

# Uncertainty about perceived inflation target and monetary policy

Kosuke Aoki

(London School of Economics and Political Science)

Takeshi Kimura

(Bank of Japan)



Discussion Paper  
Series 1: Economic Studies  
No 18/2007

Discussion Papers represent the authors' personal opinions and do not necessarily reflect the views of the Deutsche Bundesbank or its staff.

**Editorial Board:**

Heinz Herrmann  
Thilo Liebig  
Karl-Heinz Tödter

Deutsche Bundesbank, Wilhelm-Epstein-Strasse 14, 60431 Frankfurt am Main,  
Postfach 10 06 02, 60006 Frankfurt am Main

Tel +49 69 9566-1

Telex within Germany 41227, telex from abroad 414431

Please address all orders in writing to: Deutsche Bundesbank,  
Press and Public Relations Division, at the above address or via fax +49 69 9566-3077

Internet <http://www.bundesbank.de>

Reproduction permitted only if source is stated.

ISBN 978-3-86558-317-8 (Printversion)

ISBN 978-3-86558-318-5 (Internetversion)

This paper was presented at the joint Bundesbank/Fed Cleveland conference (June 2007) on “Monetary policy strategy: Old issues and new challenges”. The views expressed in the paper are those of the authors and not necessarily those of the Bundesbank or the Federal Reserve Bank of Cleveland.

## Monetary policy strategy: Old issues and new challenges

Joint Deutsche Bundesbank/Federal Reserve Bank of Cleveland  
Conference

6-7 June 2007

Frankfurt am Main

Wednesday, 6 June 2007

09:45 – 10:05

### Introduction

*Sandra Pianalto (President, Federal Reserve Bank of Cleveland)*

10:05 – 11:15

### The optimal monetary policy response to exchange rate misalignments

Campbell Leith (*University of Glasgow*)

*Simon Wren-Lewis (University of Oxford)*

Discussants:

*Mathias Hoffmann (Deutsche Bundesbank)*

*Robert Kollmann (Université Libre de Bruxelles)*

11:15 – 11:45

### Break

11:45 – 12:55

### Monetary policy and core inflation

Michele Lenza (*European Central Bank*)

Discussants:

*Andreas Hornstein (Federal Reserve Bank of Richmond)*

*Michael Krause (Deutsche Bundesbank)*

- 12:55 – 14:30      **Lunch**
- 14:30 – 15:40      **Reconsidering the role of monetary indicators for euro area inflation from a Bayesian perspective using group inclusion probabilities**  
Michael Scharnagl (*Deutsche Bundesbank*)  
Christian Schumacher (*Deutsche Bundesbank*)
- Discussants:      David Altig (*Federal Reserve Bank of Cleveland*)  
                         Livio Stracca (*European Central Bank*)
- 15:40 – 16:10      **Break**
- 16:10 – 17:20      **Uncertainty about perceived inflation target and monetary policy**  
Kosuke Aoki (*London School of Economics and Political Science*)  
Takeshi Kimura (*Bank of Japan*)
- Discussants:      Nicoletta Batini (*International Monetary Fund*)  
                         Martin Bodenstein (*Federal Reserve Board*)
- 18:30                **Dinner**
- Speaker:            Axel Weber (*President, Deutsche Bundesbank*)

Thursday, 7 June 2007

- 10:00-11:10      **Mortgage markets, collateral constraints and monetary policy: Do institutional factors matter?**  
Alessandro Calza (*European Central Bank*)  
Tommaso Monacelli (*Università Commerciale Luigi Bocconi*)  
Livio Stracca (*European Central Bank*)
- Discussants:      Fiorella de Fiore (*European Central Bank*)  
                         Andreas Schabert (*University of Dortmund*)
- 11:10 – 11:30      **Break**

11:30 – 12:40 **Money in monetary policy design : ECB-style cross-checking in the New Keynesian Model**

Günter Beck (*Goethe University Frankfurt*)

Volker Wieland (*Goethe University Frankfurt*)

Discussants: Stefan Gerlach (*Bank for International Settlements*)  
Samuel Reynard (*Swiss National Bank*)

12:40 – 14:00 **Lunch**

14:00 – 15:10 **The inflation dynamics mystery**

Robert King (*Boston University*)

Anthony Landry (*Federal Reserve Bank of Dallas*)

Discussants: Ragner Nymoen (*University of Oslo*)  
John M Roberts (*Federal Reserve Board*)

15:10 – 15:30 **Break**

15:30 – 16:40 **The rationality and reliability of expectations reported by British households: Micro evidence from the British household panel survey**

James Mitchell (*National Institute of Economic and Social Research*)

Martin Weale (*National Institute of Economic and Social Research*)

Discussants: Mike Bryan (*Federal Reserve Bank of Cleveland*)  
Joachim Winter (*University of Munich*)

# Uncertainty about Perceived Inflation Target and Monetary Policy\*

Kosuke Aoki  
LSE  
k.aoki@lse.ac.uk

Takeshi Kimura  
Bank of Japan  
takeshi.kimura@boj.or.jp

July 2007

## Abstract

We analyse the interaction between private agents' uncertainty about inflation target and the central bank's data uncertainty. In our model, private agents update their perceived inflation target and the central bank estimates unobservable economic shocks as well as the perceived inflation target. Under those two uncertainties, the learning process of both private agents and the central bank causes higher order beliefs to become relevant, and this mechanism is capable of generating high persistence and volatility of inflation even though the underlying shocks are purely transitory. We also find that the persistence and volatility become smaller as the inflation target becomes more credible, that is, the private agents' uncertainty about inflation target (and hence the bank's data uncertainty) diminishes.

**Keywords:** Monetary policy, central banks

**JEL Classification:** E52, E58

---

\* The authors are grateful for comments from Nicoletta Baniti, Martin Bodenstein, Anton Braun, Shinichi Fukuda, Bernardo Guimaraes, Athanasios Orphanides, Nobuyuki Oda, Pedro Teles, Hiroshi Ugai, seminar participants at Bank of Canada, Bank of England, Bank of Japan, Bank of Portugal, BIS, Cambridge, ESSIM 2005, LSE, University of Tokyo, Hitotsubashi, Kobe, Osaka and Tohoku Universities, as well as participants at the Joint Deutsche Bundesbank/Federal Reserve Bank of Cleveland Conference. The authors also thank Naohisa Hirakata for his excellent research assistance. Aoki thanks hospitality of the Bank of Japan. The paper represents the views and analysis of the authors and should not be thought to represent those of the Bank of Japan.

## Non-technical summary

Extracting information about economic activity from markets (financial markets in particular) is an important for a central bank. This is because many of the economic variables are not directly observable to the banks, but markets can provide information on such variables. In this paper, it is shown that the ability of the bank to extract information from markets depends crucially on the credibility of inflation target.

An intuition behind this can be obtained from the following example. Consider an economy in which the bank wishes to keep track of the natural interest rate, which is the equilibrium real interest rate under flexible prices. By keeping track of the natural rate, the bank can offset the effects of changes in the natural rate on inflation. Assume that the bank cannot directly observe inflation expectations and the natural interest rate. Suppose now that the bank observes an increase in nominal interest rates. There are two possible reasons. One reason is that the private agents may have revised their expectations about the inflation target. Another reason is that future natural interest rate may have increased. When inflation target is perfectly credible, then the first reason would disappear. If the bank knows that inflation expectation is pinned down by its inflation target, it could infer the natural interest rate from nominal interest rates. However, when the inflation target is not fully credible, the bank cannot tell if the observed increase in the nominal rate is due to a revise in the perceived inflation target or due to a change in the natural rate. This can de-stabilise inflation.

With this intuition, we show that under imperfect credibility the learning process of both private agents and the central bank causes higher order beliefs to become relevant, thus increasing the persistence and volatility of inflation. This mechanism is capable of generating high persistence and volatility even though the underlying shocks are purely transitory.



## **Nicht-technische Zusammenfassung**

Eine wichtige Aufgabe von Zentralbanken ist es, Informationen über die wirtschaftliche Entwicklung insbesondere aus dem Verhalten der Finanzmärkte zu gewinnen. Denn oft sind diese Variablen nicht direkt beobachtbar. In diesem Papier wird gezeigt, dass die Fähigkeit der Notenbank, solche Informationen zu gewinnen, ganz wesentlich von der Glaubwürdigkeit des Inflationszieles abhängt.

Das folgende Beispiel soll dies intuitiv deutlich machen. Angenommen, die Notenbank will den natürlichen Zins, das heißt den Gleichgewichtszins bei flexiblen Preisen, realisieren. Die Bank soll nicht in der Lage sein, die Inflationserwartungen und den natürlichen Zins direkt zu beobachten. Wenn nun der Nominalzins ansteigt, kann das zwei Gründe haben: Zum einen kann der private Sektor seine Meinung über das Inflationsziel der Notenbank geändert haben. Zum anderen kann der künftige natürliche Zins gestiegen sein. Wenn das Inflationsziel vollständig glaubwürdig ist, dann entfällt der erste Grund. In diesem Fall kann die Notenbank den natürlichen Zins aus dem Nominalzins ablesen. Wenn aber das Inflationsziel nicht vollständig glaubwürdig ist, dann weiß die Notenbank nicht, ob der Zinsanstieg auf eine Revision des erwarteten Inflationszieles oder auf eine Veränderung des natürlichen Zinses zurück zu führen ist.

Entsprechend dieser Idee zeigen wir, dass bei unvollständiger Glaubwürdigkeit der Lernprozess des privaten Sektors und der Zentralbank (über die Annahmen des jeweilig anderen) dazu führt, dass die Unsicherheit der Vorstellungen (und andere Momente höherer Ordnung) relevant werden und zu Persistenz und Volatilität der Inflation führen. In der Tat kann die Persistenz und Volatilität groß werden, obwohl die eigentlichen Schocks nur vorübergehender Natur sind.



# 1 Introduction

The objective of this paper is to analyse how uncertainty about inflation target affects the degree of uncertainty central bank faces and hence the stochastic properties of inflation. When the private agents are uncertain about inflation target, they generate their belief about the target, which we call ‘perceived inflation target’. It is in general quite difficult for the bank to observe perceived inflation target. First of all, there are no direct measures of perceived inflation target that are available for central banks. As proxies, several survey measures of long-term inflation expectations are available, for example, the Michigan Survey and the Survey of Professional Forecasters in the case of the United States. Also, it is possible to extract information on inflation expectations from financial variables such as inflation-indexed bonds. However, private agents’ inflation expectations are affected not only by their perceived inflation target but also by their expectations about future conditions of the economy, such as future demand and supply shocks. Therefore, the measures of inflation expectations are only noisy measures of perceived target. Recently, Bekaert et al. (2005) and Kozicki and Tinsley (2005) report their estimates of perceived inflation target in the United States. For the US economy in the late-1970s to early 1980s, Kozicki and Tinsley (2005) report that the perceived inflation target is estimated to be around 8%,<sup>1</sup> while Bekaert et al. (2005)’s estimate is around 14%. From policy point of view, the difference between 8% and 14% is too large — the policy prescription can be very different depending on which to believe. Those examples imply that it is not a trivial task to extract information about perceived inflation target. As a result, the private-sector uncertainty about inflation target creates uncertainty facing the bank about the perceived inflation target. In this paper, we focus our analysis on how this uncertainty distorts bank’s stabilisation policy, and draw some implica-

---

<sup>1</sup>Their estimate of the target is around 3.5%.

tions for inflation dynamics.

It is shown that uncertainty about inflation target contributes to inflation persistence and volatility through two channels. One channel is the private-sector uncertainty about the inflation target. The private-sector learning about the target creates inflation persistence, as is shown in Erceg and Levin (2003). The other, which is our main focus, is the central-bank uncertainty about the perceived inflation target. This uncertainty makes it more difficult for the bank to estimate the state of the economy, leading policy errors. Thus the degree of uncertainty facing the bank is endogenously determined by the credibility problem. In other words, imperfect credibility is bad not only because it fails to fix inflation expectations, but also because it makes the bank's stabilisation policy more difficult.

An intuition behind this can be obtained from the following example. Consider an economy in which the bank wishes to keep track of the natural interest rate, which is the equilibrium real interest rate under flexible prices.<sup>2</sup> By keeping track of the natural rate, the bank can offset the effects of changes in the natural rate on inflation. Suppose now that the bank observes an increase in nominal interest rates. There are two possible reasons. One reason is that the private agents may have revised their expectations about the inflation target. Another reason is that future natural interest rate may have increased. When inflation target is perfectly credible, then the first reason would disappear. If the bank knows that inflation expectation is pinned down by its inflation target, it could infer the natural interest rate from nominal interest rates. However, when the inflation target is not fully credible, the bank cannot tell if the observed increase in the nominal rate is due to a revise in the perceived inflation target or due to a change in the natural rate. This can de-stabilise inflation. With this intuition, we show that under imperfect credibility the learning process of both private agents and the central bank causes higher order beliefs to become relevant, thus increasing the persistence

---

<sup>2</sup>In section 2 we will consider a model of this kind.

and volatility of inflation. This mechanism is capable of generating high persistence and volatility even though the underlying shocks are purely transitory.<sup>3</sup>

Our model can naturally connect the literature on monetary policy under data uncertainty and that on imperfect credibility. In a series of papers, Orphanides (2001, 2002, 2003) show that the mismeasurement of economic activity, such as the output gap and natural unemployment rate, was responsible for the ‘Great Inflation’ of the 1970s-1980s in the United States. While his work takes the measurement problem as exogenously given, our paper shows that the measurement problem can arise endogenously from lack of credibility.

Our model also predicts that the measurement problem can decrease as monetary policy gains more credibility. This implies that inflation becomes less volatile and less persistent. In recent years, a large amount of literature has documented changing stochastic properties of inflation and output—the so-called ‘Great Moderation’. For example, Benati (2004) reports that output and inflation in the UK has become less persistent and volatile since the UK introduction of inflation target in 1992. Our model can explain this empirical fact. One of the controversial issues in the literature is whether the Great Moderation was caused by good luck (shocks became smaller) or good policy. The existing literature has mainly supported the good-luck hypothesis (See, for example, Ahmed et al. (2004), Stock and Watson (2003)). However, Bernanke (2004) claims that the econometric technique used in the literature may confuse good policy with good luck. His insight is that the existing literature does not take into account the impact of systematic component in monetary policy on inflation expectations. That implies that any fluctuations caused by de-anchored expectations may get confused with genuine non-policy shocks. In our model the change in the stochastic properties of inflation is purely

---

<sup>3</sup>Woodford (2002) and Amato and Shin (2003) consider the roles of higher order beliefs in monetary models. They consider higher order beliefs among firms under strategic complementarity and how this setting generates persistent effect of monetary policy. On the contrary, we focus on the interaction of beliefs between private agents and the central bank.

driven by learning by both central bank and private agents. By using stochastic simulation based on our model, we confirm Bernanke's conjecture.

The structure of the paper is as follows. The next section layouts the model. Section 3 derives equilibrium, and Section 4 analyses inflation dynamics in our model and draws policy implications. Section 6 concludes.

## 2 Model

We present a very simple model of inflation determination. It consists of two equations: a Fisher equation that relates the nominal interest rate and the natural interest rate (equilibrium real interest rate), and a monetary policy rule that sets the nominal interest rate as the instrument of monetary policy. The model can be interpreted as a model of inflation determination in an economy under flexible prices.<sup>4</sup>

### 2.1 Structural equations

The first equation in our model is the linearised Fisher equation of the form:

$$i_t = r_t^n + E_{t|p} \pi_{t+1}, \quad (1)$$

where  $i_t$  is nominal interest rate at time  $t$ ,  $r_t^n$  is the natural interest rate at time  $t$ ,  $\pi_t$  is inflation rate at time  $t$ . The expectation operator  $E_{t|p}$  represents the expectation conditional on the private-sector information at time  $t$ . The information set is defined in Section 2.2.

---

<sup>4</sup>See, for example, Woodford (2003), Chapter 2.

Equation (1) can be interpreted as a log-linear approximation to the Euler equation of the representative household in an endowment economy with flexible prices. A log-linearised Euler equation in such an economy is given by

$$i_t = \sigma[(E_{t|p}y_{t+1} - y_t) - (E_{t|p}g_{t+1} - g_t)] + E_{t|p}\pi_{t+1}, \quad (2)$$

where  $y_t$  and  $g_t$  are respectively the log-deviation of exogenous output and demand shock from their steady state values, and  $\sigma$  is the inverse of the elasticity of intertemporal substitution. By denoting

$$r_t^n \equiv \sigma[(E_{t|p}y_{t+1} - y_t) - (E_{t|p}g_{t+1} - g_t)], \quad (3)$$

we obtain (1). Notice that  $r_t^n$  represents the equilibrium real interest rate under flexible prices, that is, the natural interest rate.<sup>5</sup>

The second equation in the model is a monetary policy rule. It is assumed that the central bank chooses the nominal interest rate by following the simple monetary policy rule:

$$i_t = \phi(\pi_t - \pi_t^*) + \pi_t^* + E_{t|c}r_t^n, \quad \phi > 1. \quad (4)$$

Here  $\pi_t^*$  is the central bank's inflation target at time  $t$ , and  $E_{t|c}$  is the expectation operator conditional on the bank's information set at time  $t$ . The information set of the bank is specified in Section 2.2. Equation (4) assumes that the bank tries to keep track of the path of the natural interest rate  $r_t^n$  conditional on its information set. We interpret this term as representing the stabilisation policy of the bank. As is shown in Section 2.3, the bank can offset the effect of the changes in  $r_t^n$  on inflation by keeping track of  $r_t^n$ . Finally, by assuming  $\phi > 1$ , the monetary policy rule (4) satisfies the so-called Taylor principle.

---

<sup>5</sup>See, for example, Woodford (2003) for this concept.

We assume that the inflation target consists of the long-run component ( $\pi^*$ ), and the transitory shock ( $\varepsilon_t$ ):

$$\pi_t^* = \pi^* + \varepsilon_t, \quad (5)$$

where  $\varepsilon_t$  is i.i.d. with mean zero. This assumption is similar to Erceg and Levin (2003), who also assume that the inflation target varies due to a combination of transitory and highly persistent shocks.<sup>6</sup> Combining (4) and (5), one obtains

$$i_t = \phi(\pi_t - \pi^*) + \pi^* + E_{t|c}r_t^n + u_t, \quad (6)$$

where

$$u_t \equiv (1 - \phi)\varepsilon_t.$$

## 2.2 Information structure

Now we specify the information structure. On one hand, the private agents are assumed to know the monetary policy rule (4), including the parameter value for  $\phi$ . They observe inflation rate  $\pi_t$ , the nominal interest rate  $i_t$  and the natural rate  $r_t^n$ . Later we assume that the central bank cannot observe the natural rate. As is shown in Aoki (2006), this assumption can be justified as the equilibrium information structure of a certain island economy.<sup>7</sup> The private agents also observe the bank's estimate of  $r_t^n$  at time  $t$  that is denoted by  $E_{t|c}r_t^n$ . The underlying assumption is the situation in which the bank publishes its assessment of the current economic conditions.<sup>8</sup> Following Erceg and Levin (2003), we assume that the pri-

<sup>6</sup>They assume that the auto-regressive root of the persistent shock is 0.999.

<sup>7</sup>Aoki (2006) considers an island economy where information is dispersed such that no one can observe aggregate variables directly. However, the paper shows that the equilibrium of this economy is equivalent to that of economy where there exists the representative household who has perfect information regarding the aggregate states while the central bank does not.

<sup>8</sup>By equation (3), this assumption is equivalent to the assumption that the bank announces its forecasts of the growth rates of demand shocks (such as the government expenditure) and



vate agents cannot directly observe the underlying components of  $\pi_t^*$ , while they can infer  $\pi_t^*$  from knowledge of the bank's reaction function. This may be either because the bank does not explicitly announce its long-run target  $\pi^*$ , or because the target is not fully credible. In this case, for example, when they observe a high nominal interest rate, they cannot tell whether this is because  $\pi^*$  is low or  $u_t$  is high. In each period, they update their belief about  $\pi^*$ . Let  $E_{t|p}\pi^*$  be the perceived inflation target at time  $t$  conditional on the private-sector information at time  $t$ .

On the other hand, the bank knows the form of the IS equation (2), including the value of  $\sigma$ . It observes inflation, the nominal interest rate and the inflation target. However it cannot observe the natural rate  $r_t^n$  and the private-sector inflation expectations  $E_{t|p}\pi_{t+1}$ . In our model, the latter assumption is equivalent to the assumption that the bank cannot observe the perceived inflation target  $E_{t|p}\pi^*$ . This implies that, when the nominal interest rate is high, the bank cannot tell whether this is because the natural rate is high or inflation expectation is high. In each period, the bank estimates the natural rate and the perceived target. Let  $E_{t|c}r_t^n$  and  $E_{t|c}E_{t|p}\pi^*$  respectively denote the bank's estimate of the natural rate and the perceived target conditional on the bank's information set at time  $t$ .

In equilibrium, the endogenous variables  $\{i_t, \pi_t\}_{t=0}^\infty$  satisfies equations (1) and (6), taking the exogenous variables  $(\{r_t^n, u_t\}_{t=0}^\infty)$  as given. Expectations of each of the bank and the private agents are rational conditional on each of the information set. Our main objective is to analyse the interaction between the uncertainty facing the private sector and the uncertainty facing the central bank, and to draw its implications for inflation dynamics. In order to be able to obtain clear results, let us focus on the simplest case. From now on, we assume the natural interest rate and monetary policy shock are i.i.d. normal and independent

---

output. Publishing those forecasts are not uncommon in practice. For example, the Bank of England publishes its forecast of GDP in the *Inflation Report*.

from each other.<sup>9</sup> More specifically, we assume

$$r_t^n \sim N(0, \sigma_r^2), \quad (7)$$

$$u_t \sim N(0, \sigma_u^2). \quad (8)$$

It is assumed that the distributions are known and common knowledge.

### 2.3 Equilibrium when inflation target is observable

As the benchmark case, it is useful to discuss the rational expectations equilibrium when  $\pi^*$  is known and common knowledge. In this case, the agents can also infer  $u_t$  from the monetary policy rule (6), implying that the agents have perfect information. It is then shown that information is fully revealed to the bank as well as to the private agents in equilibrium. In order to show this, suppose information is fully revealed in equilibrium. This implies that both the bank and the private agents can infer time- $t$  variables. It also implies that for any future variables  $x_{t+i}$ ,  $E_{t|c}x_{t+i} = E_{t|p}x_{t+i} \equiv E_t x_{t+i}$ , where  $E_t$  denotes the expectations operator under full information. In particular, the bank can infer  $r_t^n$  in equilibrium so that  $E_{t|c}r_t^n = r_t^n$ . Then, from (1) and (6), it is straightforward to show that the equilibrium inflation is given by

$$\pi_t = \pi^* - \phi^{-1} u_t. \quad (9)$$

Since monetary policy satisfies the Taylor principle, the equilibrium is uniquely determined. Because we assume  $u_t$  is white noise (8), equation (9) implies that  $E_t \pi_{t+1} = \pi^*$ . The bank thus infer that inflation expectations are pinned down

---

<sup>9</sup>We can extend our analysis to the case in which the natural rate follows an AR(1) process, which does not change our main results. The results in the the case of AR(1) are available upon request.

by  $\pi^*$  even if it cannot directly observe expectations. Then, from (1) it can infer  $r_t^n$  because  $E_t \pi_{t+1}$  is identified. Therefore we have confirmed that information is fully revealed to the bank even though  $r_t^n$  is not directly observable. In other words, when  $\pi^*$  is credible, the bank is not subject to uncertainty regarding the measurement of the natural rate.

Equation (9) implies that inflation fluctuation does not involve any persistence when  $u_t$  is white noise. The other disturbance,  $r_t^n$ , does not affect inflation fluctuations because the bank fully offsets its effects on inflation. In this sense, the bank's stabilisation policy works perfectly. To summarise, once the bank's inflation target is known to the private sector and becomes common knowledge, all of the uncertainty in the model disappears. Now let us analyse the equilibrium when  $\pi^*$  is not credible.

### 3 Equilibrium with uncertain inflation target

#### 3.1 Equilibrium given belief

Although beliefs are determined endogenously in equilibrium, it is useful to see how inflation depends on the beliefs of the central bank and the private agents. Complete analysis of the equilibrium is in Section 3.3. From (1) and (6), inflation is given by

$$\pi_t = \phi^{-1} [(\phi - 1)\pi^* - u_t] + \phi^{-1}(r_t^n - E_{t|c}r_t^n) + \phi^{-1}E_{t|p}\pi_{t+1}. \quad (10)$$

Equation (10) shows that  $\pi_t$  depends on the deviation of  $r_t^n$  from the bank's estimate  $E_{t|c}r_t^n$ . If one takes expectation of the both sides of (10) conditional on  $E_{t|c}$ ,

one obtains<sup>10</sup>

$$\pi_t = \phi^{-1} [(\phi - 1)\pi^* - u_t] + \phi^{-1} E_{t|c} E_{t|p} \pi_{t+1}. \quad (11)$$

By solving this equation forward, the bounded solution for  $\pi_t$  in terms of the bank's belief is given by<sup>11</sup>

$$\pi_t = \pi^* - \phi^{-1} u_t + \phi^{-1} (E_{t|c} E_{t|p} \pi^* - \pi^*). \quad (12)$$

Compare (12) with (9). Equation (12) can be reduced to (9) when  $\pi^*$  is common knowledge. In contrast, under our information structure,  $\pi_t$  depends on the second-order belief, namely, the bank's belief about  $E_{t|p} \pi^*$ . Intuitively, the bank's information problem is the inability to distinguish  $r_t^n$  and  $E_{t|p} \pi_{t+1}$ , and the latter depends on  $E_{t|p} \pi^*$ . An imprecise estimate of  $E_{t|p} \pi^*$  results in an imprecise estimate of  $r_t^n$ . This represents the negative feedback effect from the private-sector uncertainty about inflation target to the bank's estimate of the state of the economy ( $r_t^n$ ).

Alternatively, one can take expectations of the both sides of (10) conditional on  $E_{t|p}$  and solve forward to obtain

$$\pi_t = \pi^* - \phi^{-1} u_t + \phi^{-1} (E_{t|p} \pi^* - \pi^*) + E_{t|p} \sum_{j=0}^{\infty} \phi^{-(j+1)} \left[ r_{t+j}^n - E_{t+j|c} r_{t+j}^n \right] \quad (13)$$

This expression implies that inflation depends on the perceived inflation target and the private-sector expectations about the bank's current and future estimation errors of the natural rates.

<sup>10</sup>Here we use the fact that  $E_{t|c} \pi_t = \pi_t$ .

<sup>11</sup>Here we use the fact that  $\lim_{j \rightarrow \infty} [E_{t|c} E_{t|p} E_{t+1|c} E_{t+1|p} \dots E_{t+j|c} E_{t+j|p}] \phi^{-j-1} \pi_{t+j} = 0$  when  $\pi_t$  is bounded

The interaction between the uncertainty facing private agents and that facing the bank also has implications for inflation expectations. Equation (12) implies that

$$\pi_{t+1} = (1 - \phi^{-1})\pi^* - \phi^{-1}u_{t+1} + \phi^{-1}E_{t+1|c}\pi_{t+1|p}^*.$$

Therefore, inflation expectation  $E_{t|p}\pi_{t+1}$  is given by

$$E_{t|p}\pi_{t+1} = E_{t|p}\pi^* + \phi^{-1}E_{t|p}(E_{t+1|c}E_{t+1|p}\pi^* - E_{t+1|p}\pi^*). \quad (14)$$

Equation (14) shows that  $E_{t|p}\pi_{t+1} \neq E_{t|p}\pi^*$ . Inflation expectation depends on the third-order belief, that is, how the private agents expect that the central bank will mis-estimate the perceived inflation target in the future. Inflation at time  $t$  depends on the private-sector expectations about future monetary policy, and therefore it depends on the private-sector expectation about how the bank will mis-estimate the natural rate in the future, as is shown in equation (13). The bank's estimate of the natural rates is related with its estimate of the perceived inflation target. Note that  $E_{t|p}E_{t+1|c}r_{t+1}^n \neq 0$  even if  $E_{t|p}r_{t+1}^n = 0$ . When the private agents expect that the bank's estimate about the perceived inflation target is different from their own perceived target, they will expect that the bank will incorrectly estimate the natural rates. In other words, uncertainty about  $E_{t|p}\pi^*$  distorts the bank's estimation of  $r_t^n$ , and the private agents understand this information problem the bank faces.

Now we turn to the filtering by private agents and the central bank.

### 3.2 Evolution of the private-sector belief

In each period, the private agents update their perceived long-run inflation target  $\pi^*$ . From monetary policy rule (6), the observation equation for the private agents

is given by

$$i_t - \phi\pi_t - E_{t|c}r_t^n = (1 - \phi)\pi^* + u_t. \quad (15)$$

The left hand side of equation (15) is observable, and the right hand side is not. In equation (15), we use the assumption that the bank's estimate of  $r_t^n$  is observable. Denote by  $z_t$  the linear combination of the observable variables of the private sector:

$$z_t \equiv i_t - \phi\pi_t - E_{t|c}r_t^n.$$

Under assumption (8), the distribution of  $z_t$  is given by

$$z_t \sim N((1 - \phi)\pi^*, \sigma_u^2). \quad (16)$$

The filtering problem of the private agents is to distinguish the transitory component  $u_t$  from the constant term  $(1 - \phi)\pi^*$ . This is a classic inference problem from a normal distribution with unknown mean and known variance. From now on, it is useful to work with 'precision,'  $\gamma_u \equiv 1/\sigma_u^2$ , rather than variance  $\sigma_u^2$ . Let the initial prior (at time 0) on  $(1 - \phi)\pi^*$  be

$$(1 - \phi)\pi^* \sim N((1 - \phi)\pi_{0|p}^*, 1/\tau_{0|p}), \quad (17)$$

where  $\pi_{0|p}^*$  is the initial prior about  $\pi^*$ , and  $\tau_{0|p}$  is the initial precision. Then the posterior mean after  $t$  observations is given by (see DeGroot (1970))

$$E_{t|p}\pi^* = \frac{\tau_{0|p}\pi_{0|p}^* + t\gamma_u(1 - \phi)^{-1}\bar{z}_t}{\tau_{0|p} + t\gamma_u}, \quad (18)$$

where  $\bar{z}_t \equiv \frac{1}{t} \sum_{s=1}^t z_s$ . Define

$$\alpha_t \equiv \frac{\tau_{0|p}}{\tau_{0|p} + t\gamma_u}.$$

Then, one can rewrite (18) as

$$E_{t|p}\pi^* = \alpha_t \pi_{0|p}^* + \frac{1 - \alpha_t}{1 - \phi} \bar{z}_t.$$

This means that  $E_{t|p}\pi^*$  is a weighted average of the initial belief  $\pi_{0|p}^*$  and the news  $\bar{z}$ . Furthermore, since  $z_t = (1 - \phi)\pi^* + u_t$ , (18) can be expressed as

$$E_{t|p}\pi^* = \alpha_t \pi_{0|p}^* + (1 - \alpha_t)\pi^* + \frac{1 - \alpha_t}{1 - \phi} \bar{u}_t, \quad (19)$$

where  $\bar{u}_t \equiv \frac{1}{t} \sum_{s=1}^t u_s$ . Notice that  $\alpha_t \rightarrow 0$  as  $t \rightarrow \infty$ . Also,  $\bar{u}_t \rightarrow 0$  by the law of large numbers. Therefore, as the private agents observe more information over time, they will eventually learn  $\pi^*$ . Alternatively, we can write (19) in a recursive form:

$$E_{t|p}\pi^* - \pi^* = b_t(E_{t-1|p}\pi^* - \pi^*) + \frac{1 - b_t}{1 - \phi} u_t, \quad (20)$$

where

$$b_t \equiv \frac{\tau_{t-1|p}}{\tau_{t-1|p} + \gamma_u},$$

$$\tau_{t|p} \equiv \tau_{t-1|p} + \gamma_u.$$

Equation (20) gives the evolution of the perceived inflation target.

### 3.3 Evolution of the bank's belief

Next, we compute the optimal filtering problem by the central bank. The bank's observation equation is given by the Fisher equation (1). The bank's observable variable is the nominal interest rate  $i_t$ , and the unobservable variables are  $r_t^n$  and  $E_{t|p}\pi_{t+1}$  that is given by (14). Notice that  $E_{t|p}\pi_{t+1}$  is determined endogenously in equilibrium. Here it is necessary to solve the filtering problem and equilibrium

simultaneously, since equilibrium depends on the bank's policy, and the bank's policy depends on its estimate of the natural interest rate.<sup>12</sup> This estimate in turn depends on the statistical properties of the bank's observables and the natural rate in equilibrium. In Appendix A, it is shown that the evolution of the bank's estimation error of the natural rate is given by

$$r_t^n - E_{t|c}r_t^n = d_t \frac{B_t}{B_{t-1}} \left( r_{t-1}^n - E_{t-1|c}r_{t-1}^n \right) + (1 - d_t)r_t^n, \quad (21)$$

where  $B_t$  and  $d_t$  are time-varying deterministic parameters that are given in Appendix A. Equivalently, it is shown in Appendix A the evolution of the bank's estimation error of the perceived inflation target can be written as

$$E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^* = d_t b_t \left( E_{t-1|c}E_{t-1|p}\pi^* - E_{t-1|p}\pi^* \right) + (1 - d_t) \frac{a_t}{B_t} r_t^n. \quad (22)$$

There is a close relationship between those estimates. Indeed, Appendix A shows that the relationship is given by

$$E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^* = \frac{a_t}{B_t} \left( r_t^n - E_{t|c}r_t^n \right). \quad (23)$$

Equation (23) implies that imprecise estimate of the perceived inflation target results in imprecise estimate of the natural rate. This is due to the bank's inability to distinguish inflation expectations and the natural rate when it observes the nominal interest rate.

---

<sup>12</sup>See, Aoki (2003) and Svensson and Woodford (2003) for optimal filtering in forward looking models.



## 4 Inflation dynamics under uncertain inflation target

### 4.1 Variance and autocorrelation of inflation

Now we are able to complete our analysis of inflation dynamics. Using (12) and (23), Equilibrium inflation can be written as

$$\begin{aligned}\pi_t &= \pi^* - \phi^{-1}u_t + \tilde{\pi}_t, \quad \text{where} \\ \tilde{\pi}_t &\equiv \phi^{-1} [(E_{t|p}\pi^* - \pi^*) + (E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^*)] \\ &= \phi^{-1}(E_{t|p}\pi^* - \pi^*) + \phi^{-1}\frac{\alpha_t}{B_t}(r_t^n - E_{t|c}r_t^n)\end{aligned}\tag{24}$$

where  $E_{t|p}\pi^* - \pi^*$  and  $r_t^n - E_{t|c}r_t^n$  respectively evolve according to (20) and (21). The first two terms ( $\pi^* - \phi^{-1}u_t$ ) of equation (24) are identical to (9), that is, the equilibrium inflation when the inflation target is credible. The term  $\tilde{\pi}_t$  represents inflation fluctuations that are caused by the credibility problem. The term  $\phi^{-1}(E_{t|p}\pi^* - \pi^*)$  represents fluctuations that are caused by private-sector uncertainty about the inflation target. When the perceived inflation target deviates from the true target, fluctuations in inflation expectations add more fluctuations to the equilibrium inflation. The term  $\phi^{-1}\alpha_t/B_t(r_t^n - E_{t|c}r_t^n)$  represents the fluctuations caused by central-bank uncertainty about the perceived target. This term arises from the bank's inability to distinguish the natural rate and inflation expectations when inflation target is not credible.

Equation (20) implies that  $E_{t|p}\pi^* - \pi^* \rightarrow 0$  as  $t \rightarrow \infty$ , therefore that the private-sector uncertainty diminishes over time and the private agents will eventually learn about  $\pi^*$ . This in turn implies that the uncertainty facing central bank also diminishes over time. Therefore, the contribution of  $\tilde{\pi}_t$  to overall inflation persistence and volatility decrease over time and  $\pi_t \rightarrow \pi^* - \phi^{-1}u_t$  as  $t \rightarrow \infty$ . We can compute the variance and autocorrelation of inflation. In Appendix B, those

are given by

$$V[\pi_t] = \phi^{-2} \left[ \frac{\sigma_u^2}{(1-\phi)^2} \left\{ (b_t - \phi)^2 + \sum_{k=0}^{t-1} \left( \prod_{j=k}^{t-1} b_{t+j}^2 \right) (b_k - 1)^2 \right\} + \sigma_r^2 \left\{ h_t^2 + \sum_{k=0}^{t-1} \left( \prod_{j=k}^{t-1} g_{t+j}^2 \right) h_k^2 \right\} \right], \quad (25)$$

$$\text{Cov}[\pi_t, \pi_{t-1}] = \phi^{-2} \left[ \frac{b_t \sigma_u^2}{(1-\phi)^2} \left\{ (b_{t-1} - 1)(b_{t-1} - \phi) + \sum_{k=0}^{t-2} \left( \prod_{j=k}^{t-2} b_{j+1}^2 \right) (b_k - 1)^2 \right\} + g_t \sigma_r^2 \left\{ h_{t-1} + \sum_{k=0}^{t-2} \left( \prod_{j=k}^{t-2} g_{t+1}^2 \right) h_k^2 \right\} \right], \quad (26)$$

where  $g_t \equiv b_t d_t$  and  $h_t \equiv \frac{a_t}{B_t} (1 - d_t)$ . Since  $\lim_{t \rightarrow \infty} g_t = 1$ ,  $\lim_{t \rightarrow \infty} b_t = 1$  and  $\lim_{t \rightarrow \infty} h_t = 0$ , it is easily shown that the variance and autocorrelation satisfy<sup>13</sup>

$$\lim_{t \rightarrow \infty} V[\pi_t] = (\sigma_u / \phi)^2, \quad \lim_{t \rightarrow \infty} \text{Cov}[\pi_t, \pi_{t-1}] = 0,$$

which correspond to the variance and autocorrelation of the inflation process when inflation target is observable (equation (9)).

## 4.2 A reduced-form estimation of model-simulated data

In order to investigate the properties of inflation in our model further, we conduct a simple stochastic simulation of our model. We generated 1000 sets of artificial normally-distributed shocks of 40 periods in each set, and obtained the stochastic process of the inflation under the learning process of the private-sector and the central bank.

Then, we consider the reduced-form dynamics of inflation by estimating an AR

---

<sup>13</sup>See Appendix B.

model, in line with Ahmed et al. (2004); Stock and Watson (2002).

$$\pi_t = c + \alpha(L)\pi_{t-1} + \eta_t, \quad \text{Var}[\eta_t] = \sigma_\eta^2. \quad (27)$$

By model selection criterion (AIC), we set the AR lag order to one. The estimated AR parameter  $\alpha$ , the standard deviation of the innovation  $\sigma_\eta^2$ , and the variance of inflation  $\text{Var}[\pi_t]$  are calculated for each data set, and the summary statistics are averaged over 1000 sets. In order to examine how these statistics change under the learning process of the private-sector and the central bank, an AR model is estimated over the first 20 periods and the second 20 periods separately. Note that our data frequency should be interpreted as annual rather than quarterly, since our model is a flexible price model.

In the simulation, several parameters must be specified. We choose the central bank's inflation target,  $\pi^*$ , of 2%, and the private-sector prior in (17),  $\pi_{0|p}^*$ , of 10%. According to the analysis of Kozicki and Tinsley (2001, 2005), these values are roughly in line with the US economy at the beginning of 1980s. With regard to the uncertainty that the central bank initially faces,  $E_{0|c}\pi_{0|p}^* - \pi_{0|p}^*$ , we assume that it ranges from zero to five.<sup>14</sup> The standard deviation of monetary policy shock,  $\sigma_u$ , is set to 1%, and hence  $\gamma_u = 1$ . According to Roberts (2004), this is in line with the FED policy between 1960 and 1983. The standard deviation of natural rate of interest,  $\sigma_r$ , is set to 1.5%, and hence  $\gamma_r = 0.44$ . This value is based on the result of Laubach and Williams (2003), who estimate  $\sigma_r$  as between 1.1 and 2.6 using US data. The policy coefficient,  $\phi$ , is set to 1.5, like Taylor rule. Finally, we set the precision of initial prior, both  $\tau_{0|p}$  and  $\tau_{0|c}$ , to one. In Appendix C we examine some robustness against changing those parameters. Finally, notice that we have assumed the structural shocks  $r_t^n$  and  $u_t$  are white

---

<sup>14</sup>This range is in line with differences between the estimate of Bekaert et al. (2005) and Kozicki and Tinsley (2005).

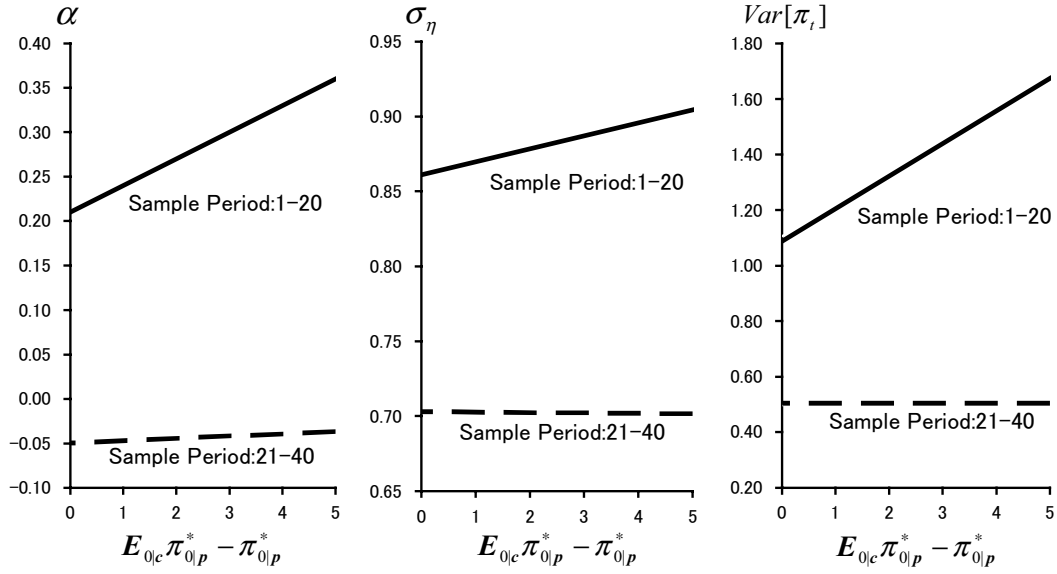


Figure 1: Time-varying persistency and volatility

noise processes. Therefore, the persistence reported below are purely driven by learning by central bank and private agents. In reality, the natural rate can be a persistent process. This implies that the persistence reported below should be interpreted as the lower bound that our theoretical model can generate.

Figure 1 shows the simulation results. The following two features are of particular importance. First, as the difference in the initial beliefs between the private sector and the central bank, i.e.  $E_{0|c}\pi_{0|p}^* - \pi_{0|p}^*$ , become large, both the estimated AR parameter  $\alpha$  and the standard deviation of the innovation  $\sigma_\eta$  become large in the first-half period. A larger gap in initial beliefs between the private sector and the central bank make the central bank's estimation of the economy more difficult, which results in higher persistence and higher volatility of inflation process. Second, for any value of  $E_{0|c}E_{0|p}\pi^* - E_{0|p}\pi^*$ ,  $\alpha$  and  $\sigma_\eta$  become smaller in the second half period than the first half period. This is because the private agents and central bank eventually learn about the inflation target and the perceived inflation target respectively. Accordingly, both inflation persistence and the volatility of inflation decline in the second half period. Now we draw some implications of

this simulation result.

### 4.3 Nominal anchor and measurement of economic activity

Figure 1 shows that inflation is persistent and volatile in the early phase of learning. (20) shows that  $u_t$  has persistent effects on  $\tilde{\pi}_t$  through the private-sector filtering. This implies that the private-sector uncertainty about  $\pi^*$  results in persistent inflation through learning. This agrees with Erceg and Levin (2003), who consider a similar economy in which the private-sector learning about inflation target can make inflation process persistent.<sup>15</sup> In our model, there is another channel through which imperfect credibility contributes to inflation persistence and volatility, namely, the bank's uncertainty about perceived inflation target. The fact that the bank cannot directly observe perceived inflation target implies that it cannot identify inflation expectations and the natural interest rates. This fact de-stabilises inflation because it prevents the bank from fully offsetting the effects of the fluctuations in  $r_t^n$  on  $\pi_t$ .<sup>16</sup>

Our model shows that the lack of strong nominal anchor and the measurement problem of economic activity are closely related with each other. In a series of papers, Orphanides (2001, 2002, 2003) show that the mismeasurement of economic activity, such as the output gap and natural unemployment rate, was responsible for the 'Great Inflation' of the 1970s-1980s in the United States. He shows that in the 70s the real-time estimate of the natural unemployment rate was too low and the estimate of the potential output was too high. This led to excess monetary expansion, resulting in high inflation. While his work takes the measurement problem as exogenously given, our paper shows that the imperfect credibility can endogenously amplify the measurement problem. Our model

<sup>15</sup>Erceg and Levin (2003) assume that the central bank has perfect information, which in our model corresponds to the case of  $E_{0|c}\pi_{0|p}^* - \pi_{0|p}^* = 0$ .

<sup>16</sup>See equation (6). When  $E_{t|c}r_t^n = r_t^n$ , then inflation does not depend on  $r_t^n$ .

implies that the measurement problem becomes serious when monetary policy loses credibility. On the contrary, gaining credibility can make the measurement problem less serious. This has important policy implications. If we take the measurement problem as exogenously given, a policy prescription would be not to respond actively to those economic variables subject to measurement errors. For example, Orphanides and Williams (2005) argue that it is desirable for monetary policy not to respond actively to the unemployment gap because the gap can be subject to large measurement errors. On the other hand, our model implies that gaining credibility helps the bank to reduce the measurement problem.

#### **4.4 Learning and time-varying stochastic process of inflation**

Figure 1 shows that the persistence and volatility of inflation decline as both of the agents and central bank learn. It is interesting to compare this observation with some empirical studies. Recently, several articles have documented that macroeconomic volatility in several OECD countries have declined over the past twenty years — the so called ‘Great Moderation.’<sup>17</sup>

For example, Benati (2007) found that under inflation targeting inflation persistence declined significantly and exhibits almost no persistence in UK, Canada, Sweden and New Zealand, while it was highly persistent between the breakdown of Bretton Woods and the introduction of inflation targeting. In Benati (2004), he found that the volatility of GDP and inflation in the UK has decreased since the introduction of inflation targeting in 1992. Our model can offer an explanation of his findings. As inflation targeting becomes credible, the private-sector uncertainty about the long-run inflation rate has decreased over time. At the same time, this has a favourable feedback to the stabilisation policy of the Bank of England. A decrease in the private-sector uncertainty has reduced the uncertainty facing the

---

<sup>17</sup>See, for example, Ahmed et al. (2004); Stock and Watson (2003); Cogley and Sargent (2004)

bank. As a result, the bank's stabilisation policy has improved, making inflation process less volatile and less persistent.

Our simulation, even though it is stylised, has some interesting implication for the econometric analysis of the Great Moderation. In the literature, two competing explanations for the Great Moderation are considered very likely. One is "good policy", i.e. improvements in monetary policy. Another is "good luck", i.e. a fortuitous reduction in exogenous shocks. Several prominent studies have provided support for the good-luck hypothesis. Roughly speaking, those econometric studies interpret the changes in estimated parameters of the model as changes in policy or economic structure, and the changes in the variances of innovations (residuals) as representing the changes in underlying economic shocks. In our simulation, both  $\alpha$  and  $\sigma_\eta$  in equation (27) change, implying that this looks as if both good policy and good luck occur. However, in our simulation, what changed between the first subperiod and the second subperiod is the perceived inflation target and the bank's estimate of the perceived target. We kept the monetary policy rule (6) and variance of shocks ( $\sigma_u, \sigma_r$ ) constant. This agrees with Bernanke (2004)'s view on the literature on the Great Moderation. He argues that the existing studies may incorrectly identify the effect of good policy as good luck. Econometricians typically do not measure exogenous shocks directly but instead infer them from movements in macroeconomic variables that they cannot otherwise explain. When the central bank's inflation target is incredible, the change in de-anchored inflation expectation may result in what appear to be change in exogenous shocks. Shocks in this sense may certainly depend on monetary policy regime. Accordingly, as the inflation expectation becomes to be anchored gradually, the standard deviation of innovation in the reduced form regression may become smaller even when the magnitude of exogenous shock (structural shock) is constant. This makes an econometric analysis based on reduced-form regression incorrectly lead to good-luck bias. This is exactly what happened in our

simulation study. Imperfect credibility creates fluctuations in inflation expectations through the private-sector learning. This diminishes over time as agents learn. In addition to this, imperfect credibility creates additional uncertainty facing the bank, which makes policy erratic. This also contributes to innovation variances that diminish over time.

## 5 Conclusion

In this paper, we analysed how private agents' uncertainty about inflation target and the central bank's uncertainty are related with each other. The model is capable of generating high persistence and volatility even when there is no intrinsic persistence and structural shocks are white noise. We also show that the degree of the bank's data uncertainty is endogenously determined by the degree of private agents' uncertainty about inflation target — the measurement problem can arise endogenously from lack of credibility. Although much of the previous literature has already suggested the great importance of considering data uncertainty in the conduct of monetary policy, it has taken the data uncertainty as exogenously given. Our model implies that decreasing the private agents' uncertainty about inflation target can make the measurement problem less serious for the central bank.

Our model can have some implications for yield curve. As Gurkaynak et al. (2005) shows, long-term nominal interest rates tend to be sensitive to changes in current monetary policy actions when there is uncertainty about nominal anchor. This is because current monetary policy actions bring some news about long-run inflation target. Our model predicts similar results. While their model predicts 'shifts' in the yield curve in response to monetary policy, our model would predict both 'shifts' and 'the change in slopes'. We plan to investigate this question in



future research.

Finally, it would be interesting to examine some other monetary policy regimes with stronger nominal anchor. In the present paper, it is assumed that the bank changes the nominal interest rate in response to deviations of inflation from its target value. It would be interesting to analyse price level targeting in the context of interest-rate rules, or monetary-aggregate control instead of interest-rate control. As is well known, price level targeting and monetary aggregate control have stronger nominal anchor than inflation targeting. It would be important to analyse how those different policy regimes perform under imperfect credibility about nominal anchor.

# Appendix

## A Bank's filtering problem

### A.1 Constructing an observation equation of the bank

From (1) and (14), the bank's observation equation is given by

$$i_t = r_t^n + (1 - \phi^{-1})E_{t|p}\pi^* + \phi^{-1}E_{t|p}E_{t+1|c}\pi_{t+1|p}^*. \quad (\text{A.1})$$

In order to solve the bank's filtering problem, it is convenient to rewrite (A.1) in terms of  $\pi_{0|p}^*$ . By taking the conditional expectation  $E_{t|c}$  of equation (19) and subtracting that conditional expectations from (19), we have

$$E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^* = \alpha_t \left( E_{t|c}\pi_{0|p}^* - \pi_{0|p}^* \right), \quad (\text{A.2})$$

and therefore

$$E_{t|p}E_{t+1|c}\pi_{t+1|p}^* - E_{t|p}\pi^* = \alpha_{t+1} \left( E_{t|p}E_{t+1|c}\pi_{0|p}^* - \pi_{0|p}^* \right). \quad (\text{A.3})$$

Here we use the fact that  $E_{t|p}\pi_{t+1|p}^* = E_{t|p}\pi^*$ . Equation (A.2) shows that what matters to the difference between the perceived inflation target and the bank's belief the perceived target is the difference of the initial belief ( $\pi_{0|p}^*$ ) between the two of them. As  $t \rightarrow \infty$ , the difference will disappear. This is because (19) implies that the private agents eventually learn about the inflation target, and the bank knows this fact.

Substituting (A.3) into (A.1), one obtains

$$i_t = r_t^n + E_{t|p}\pi^* + \phi^{-1}\alpha_{t+1} \left( E_{t|p}E_{t+1|c}\pi_{0|p}^* - \pi_{0|p}^* \right).$$

Substituting (19) into the above equation, and collecting the variables that are observable to the bank to the left hand side and the unobservables to the right hand side, one obtains

$$i_t - (1 - a_t)\pi^* - \frac{1 - a_t}{1 - \phi} \bar{u}_t = r_t^n + (a_t - \phi^{-1}a_{t+1}) \pi_{0|p}^* + \phi^{-1}a_{t+1} E_{t|p} E_{t+1|c} \pi_{0|p}^*. \quad (\text{A.4})$$

Equation (A.4) involves the private-sector expectations about the bank's future belief about  $\pi_{0|p}^*$ . This is an implication of the forward-looking nature of inflation. The term  $E_{t|p} E_{t+1|c} \pi_{0|p}^*$  comes from the last term in equation (A.1), which in turn comes from private-sector inflation expectations about future monetary policy. The private sector expectations about future monetary policy depends on their expectations about the bank's filtering in the subsequent periods.

Now the remaining task is to compute the equilibrium and the bank's filtering. The right hand side of equation (A.4) still contains endogenous variables, namely,  $E_{t|p} E_{t+1|c} \pi_{0|p}^*$ . This should be determined jointly with the bank's filtering. In the next section, we will compute the equilibrium and the filtering by the method of undetermined coefficients. We first guess the equilibrium form and solve the filtering given that guess, and then compute the equilibrium given the filtering.

## A.2 Deriving the equilibrium and the bank's filtering

Define  $X_t$  as the bank's observable variables (the right hand side of equation (A.4)):

$$X_t \equiv i_t - (1 - a_t)\pi^* - \frac{1 - a_t}{1 - \phi} \bar{u}_t.$$

First of all, notice that, in this economy, the state of the economy can be represented by  $X_t$ ,  $r_t^n$ ,  $\pi_{0|p}^*$ , and  $E_{t-1|c} \pi_{0|p}^*$ . Therefore, we guess that the equilibrium

takes the following form:

$$A_t X_t = r_t^n + B_t \pi_{0|p}^* + C_t E_{t-1|c} \pi_{0|p}^*, \quad (\text{A.5})$$

where  $A_t, B_t, C_t$  are time-varying coefficients to be determined. Since  $E_{t-1|c} \pi_{0|p}^*$  is observable to the bank at time  $t$ , we can define the new observation equation of the bank as

$$A_t X_t - C_t E_{t-1|c} \pi_{0|p}^* = r_t^n + B_t \pi_{0|p}^*. \quad (\text{A.6})$$

Again, the left hand side is observable to the bank, and the right hand side is unobservable. Equation (A.6) shows that the bank's filtering problem reduces to the sequential updating of a constant,  $\pi_{0|p}^*$ . A slight complication is that it involves a time-varying coefficient  $B_t$ . Define the new observable variable as  $Y_t \equiv A_t X_t - C_t E_{t-1|c} \pi_{0|p}^*$ . From the normality assumption (7),  $Y_t$  is again normally distributed:

$$Y_t \sim N \left( B_t \pi_{0|p}^*, \sigma_r^2 \right).$$

Let the prior distribution be:

$$B_{t-1} \pi_{0|p}^* \sim N \left( B_{t-1} E_{t-1|c} \pi_{0|p}^*, \tau_{t-1|c}^{-1} \right),$$

where  $\tau_{t-1|c}$  is the bank's precision at the end of time  $t-1$  (i.e., before the bank observes time- $t$  variables). Then the prior for  $B_t \pi_{0|p}^*$  is given by (see DeGroot (1970))

$$B_t \pi_{0|p}^* \sim N \left( B_t E_{t-1|c} \pi_{0|p}^*, \frac{B_t^2}{B_{t-1}^2} \tau_{t-1|c}^{-1} \right). \quad (\text{A.7})$$

Then, the posterior mean of  $B_t \pi_{0|p}^*$  is given by

$$B_t E_{t|c} \pi_{0|p}^* = d_t B_t E_{t-1|c} \pi_{0|p}^* + (1 - d_t) Y_t, \quad (\text{A.8})$$

where

$$d_t \equiv \frac{\frac{B_{t-1}^2}{B_t^2} \tau_{t-1|c}}{\frac{B_{t-1}^2}{B_t^2} \tau_{t-1|c} + \gamma_r} \quad (\text{A.9})$$

and  $\gamma_r \equiv 1/\sigma_r^2$ . The updating equation of  $\tau_{t|c}$  can be written as

$$\tau_{t|c} = \frac{B_{t-1}^2}{B_t^2} \tau_{t-1|c} + \gamma_r. \quad (\text{A.10})$$

Using the definition of  $Y_t$ , one can rewrite (A.8) as

$$E_{t|c} \pi_{0|p}^* = \left\{ d_t - \left( 1 - d_t \frac{C_t}{B_t} \right) \right\} E_{t-1|c} \pi_{0|p}^* + (1 - d_t) \frac{A_t}{B_t} X_t. \quad (\text{A.11})$$

This implies that, at time  $t + 1$ ,

$$E_{t+1|c} \pi_{0|p}^* = \left\{ d_{t+1} - \left( 1 - d_{t+1} \frac{C_{t+1}}{B_{t+1}} \right) \right\} E_{t|c} \pi_{0|p}^* + (1 - d_{t+1}) \frac{A_{t+1}}{B_{t+1}} X_{t+1}.$$

Taking expectations conditional on the private-sector information at time  $t$ , and arranging terms, one obtains

$$E_{t|p} E_{t+1|c} \pi_{0|p}^* = (1 - d_{t+1}) \pi_{0|p}^* + d_{t+1} E_{t|c} \pi_{0|p}^*. \quad (\text{A.12})$$

Here we use the assumption that the bank announces  $E_{t|c} \pi_{0|p}^*$  at time  $t$ . Substituting (A.12) into (A.11), and then substitute the resulting equation into (A.4).

Then we can verify that the equilibrium is indeed given by:

$$\begin{aligned} & \left\{ 1 - \phi^{-1} a_{t+1} (1 - d_t) \frac{A_t}{B_t} \right\} X_t \\ &= r_t^n + \{ a_t - \phi^{-1} a_{t+1} d_{t+1} \} \pi_{0|p}^* + \left\{ \phi^{-1} a_{t+1} d_{t+1} \left( d_t - \frac{1 - d_t}{B_t} C_t \right) \right\} E_{t-1|c} \pi_{0|p}^*. \end{aligned} \quad (\text{A.13})$$

By comparing our guess (A.5) and (A.13), we have the following three identities:

$$A_t = 1 - \phi^{-1} a_{t+1} (1 - d_t) \frac{A_t}{B_t} \quad (\text{A.14})$$

$$B_t = a_t - \phi^{-1} a_{t+1} d_{t+1} \quad (\text{A.15})$$

$$C_t = \phi^{-1} a_{t+1} d_{t+1} \left( d_t - \frac{1 - d_t}{B_t} C_t \right) \quad (\text{A.16})$$

By substituting (A.9), we notice that equations (A.15) and (A.10) represent a system of deterministic (non-linear) difference equation with respect to  $B_t$  and  $\tau_{t|c}$

$$B_t = a_t - \phi^{-1} a_{t+1} \frac{\frac{B_t^2}{B_{t+1}^2} \tau_{t|c}}{\frac{B_t^2}{B_{t+1}^2} \tau_{t|c} + \gamma_r}, \quad (\text{A.17})$$

$$\tau_{t|c} = \frac{B_{t-1}^2}{B_t^2} \tau_{t-1|c} + \gamma_r. \quad (\text{A.10})$$

Once  $B_t$  and  $\tau_{t|c}$  are solved,  $d_t$  is solved by (A.9), equations (A.14) and (A.16) respectively solve  $A_t$  and  $C_t$ .

Notice that equation (A.15) and (A.10) show that  $B_t$  depends both on  $B_{t-1}$  and  $B_{t+1}$ . Dependence on  $B_{t-1}$  is just a direct implication of recursive filtering. Dependence on  $B_{t+1}$  is an implication of the interaction between forward-looking nature of inflation and the bank's filtering. In our model, the current equilibrium variables depend on the private-sector expectations about future monetary policy. And future monetary policy depends on how the central bank will estimate the future state of the economy. This is represented in equation (A.12). Therefore, the way the bank will estimate the state of the economy in the next period will affect the current equilibrium. As a result, the bank's filtering in the current period is affected by its filtering in future periods.

The existing literature such as Aoki (2003) and Svensson and Woodford (2003)

focus on ‘stationary’ filtering by central bank, so that the Kalman gain is constant over time. In our model, since the bank’s learning is about a constant  $\pi_{0|p}^*$ , filtering is not stationary. That is the main reason why the bank’s Kalman gain, namely,  $d_t$  is not constant over time. In general, even if the bank is estimating time-varying variables, Kalman gains are not necessarily constant. Therefore, the dependence of equilibrium on the future Kalman gain of the central bank is a general property of rational equilibrium models with forward-looking private sector.

Let us finish this section by characterising the stochastic properties of the central-bank uncertainty. By using (A.11), (A.5), and (A.15), the evolution of  $E_{t|c}\pi_{0|p}^*$  is given by

$$E_{t|c}\pi_{0|p}^* = d_t E_{t-1|c}\pi_{0|p}^* + (1 - d_t)\pi_{0|p}^* + \frac{1 - d_t}{\alpha_t - \phi^{-1}\alpha_{t+1}d_{t+1}} r_t^n. \quad (\text{A.18})$$

Substitution of (A.18) into (A.2) yields

$$E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^* = \alpha_t d_t \left( E_{t-1|c}\pi_{0|p}^* - \pi_{0|p}^* \right) + \frac{\alpha_t(1 - d_t)}{\alpha_t - \phi^{-1}\alpha_{t+1}d_{t+1}} r_t^n. \quad (\text{A.19})$$

Equation (A.19) clearly shows the dependence on the bank’s current estimate of the economy on its future filtering ( $d_{t+1}$ ). It also shows that  $E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^* \rightarrow 0$  as  $t \rightarrow \infty$ .

Finally, as discussed in 3.3, there is a close relationship between the bank’s estimates of the perceived inflation target and the estimates of the natural rate. Taking the conditional expectation  $E_{t|c}$  of equation (A.6) and subtracting that conditional expectations from (A.6), we have

$$r_t^n - E_{t|c}r_t^n = B_t \left( E_{t|c}\pi_{0|p}^* - \pi_{0|p}^* \right). \quad (\text{A.20})$$

Using (A.20) and (A.2), we can see that  $E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^*$  represents the

bank's estimation error about  $r_t^n$

$$E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^* = \frac{\alpha_t}{B_t} (r_t^n - E_{t|c}r_t^n), \quad (\text{A.21})$$

which is equation (23). Therefore, the central-bank uncertainty about the real rate and about the private-sector belief are related with each other.

## B Variance and autocorrelation of inflation

We can rewrite equation (24) as

$$\begin{aligned} \pi_t &= \pi^* + \phi^{-1} [(E_{t|p}\pi^* - \pi^* - u_t) + (E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^*)] \\ &\equiv \pi^* + \phi^{-1} [\xi_t + \zeta_t], \end{aligned} \quad (\text{B.1})$$

where

$$\xi_t \equiv E_{t|p}\pi^* - \pi^* - u_t$$

and

$$\zeta_t \equiv E_{t|c}E_{t|p}\pi^* - E_{t|p}\pi^*.$$

By using (20),  $\xi_t$  can be written as

$$\xi_t = b_t\xi_{t-1} + b_tu_{t-1} - \frac{b_t - \phi}{1 - \phi}u_t. \quad (\text{B.2})$$

By using (22),  $\zeta_t$  can be written as

$$\zeta_t = g_t\zeta_{t-1} + h_tr_t^n, \quad (\text{B.3})$$

where  $g_t \equiv b_td_t$  and  $h_t = (1 - d_t)\alpha_t/B_t$ . Note that  $0 < g_t < 1$ ,  $\lim_{t \rightarrow \infty} g_t = 1$ , and  $h_t > 0$ ,  $\lim_{t \rightarrow \infty} h_t = 0$ .



Since  $u_t$  and  $r_t^n$  are independent so are  $\xi_t$  and  $\zeta_t$ . Therefore we have

$$V[\pi_t] = \phi^{-2}(V[\xi_t] + V[\zeta_t]) \quad (\text{B.4})$$

and

$$\text{Cov}[\pi_t, \pi_{t-1}] = \phi^{-2} [\text{Cov}[\xi_t, \xi_{t-1}] + \text{Cov}[\zeta_t, \zeta_{t-1}]]. \quad (\text{B.5})$$

Equation (B.2) implies that

$$V[\xi_t] = \frac{\sigma_u^2}{(1-\phi)^2} \left[ (b_t - \phi)^2 + \sum_{k=0}^{t-1} \left( \prod_{j=k}^{t-1} b_{j+1}^2 \right) (b_k - 1)^2 \right] \quad (\text{B.6})$$

and

$$\text{Cov}[\xi_t, \xi_{t-1}] = \frac{b_t \sigma_u^2}{(1-\phi)^2} \left[ (b_{t-1} - 1)(b_{t-1} - \phi) + \sum_{k=0}^{t-2} \left( \prod_{j=k}^{t-2} b_{j+1}^2 \right) (b_{k-1})^2 \right]. \quad (\text{B.7})$$

Since  $0 < b_t < 1$  and  $\lim_{t \rightarrow \infty} b_t = 0$  we obtain  $\lim_{t \rightarrow \infty} V[\xi_t] = \sigma_u^2$  and  $\lim_{t \rightarrow \infty} \text{Cov}[\xi_t, \xi_{t-1}] = 0$ .

Equation (B.3) implies that

$$V[\zeta_t] = \sigma_r^2 \left[ h_t^2 + \sum_{k=0}^{t-1} \left( \prod_{j=k}^{t-1} g_{j+1}^2 \right) h_k^2 \right], \quad (\text{B.8})$$

and

$$\text{Cov}[\zeta_t, \zeta_{t-1}] = g_t \sigma_r^2 \left[ h_{t-1} + \sum_{k=0}^{t-2} \left( \prod_{j=k}^{t-2} g_{j+1}^2 \right) h_k^2 \right]. \quad (\text{B.9})$$

Since  $0 < g_t < 1$ ,  $\lim_{t \rightarrow \infty} g_t = 1$ ,  $0 < h_t$ ,  $\lim_{t \rightarrow \infty} h_t = 0$ , we obtain  $\lim_{t \rightarrow \infty} V[\zeta_t] = 0$  and  $\lim_{t \rightarrow \infty} \text{Cov}[\zeta_t, \zeta_{t-1}] = 0$ .

## C Robustness analysis of Section

In this Appendix, we confirm that the above basic results shown in Section 4 are robust against different parameters. Table 1 shows the parameter for four robustness analysis.

	Benchmark	Case 1	Case 2	Case 3	Case 4
$\pi^*$	2	2	2	2	2
$E_{0 p}\pi^*$	10	<b>20</b>	10	10	10
$\gamma_u$	1	1	1	<b>4</b>	1
$\gamma_r$	0.44	0.44	0.44	0.44	0.44
$\phi$	1.5	1.5	<b>1.1</b>	1.5	1.5
$\tau_{0 p}$	1	1	1	1	<b>10</b>
$\tau_{0 c}$	1	1	1	1	1

Table 1: Parameter values for sensitivity analysis

**Case 1: higher perceived target** Initial perceived inflation target is set to 20 %. This may correspond to the case of the introduction of inflation targeting in some emerging countries. When Chile, Israel and Hungary adapted inflation targeting, the inflation rates were about 20 %.

**Case 2: less aggressive monetary policy**  $\phi$  is set to 1.1, which is lower than the original Taylor rule

**Case 3: smaller monetary policy shock**  $\sigma_u$  is set to 0.5 % and hence  $\gamma_u=0.4$ . According to Roberts (2004), this is almost in line with the Fed policy after 1984.

**Case 4: More stubborn belief** The initial value of the private-sector precision parameter,  $\tau_{0|p}$ , is 10, which means that the private sector is more convinced by their own belief.

Figure 2-5 shows that higher volatility of inflation in the first-half period results from higher perceived target (Case1), less aggressive monetary policy (Case2), larger monetary policy shock (Case3) and more stubborn belief (Case4). In all these cases, as in the benchmark case, the larger  $E_{0|c}\pi_{0|p}^* - \pi_{0|p}^*$ , the larger the volatility of inflation in the first-half period. Also, the estimated AR parameter  $\alpha$ , the standard deviation of the innovation  $\sigma_\eta$ , and hence the volatility of inflation  $Var[\pi_t]$  become smaller in the second half period than the first half period.

Benchmark ( $\pi_{0,p}^* = 10$ , Black line) vs. Higher perceived target ( $\pi_{0,p}^* = 20$ , Gray line)  
 ( Solid line: Sample period 1-20, Dashed line: Sample period 21-40 )

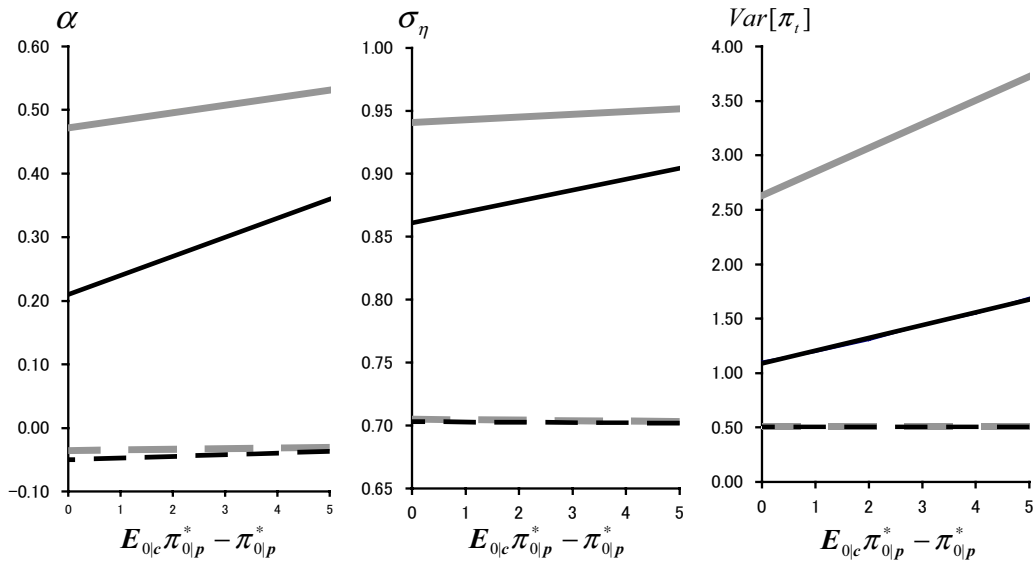


Figure 2: Robustness analysis: case 1

Benchmark ( $\phi = 1.5$ , Black line) vs. Less aggressive monetary policy ( $\phi = 1.1$ , Gray line)  
 ( Solid line: Sample period 1-20, Dashed line: Sample period 21-40 )

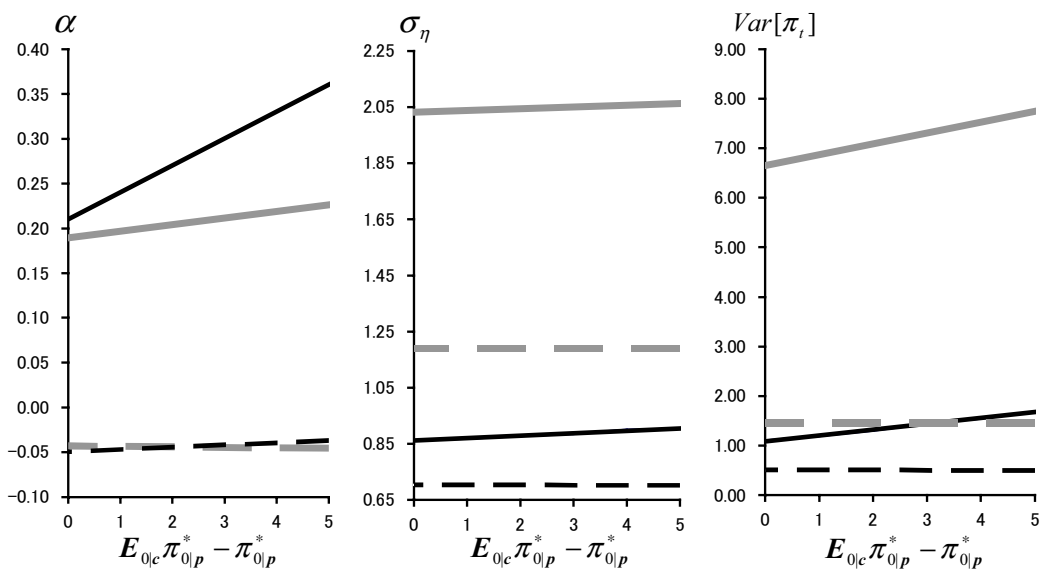


Figure 3: Robustness analysis: case 2

Benchmark ( $\gamma_u = 1$ , Black line) vs. Smaller monetary policy shock ( $\gamma_u = 4$ , Gray line)  
 ( Solid line: Sample period 1–20, Dashed line: Sample period 21–40 )

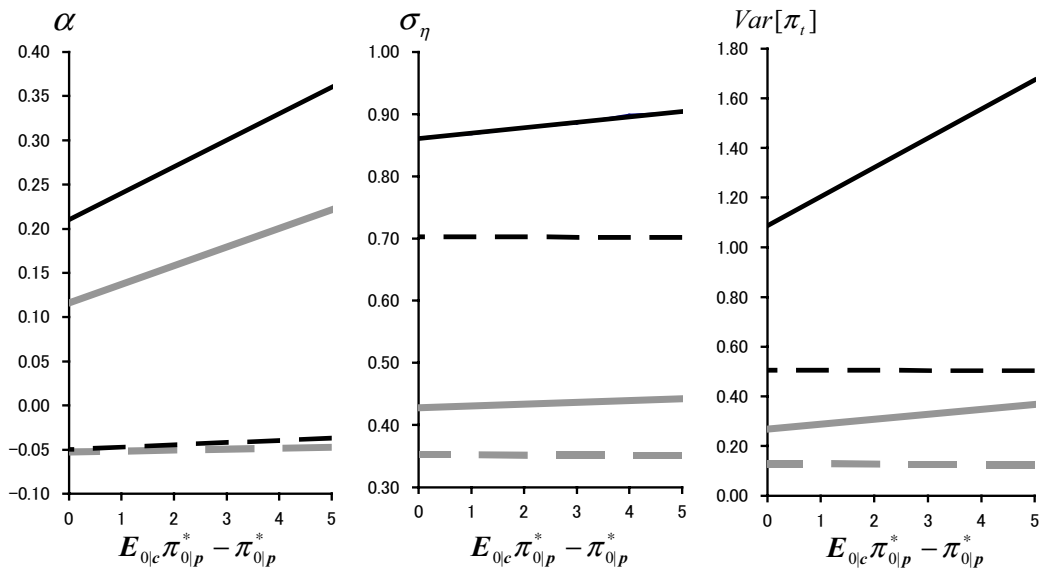


Figure 4: Robustness analysis: case 3

Benchmark ( $\tau_{0|p} = 1$ , Black line) vs. More stubborn belief ( $\tau_{0|p} = 10$ , Gray line)  
 ( Solid line: Sample period 1–20, Dashed line: Sample period 21–40 )

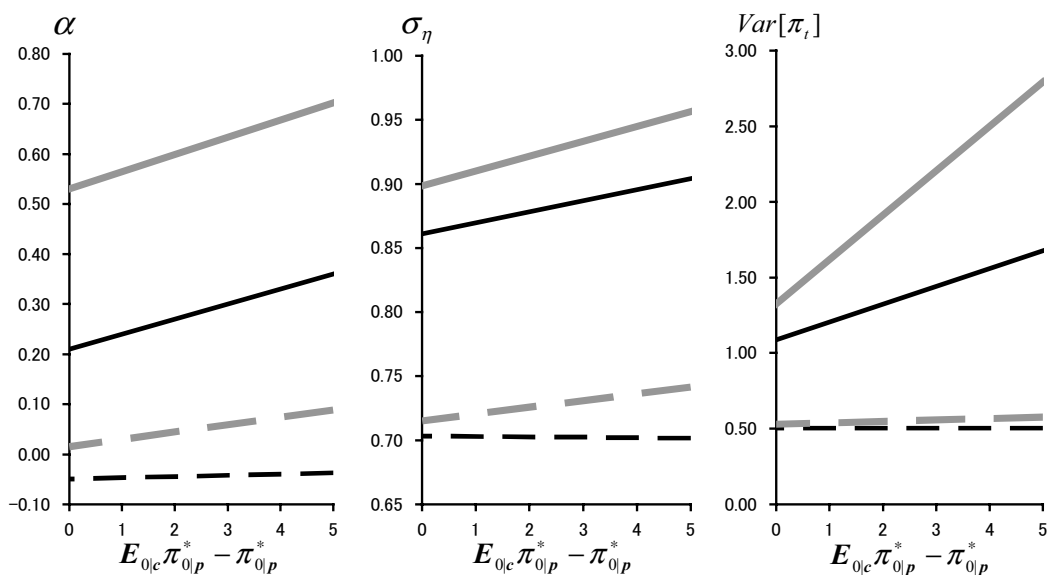


Figure 5: Robustness analysis: case 4

## References

- Ahmed, S., Levin, A., Wilson, B., 2004. Recent u.s. macroeconomic stability: Good policies, good practices, or good luck? *Review of economics and statistics* 86, 824–832.
- Amato, J., Shin, H. S., 2003. Public and private information in monetary policy models. *BIS Working Papers* No 138.
- Aoki, K., 2003. On the optimal monetary policy response to noisy indicators. *Journal of Monetary Economics* 50 (3), 501–523.
- Aoki, K., 2006. Price-level determination under dispersed information and monetary policy. *Japanese Economic Review* 57, 406–425 (Invited lecture).
- Bekaert, G., Cho, S., Moreno, A., 2005. New-Keynesian macroeconomics and the term structure. working paper, Columbia University.
- Benati, L., 2004. Evolving post-World War II U.K. economic performance. *Journal of Money, Credit, and Banking* 36(5), 691–718.
- Benati, L., 2007. Investigating inflation persistence across monetary regimes. *ECB Working Paper*, forthcoming.
- Bernanke, B., 2004. The great moderation. Remarks at the meetings of the Eastern Economic Association.
- Cogley, T., Sargent, T., 2004. Drifts and volatilities: Monetary policies and outcomes in the post WWII US. working paper, New York University.
- DeGroot, M., 1970. *Optimal Statistical Decisions*. John Wiley and Sons, New Jersey.
- Erceg, C., Levin, A., 2003. Imperfect credibility and inflation persistence. *Journal of monetary economics* 50 (4), 915–944.
- Gurkaynak, R., Sack, B., Swanson, E., 2005. The excess sensitivity of long-term interest rates: Evidence and implications for macroeconomic models. *American Economic Review* forthcoming.
- Kozicki, S., Tinsley, P., 2001. Term structure views of monetary policy under alternative models of agent expectations. *journal of economic dynamics and control* 25, 149–184.
- Kozicki, S., Tinsley, P., 2005. Permanent and transitory policy shocks in an estimated model with asymmetric information. *Journal of economic dynamics and control* 29 (11), 1985–2015.
- Laubach, T., Williams, J., 2003. Measuring the natural rate of interest. *review of economics and statistics* 85(4), 1063–1070.

- Orphanides, A., 2001. Monetary policy rules based on real-time data. *American Economic Review* 91, 964–985.
- Orphanides, A., May 2002. Monetary policy rules and the great inflation. *American economic review* 92, 115–120.
- Orphanides, A., 2003. Monetary policy evaluation with noisy information. *Journal of Monetary Economics* 50 (3), 605–631.
- Orphanides, A., Williams, J., 2005. The decline of activist stabilisation policy: Natural rate misperceptions, learning, and expectations. *Journal of Economic Dynamics and Control* 29, 1927–1950.
- Stock, J., Watson, M., 2002. Has the business cycle changed and why. NBER macroeconomics annual.
- Stock, J., Watson, M., 2003. Has the business cycle changed? evidence and explanations. prepared for the Federal Reserve Bank of Kansas City Symposium, “Monetary policy and uncertainty”.
- Svensson, L., Woodford, M., 2003. Indicator variables and optimal policy. *Journal of Monetary Economics* 50 (3), 691–720.
- Woodford, M., 2002. Imperfect common knowledge and the effects of monetary policy. In: Aghion, P., Frydman, R., Stiglitz, J., Woodford, M. (Eds.), *Knowledge, Information, and Expectations in Modern Macroeconomics: In Honor of Edmund S. Phelps*. Princeton University Press, Princeton, NJ.
- Woodford, M., 2003. *Interest and Prices*. Princeton University Press, Princeton.

## The following Discussion Papers have been published since 2006:

### Series 1: Economic Studies

1	2006	The dynamic relationship between the Euro overnight rate, the ECB's policy rate and the term spread	Dieter Nautz Christian J. Offermanns
2	2006	Sticky prices in the euro area: a summary of new micro evidence	Álvarez, Dhyne, Hoeberichts Kwapil, Le Bihan, Lünnemann Martins, Sabbatini, Stahl Vermeulen, Vilmunen
3	2006	Going multinational: What are the effects on home market performance?	Robert Jäckle
4	2006	Exports versus FDI in German manufacturing: firm performance and participation in international markets	Jens Matthias Arnold Katrin Hussinger
5	2006	A disaggregated framework for the analysis of structural developments in public finances	Kremer, Braz, Brosens Langenus, Momigliano Spolander
6	2006	Bond pricing when the short term interest rate follows a threshold process	Wolfgang Lemke Theofanis Archontakis
7	2006	Has the impact of key determinants of German exports changed? Results from estimations of Germany's intra euro-area and extra euro-area exports	Kerstin Stahn
8	2006	The coordination channel of foreign exchange intervention: a nonlinear microstructural analysis	Stefan Reitz Mark P. Taylor
9	2006	Capital, labour and productivity: What role do they play in the potential GDP weakness of France, Germany and Italy?	Antonio Bassanetti Jörg Döpke, Roberto Torrini Roberta Zizza

10	2006	Real-time macroeconomic data and ex ante predictability of stock returns	J. Döpke, D. Hartmann C. Pierdzioch
11	2006	The role of real wage rigidity and labor market frictions for unemployment and inflation dynamics	Kai Christoffel Tobias Linzert
12	2006	Forecasting the price of crude oil via convenience yield predictions	Thomas A. Knetsch
13	2006	Foreign direct investment in the enlarged EU: do taxes matter and to what extent?	Guntram B. Wolff
14	2006	Inflation and relative price variability in the euro area: evidence from a panel threshold model	Dieter Nautz Juliane Scharff
15	2006	Internalization and internationalization under competing real options	Jan Hendrik Fisch
16	2006	Consumer price adjustment under the microscope: Germany in a period of low inflation	Johannes Hoffmann Jeong-Ryeol Kurz-Kim
17	2006	Identifying the role of labor markets for monetary policy in an estimated DSGE model	Kai Christoffel Keith Küster Tobias Linzert
18	2006	Do monetary indicators (still) predict euro area inflation?	Boris Hofmann
19	2006	Fool the markets? Creative accounting, fiscal transparency and sovereign risk premia	Kerstin Bernoth Guntram B. Wolff
20	2006	How would formula apportionment in the EU affect the distribution and the size of the corporate tax base? An analysis based on German multinationals	Clemens Fuest Thomas Hemmelgarn Fred Ramb



21	2006	Monetary and fiscal policy interactions in a New Keynesian model with capital accumulation and non-Ricardian consumers	Campbell Leith Leopold von Thadden
22	2006	Real-time forecasting and political stock market anomalies: evidence for the U.S.	Martin Bohl, Jörg Döpke Christian Pierdzioch
23	2006	A reappraisal of the evidence on PPP: a systematic investigation into MA roots in panel unit root tests and their implications	Christoph Fischer Daniel Porath
24	2006	Margins of multinational labor substitution	Sascha O. Becker Marc-Andreas Müндler
25	2006	Forecasting with panel data	Badi H. Baltagi
26	2006	Do actions speak louder than words? Household expectations of inflation based on micro consumption data	Atsushi Inoue Lutz Kilian Fatma Burcu Kiraz
27	2006	Learning, structural instability and present value calculations	H. Pesaran, D. Pettenuzzo A. Timmermann
28	2006	Empirical Bayesian density forecasting in Iowa and shrinkage for the Monte Carlo era	Kurt F. Lewis Charles H. Whiteman
29	2006	The within-distribution business cycle dynamics of German firms	Jörg Döpke Sebastian Weber
30	2006	Dependence on external finance: an inherent industry characteristic?	George M. von Furstenberg Ulf von Kalckreuth
31	2006	Comovements and heterogeneity in the euro area analyzed in a non-stationary dynamic factor model	Sandra Eickmeier

32	2006	Forecasting using a large number of predictors: is Bayesian regression a valid alternative to principal components?	Christine De Mol Domenico Giannone Lucrezia Reichlin
33	2006	Real-time forecasting of GDP based on a large factor model with monthly and quarterly data	Christian Schumacher Jörg Breitung
34	2006	Macroeconomic fluctuations and bank lending: evidence for Germany and the euro area	S. Eickmeier B. Hofmann, A. Worms
35	2006	Fiscal institutions, fiscal policy and sovereign risk premia	Mark Hallerberg Guntram B. Wolff
36	2006	Political risk and export promotion: evidence from Germany	C. Moser T. Nestmann, M. Wedow
37	2006	Has the export pricing behaviour of German enterprises changed? Empirical evidence from German sectoral export prices	Kerstin Stahn
38	2006	How to treat benchmark revisions? The case of German production and orders statistics	Thomas A. Knetsch Hans-Eggert Reimers
39	2006	How strong is the impact of exports and other demand components on German import demand? Evidence from euro-area and non-euro-area imports	Claudia Stirböck
40	2006	Does trade openness increase firm-level volatility?	C. M. Buch, J. Döpke H. Strotmann
41	2006	The macroeconomic effects of exogenous fiscal policy shocks in Germany: a disaggregated SVAR analysis	Kirsten H. Heppke-Falk Jörn Tenhofen Guntram B. Wolff

42	2006	How good are dynamic factor models at forecasting output and inflation? A meta-analytic approach	Sandra Eickmeier Christina Ziegler
43	2006	Regionalwährungen in Deutschland – Lokale Konkurrenz für den Euro?	Gerhard Rösl
44	2006	Precautionary saving and income uncertainty in Germany – new evidence from microdata	Nikolaus Bartsch
45	2006	The role of technology in M&As: a firm-level comparison of cross-border and domestic deals	Rainer Frey Katrin Hussinger
46	2006	Price adjustment in German manufacturing: evidence from two merged surveys	Harald Stahl
47	2006	A new mixed multiplicative-additive model for seasonal adjustment	Stephanus Arz
48	2006	Industries and the bank lending effects of bank credit demand and monetary policy in Germany	Ivo J.M. Arnold Clemens J.M. Kool Katharina Raabe
01	2007	The effect of FDI on job separation	Sascha O. Becker Marc-Andreas Müндler
02	2007	Threshold dynamics of short-term interest rates: empirical evidence and implications for the term structure	Theofanis Archontakis Wolfgang Lemke
03	2007	Price setting in the euro area: some stylised facts from individual producer price data	Dias, Dossche, Gautier Hernando, Sabbatini Stahl, Vermeulen
04	2007	Unemployment and employment protection in a unionized economy with search frictions	Nikolai Stähler

05	2007	End-user order flow and exchange rate dynamics	S. Reitz, M. A. Schmidt M. P. Taylor
06	2007	Money-based interest rate rules: lessons from German data	C. Gerberding F. Seitz, A. Worms
07	2007	Moral hazard and bail-out in fiscal federations: evidence for the German Länder	Kirsten H. Heppke-Falk Guntram B. Wolff
08	2007	An assessment of the trends in international price competitiveness among EMU countries	Christoph Fischer
09	2007	Reconsidering the role of monetary indicators for euro area inflation from a Bayesian perspective using group inclusion probabilities	Michael Scharnagl Christian Schumacher
10	2007	A note on the coefficient of determination in regression models with infinite-variance variables	Jeong-Ryeol Kurz-Kim Mico Loretan
11	2007	Exchange rate dynamics in a target zone - a heterogeneous expectations approach	Christian Bauer Paul De Grauwe, Stefan Reitz
12	2007	Money and housing - evidence for the euro area and the US	Claus Greiber Ralph Setzer
13	2007	An affine macro-finance term structure model for the euro area	Wolfgang Lemke
14	2007	Does anticipation of government spending matter? Evidence from an expectation augmented VAR	Jörn Tenhofen Guntram B. Wolff
15	2007	On-the-job search and the cyclical dynamics of the labor market	Michael Krause Thomas Lubik
16	2007	Heterogeneous expectations, learning and European inflation dynamics	Anke Weber

17	2007	Does intra-firm bargaining matter for business cycle dynamics?	Michael Krause Thomas Lubik
18	2007	Uncertainty about perceived inflation target and monetary policy	Kosuke Aoki Takeshi Kimura

## Series 2: Banking and Financial Studies

01	2006	Forecasting stock market volatility with macroeconomic variables in real time	J. Döpke, D. Hartmann C. Pierdzioch
02	2006	Finance and growth in a bank-based economy: is it quantity or quality that matters?	Michael Koetter Michael Wedow
03	2006	Measuring business sector concentration by an infection model	Klaus Düllmann
04	2006	Heterogeneity in lending and sectoral growth: evidence from German bank-level data	Claudia M. Buch Andrea Schertler Natalja von Westernhagen
05	2006	Does diversification improve the performance of German banks? Evidence from individual bank loan portfolios	Evelyn Hayden Daniel Porath Natalja von Westernhagen
06	2006	Banks' regulatory buffers, liquidity networks and monetary policy transmission	Christian Merkl Stéphanie Stolz
07	2006	Empirical risk analysis of pension insurance – the case of Germany	W. Gerke, F. Mager T. Reinschmidt C. Schmieder
08	2006	The stability of efficiency rankings when risk-preferences and objectives are different	Michael Koetter
09	2006	Sector concentration in loan portfolios and economic capital	Klaus Düllmann Nancy Masschelein
10	2006	The cost efficiency of German banks: a comparison of SFA and DEA	E. Fiorentino A. Karmann, M. Koetter
11	2006	Limits to international banking consolidation	F. Fecht, H. P. Grüner

12	2006	Money market derivatives and the allocation of liquidity risk in the banking sector	Falko Fecht Hendrik Hakenes
01	2007	Granularity adjustment for Basel II	Michael B. Gordy Eva Lütkebohmert
02	2007	Efficient, profitable and safe banking: an oxymoron? Evidence from a panel VAR approach	Michael Koetter Daniel Porath
03	2007	Slippery slopes of stress: ordered failure events in German banking	Thomas Kick Michael Koetter
04	2007	Open-end real estate funds in Germany – genesis and crisis	C. E. Bannier F. Fecht, M. Tyrell
05	2007	Diversification and the banks' risk-return-characteristics – evidence from loan portfolios of German banks	A. Behr, A. Kamp C. Memmel, A. Pfingsten
06	2007	How do banks adjust their capital ratios? Evidence from Germany	Christoph Memmel Peter Raupach
07	2007	Modelling dynamic portfolio risk using risk drivers of elliptical processes	Rafael Schmidt Christian Schmieder
08	2007	Time-varying contributions by the corporate bond and CDS markets to credit risk price discovery	Niko Dötz
09	2007	Banking consolidation and small business finance – empirical evidence for Germany	K. Marsch, C. Schmieder K. Forster-van Aerssen

## **Visiting researcher at the Deutsche Bundesbank**

The Deutsche Bundesbank in Frankfurt is looking for a visiting researcher. Among others under certain conditions visiting researchers have access to a wide range of data in the Bundesbank. They include micro data on firms and banks not available in the public. Visitors should prepare a research project during their stay at the Bundesbank. Candidates must hold a Ph D and be engaged in the field of either macroeconomics and monetary economics, financial markets or international economics. Proposed research projects should be from these fields. The visiting term will be from 3 to 6 months. Salary is commensurate with experience.

Applicants are requested to send a CV, copies of recent papers, letters of reference and a proposal for a research project to:

Deutsche Bundesbank  
Personalabteilung  
Wilhelm-Epstein-Str. 14

60431 Frankfurt  
GERMANY