The)	169.84	72442901924	n/a	1999	Finance	Investment Bankers/Brokers/Service	<a href="http://www.nasdaq.com/symbol/gs">http://www.nasdaq.com/symbol/gs</a>
<b>USB</b>	U.S. Bancorp	41.05	71803718395	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/usb">http://www.nasdaq.com/symbol/usb</a>
<b>AXP</b>	American Express Company	64.42	63405122360	n/a	n/a	Finance	Finance: Consumer Services	<a href="http://www.nasdaq.com/symbol/axp">http://www.nasdaq.com/symbol/axp</a>
<b>MS</b>	Morgan Stanley	30.5	59054830750	n/a	n/a	Finance	Investment Bankers/Brokers/Service	<a href="http://www.nasdaq.com/symbol/ms">http://www.nasdaq.com/symbol/ms</a>
<b>BLK</b>	BlackRock, Inc.	330.16	54848693699	n/a	1999	Finance	Investment Bankers/Brokers/Service	<a href="http://www.nasdaq.com/symbol/blk">http://www.nasdaq.com/symbol/blk</a>
<b>MET</b>	MetLife, Inc.	44.37	49322866962	n/a	2000	Finance	Life Insurance	<a href="http://www.nasdaq.com/symbol/met">http://www.nasdaq.com/symbol/met</a>
<b>PNC</b>	PNC Financial Services Group, Inc. (The)	91.6	46515010272	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/pnc">http://www.nasdaq.com/symbol/pnc</a>
<b>BK</b>	Bank Of New York Mellon Corporation (The)	38.82	42428419621	n/a	n/a	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/bk">http://www.nasdaq.com/symbol/bk</a>
<b>SCHW</b>	The Charles Schwab Corporation	30.79	40535754347	n/a	n/a	Finance	Investment Bankers/Brokers/Service	<a href="http://www.nasdaq.com/symbol/schw">http://www.nasdaq.com/symbol/schw</a>
<b>COF</b>	Capital One Financial Corporation	68.55	36471702025	n/a	1994	Finance	Major Banks	<a href="http://www.nasdaq.com/symbol/cof">http://www.nasdaq.com/symbol/cof</a>
<b>PRU</b>	Prudential Financial, Inc.	76.92	34537080000	n/a	2001	Finance	Life Insurance	<a href="http://www.nasdaq.com/symbol/pru">http://www.nasdaq.com/symbol/pru</a>
<b>TRV</b>	The Travelers Companies, Inc.	109.04	33172017516	n/a	n/a	Finance	Property-Casualty Insurers	<a href="http://www.nasdaq.com/symbol/trv">http://www.nasdaq.com/symbol/trv</a>
<b>BX</b>	The Blackstone Group L.P.	27.29	32092061544	n/a	2007	Finance	Investment Managers	<a href="http://www.nasdaq.com/symbol/bx">http://www.nasdaq.com/symbol/bx</a>
<b>CME</b>	CME Group Inc.	88.93	30079362252	n/a	2002	Finance	Investment Bankers/Brokers/Service	<a href="http://www.nasdaq.com/symbol/cme">http://www.nasdaq.com/symbol/cme</a>

FRM equations



# NBER recession Indicator

- From FRED NBER



**Table 2:** Logistic regression results

	<i>Dependent variable:</i>
	recession
frm	215.513*** (12.978)
Constant	-5.852*** (0.325)
Observations	1,370
Log Likelihood	-539.147
Akaike Inf. Crit.	1,082.294

*Note:* \*p<0.1; \*\*p<0.05; \*\*\*p<0.01