Fiscal and Monetary Policy with Heterogeneous Agents

Bundesbank Spring Conference 2024



* Active literature on Heterogeneous-Agent New-Keynesian models

- * **Today:** Three questions...
 - * What is a "HANK" model?
 - * When does heterogeneity matter for macro aggregates?

Demystifying "HANK" models

* How can "HANK" models help us make sense of the current economy?



- 1. Introduce a canonical "HANK" model
- 2. Fiscal policy: Persistent inflation
- 3. Monetary policy: Reliance on investment for transmission
- 4. Energy shocks: Stagflation

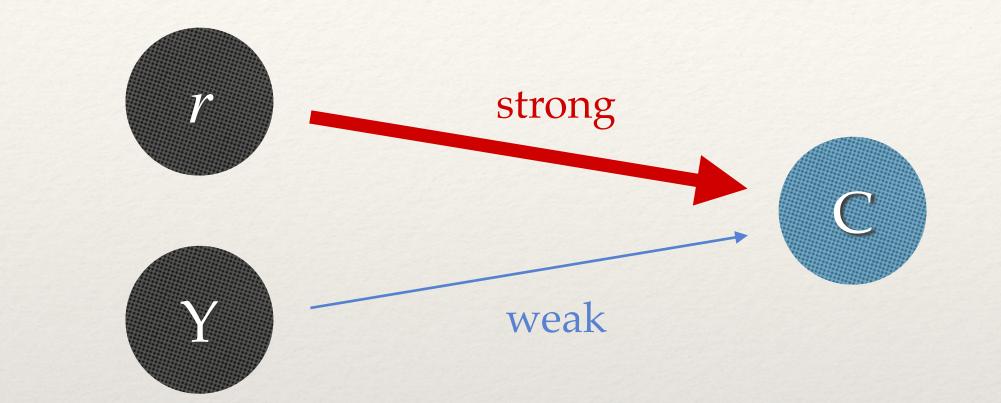
This talk



- 1. Introduce a canonical "HANK" model
- 2. Fiscal policy: Persistent inflation
- 3. Monetary policy: Reliance on investment for transmission
- 4. Energy shocks: Stagflation
- * Throughout: work in the sequence space! Will buy us a lot of tractability.
- * Based on joint agenda with Adrien Auclert and Matt Rognlie
 - + Rishabh Aggarwal, Bence Bardóczy, Hugo Monnery, Martin Souchier...

his tak

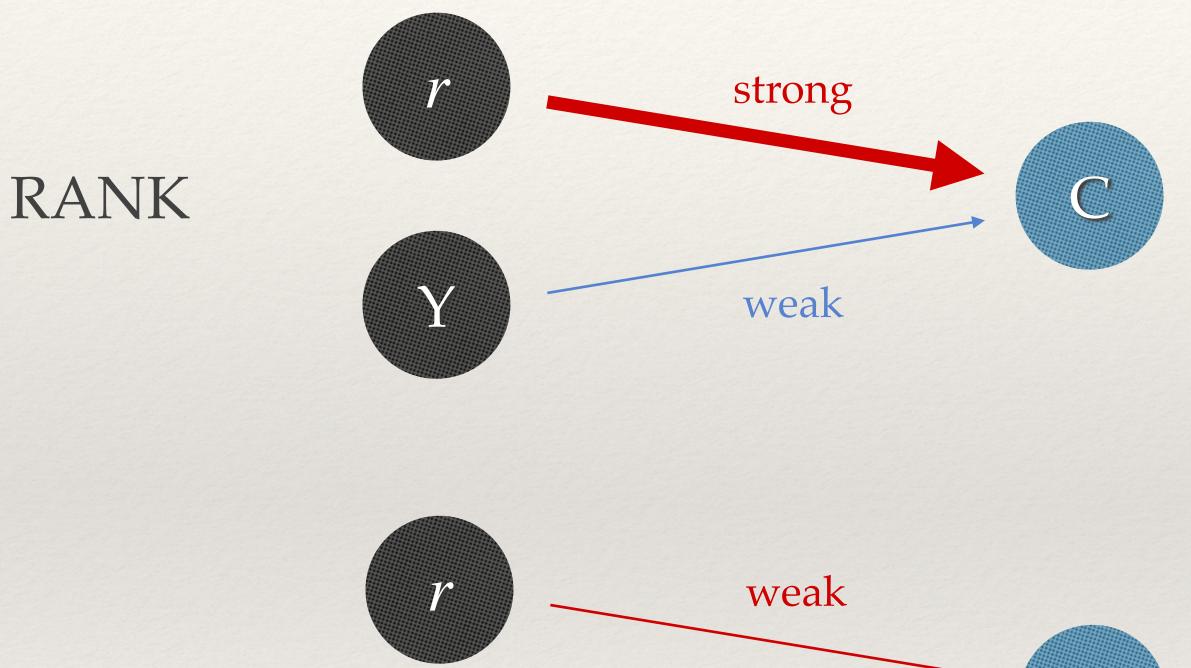
Core idea why HANK is so different



RANK

Consumption mostly determined by **interest rates**

Core idea why HANK is so different

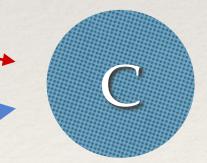


strong

HANK



Consumption mostly determined by **interest rates**



Consumption mostly determined by **income**

A canonical HANK model

- * The textbook representative-agent NK (RANK) model consists of:
 - 1. household side: representative agent
 - 2. fiscal policy: irrelevant due to Ricardian equivalence
 - 3. monetary policy: Taylor rule
 - 4. supply side: linear production, sticky prices set by firms



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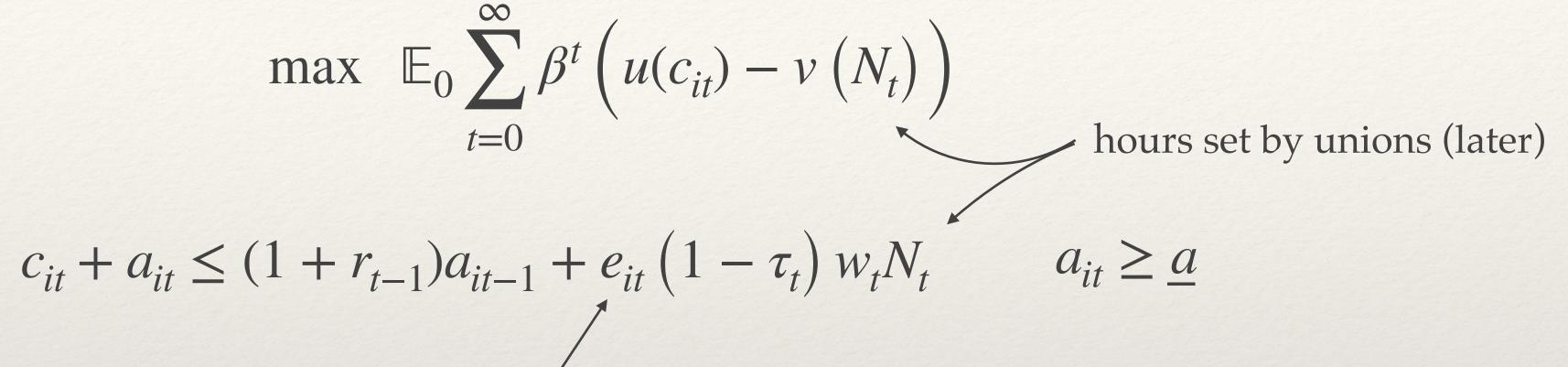
 - 2. fiscal policy: Andreande de Recentration de la company de la company
 - 3. monetary policy: Taylor rule Start with "real interest rate rule"
- * Will go over all four ingredients in an economy with perfect foresight
 - * without loss to first order (certainty equivalence)

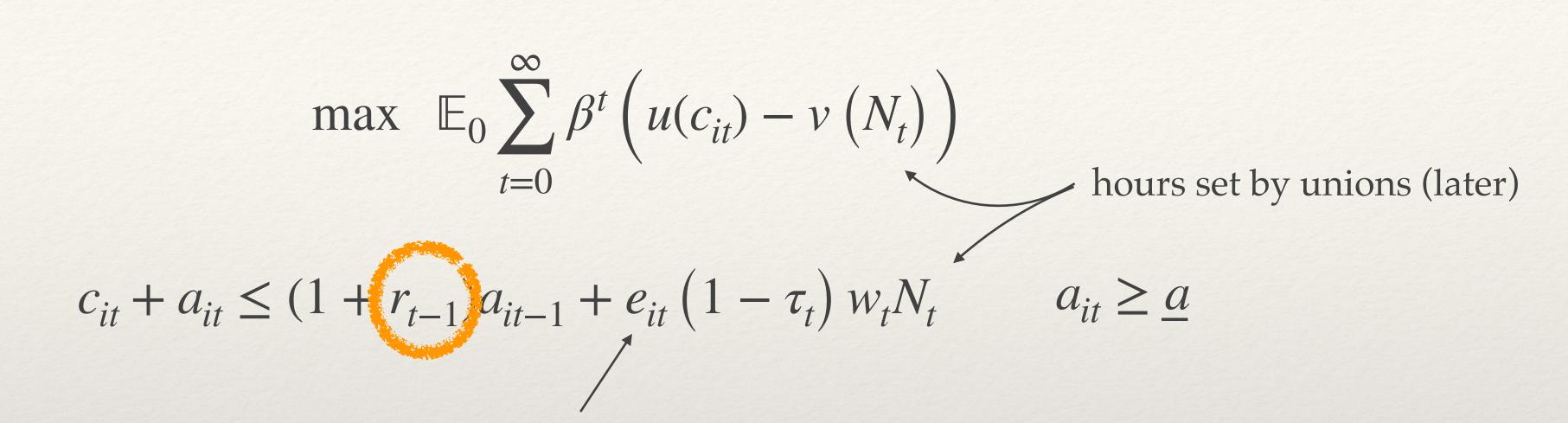
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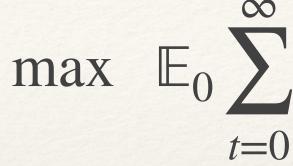
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4. supply side: linear production, sticky presses by unions

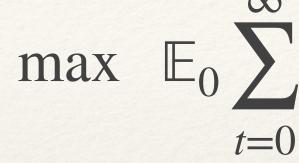








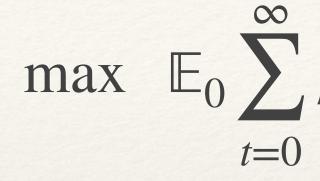
 $\max \mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \left(u(c_{it}) - v(N_t) \right)$ hours set by unions (later) $c_{it} + a_{it} \le (1 + r_{t-1})a_{it-1} + e_{it}(1 - \tau_t)w_t N_t = a_{it} \ge \underline{a}$



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idiosyncratic productivity shocks (Markov chain)

Two aggregate variables: $\{r_s, Z_s\}$

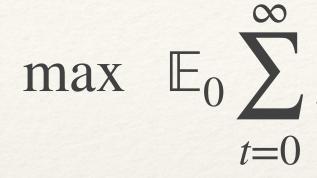


 $c_{it} + a_{it} \le (1 + r_{t-1})a_{it-1}$

Two aggregate variables: $\{r_s, Z_s\}$ **—** Backward (policy) iteration

$$\beta^{t} \left(u(c_{it}) - v(N_{t}) \right)$$

+ $e_{it} (1 - \tau_{t}) w_{t} N_{t}$ $a_{it} \ge \underline{a}$
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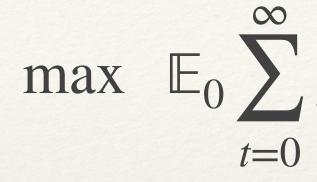
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Policy functions $c_{t}^{*}(e, a)$





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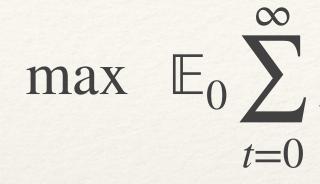
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Forward (distribution) iteration $\Psi_t(a, e)$





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idiosyncratic productivity shocks (Markov chain)

Two aggregate variables: $\{r_s, Z_s\}$ **—** Backward (policy) iteration

Aggregate consumption:



$$\beta^{t} \left(u(c_{it}) - v(N_{t}) \right)$$

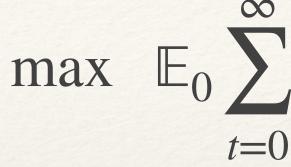
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Policy functions $c_{\star}^{*}(e, a)$

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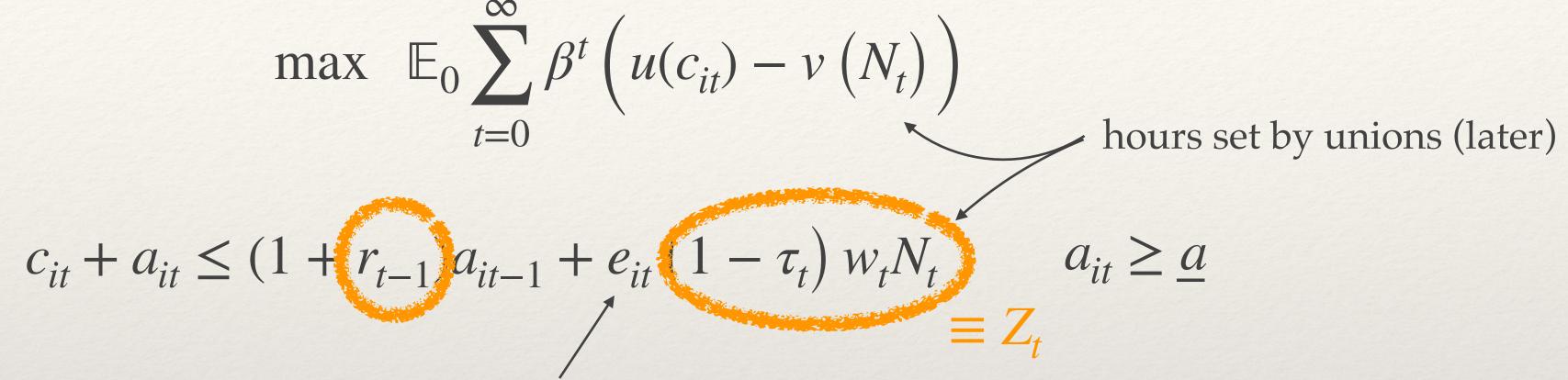




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 $\mathscr{C}_t(\{r_s, Z_s\})$



idiosyncratic productivity shocks (Markov chain)



 $\mathscr{C}_t(\{r_s, Z_s\})$ Aggregate consumption function in the sequence space

* Government sets $\{G_s, T_s\}$ subject to

$$B_t = (1 + r_{t-1}) B_{t-1} + G_t -$$

* Central bank sets nominal rate

$$i_t = r_t + \phi \pi_{t+1}$$

(2, 3) Fiscal and monetary policy

 $-T_t$ $T_t = \tau_t w_t N_t$ B_t bounded

today: $\phi \searrow 1$ i.e. real rate = r_t

- * Linear production $Y_t = N_t$ with flexible prices, so that real wage $w_t = 1$
- * Sticky nominal wages, set by unions

$$\pi_{t} = \kappa \int \left(v'(n_{it}) - \frac{\epsilon}{\epsilon - 1} \left(1 - \tau_{t} \right) w_{t} e_{it} u'(c_{it}) \right) di + \beta \pi_{t+1}$$

* useful starting point: labor rationed equally $n_{it} = N_t$

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average gap in households' FOC for labor



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Better than sticky prices + flexible wages (\rightarrow countercyclical profits...)



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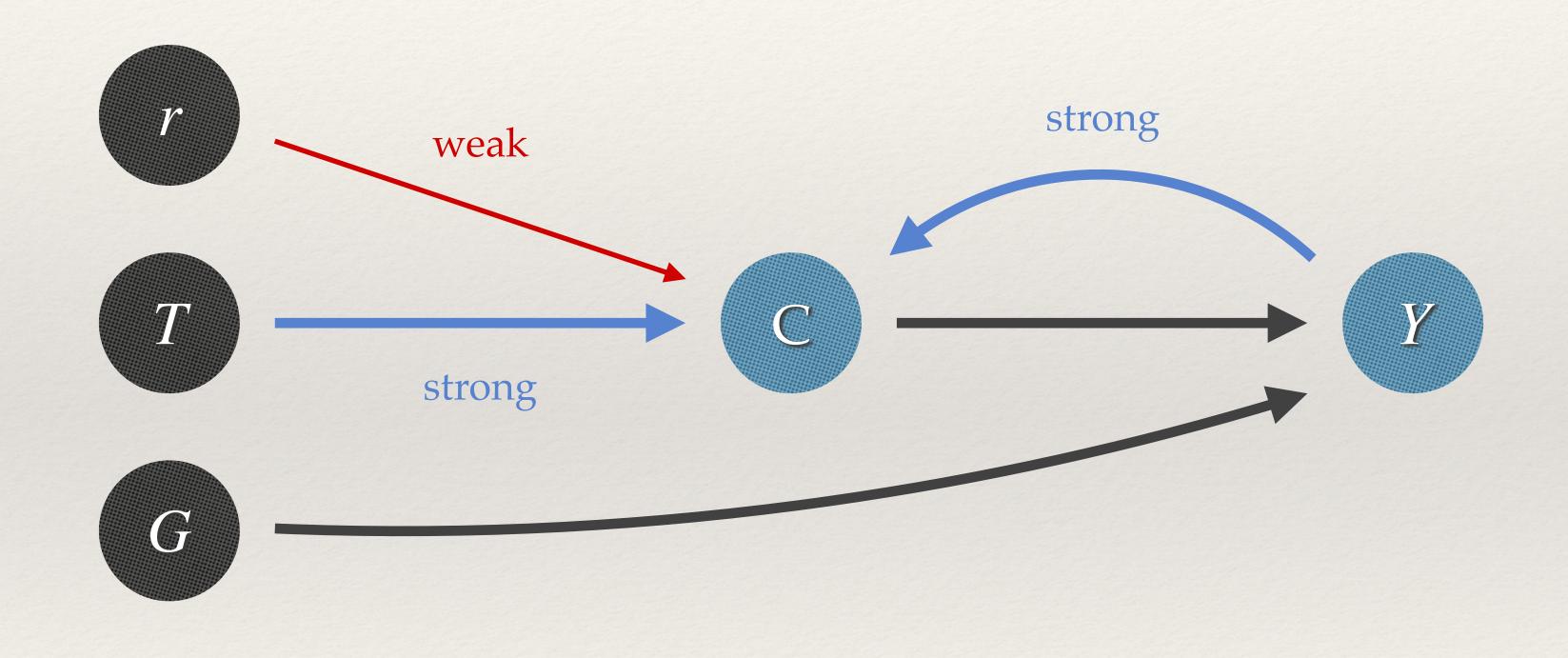
- * useful starting point: labor rationed equally $n_{it} = N_t$
- *
- * That's it!

average gap in households' FOC for labor

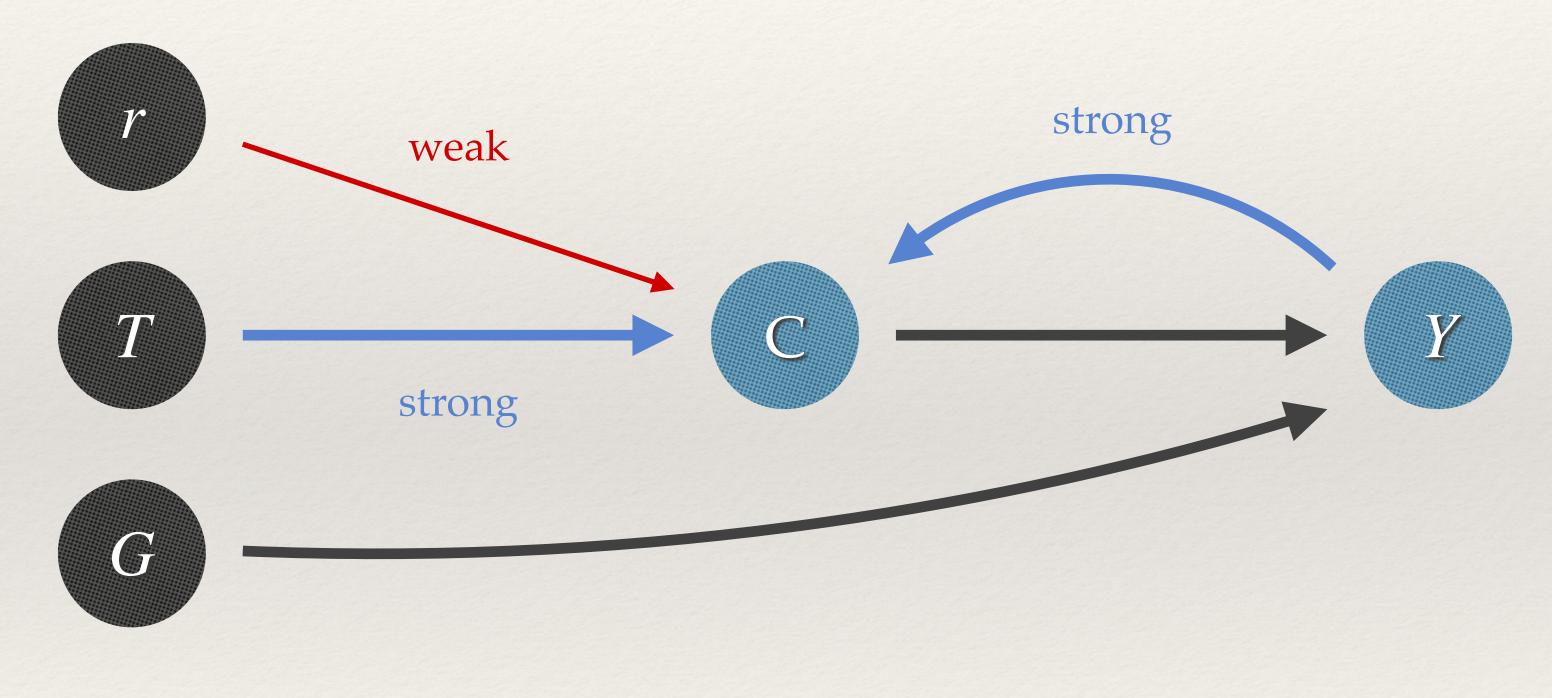
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Equilibrium as a graph

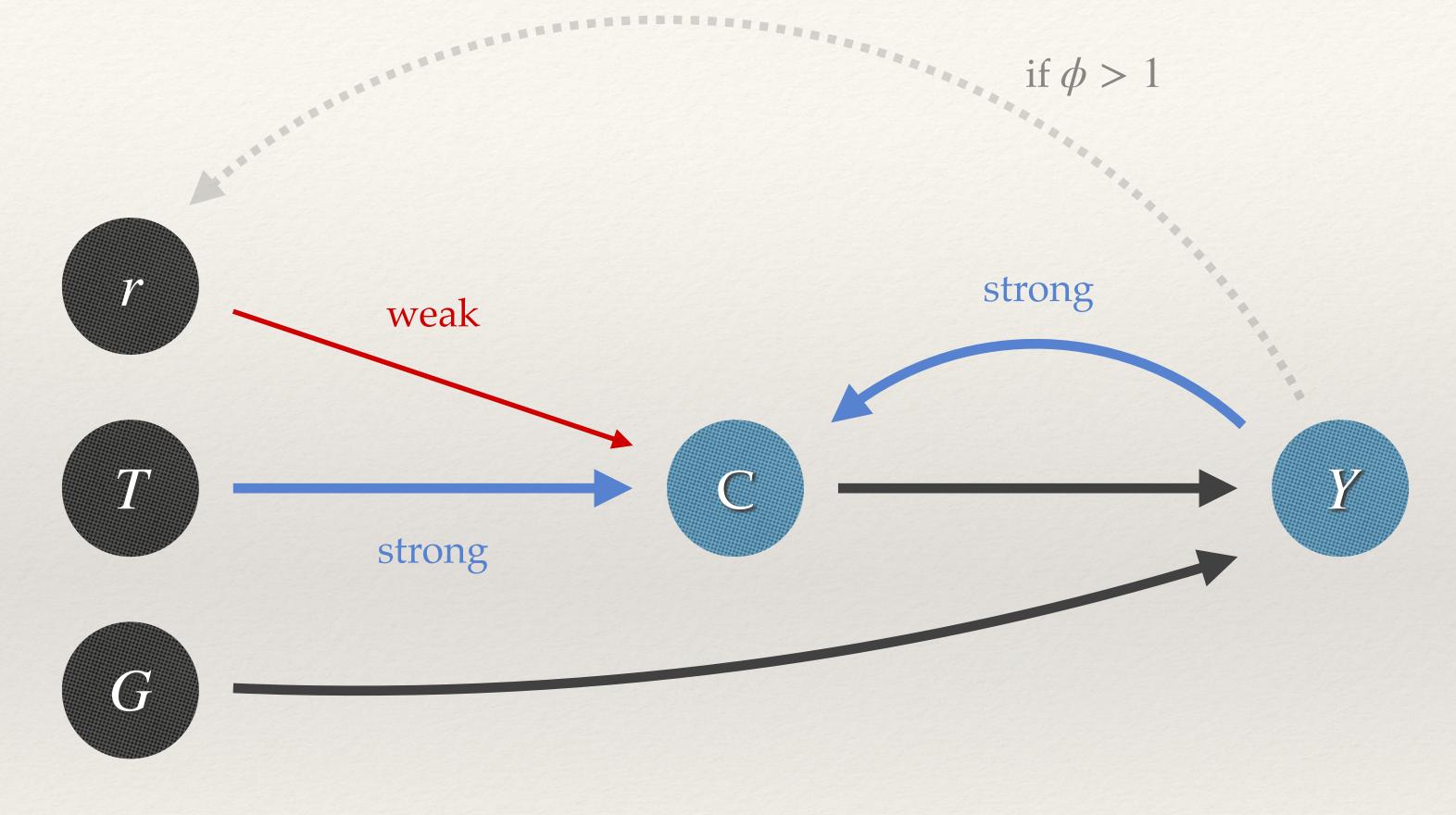


Equilibrium as a graph



 $Y_t = G_t + \mathscr{C}_t \left(\left\{ r_s, Y_s - T_s \right\} \right)$

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Fiscal policy in HANK

- * Imagine central bank keeps real interest rate constant: $r_t = r$.
- * Fiscal policy shock $d\mathbf{G} = (dG_0, dG_1, \ldots), d\mathbf{T} = (dT_0, dT_1, \ldots)$, same NPV.
- * What happens to **output**, $d\mathbf{Y} = ?$



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 - $Y_t = G_t +$

$$\mathscr{C}_t\left(\left\{\frac{Y_s-T_s}{s}\right\}\right)$$

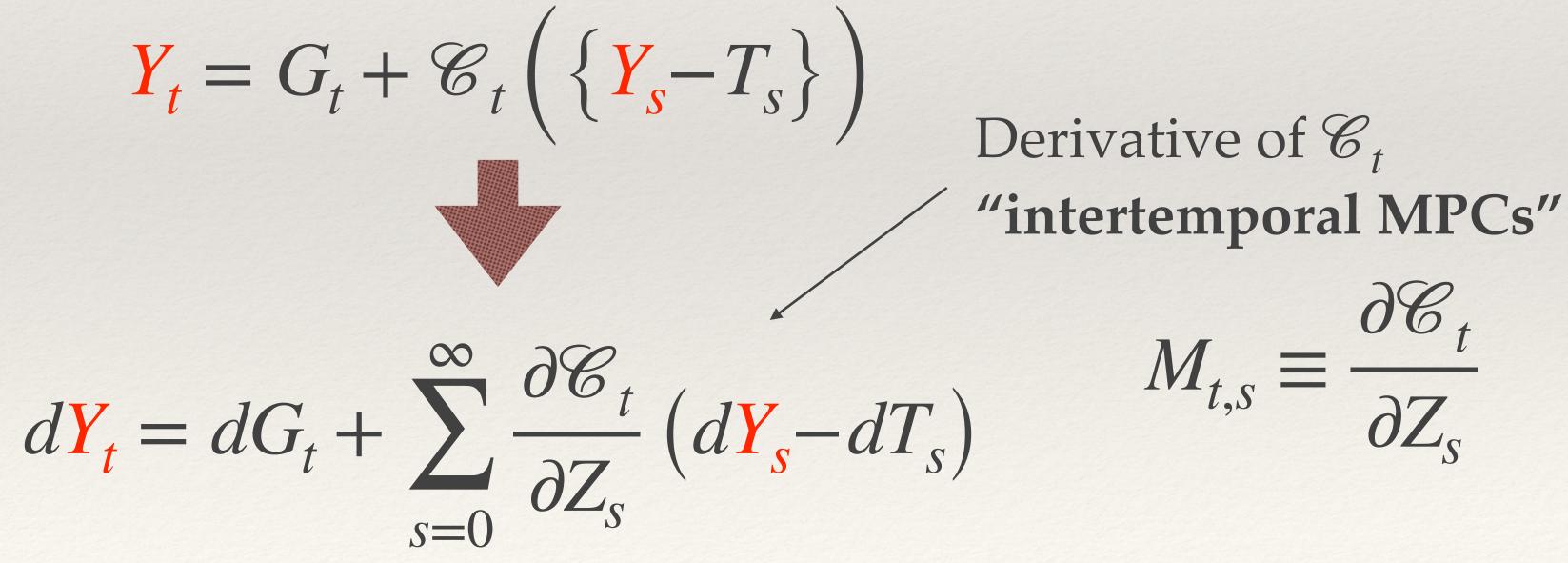


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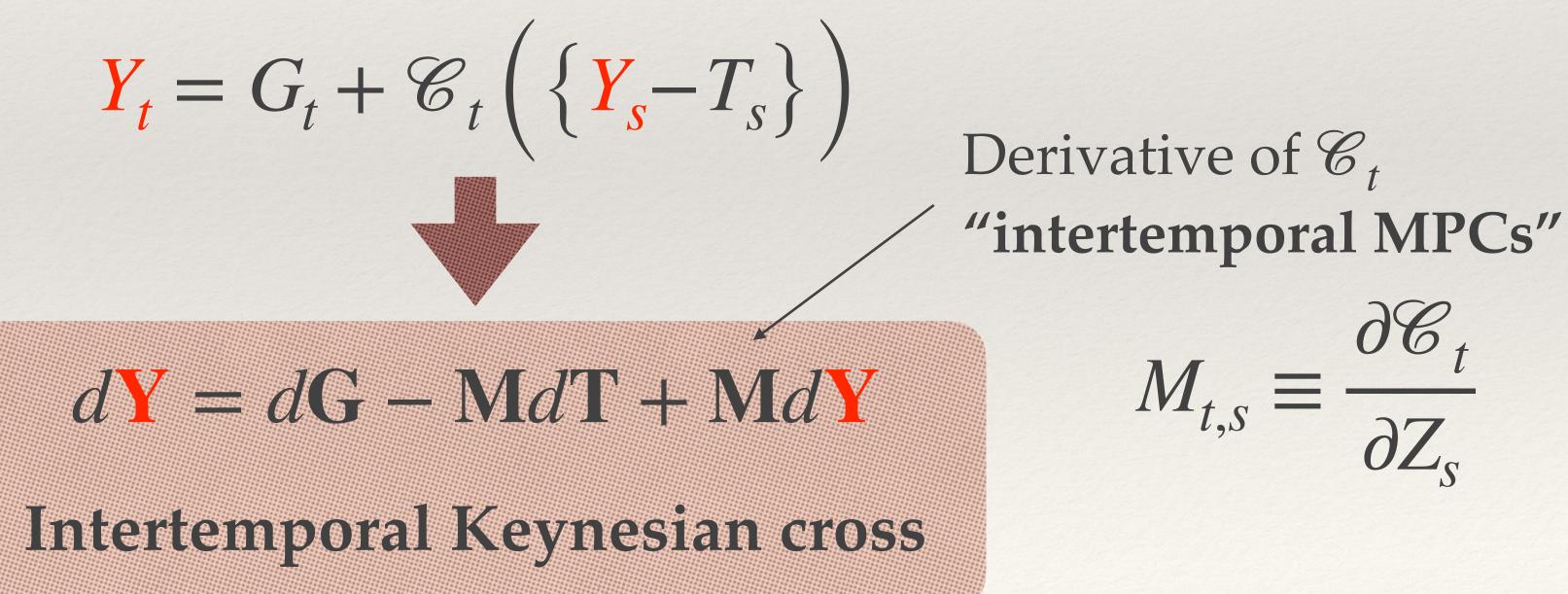
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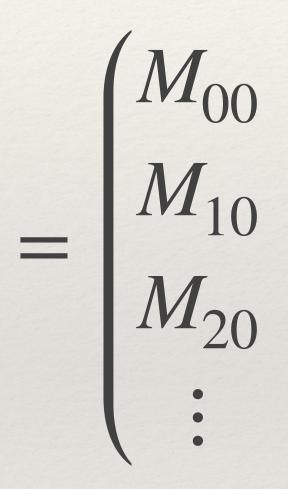
Intertemporal Keynesian cross

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What is V?

 $\mathbf{M} = \begin{pmatrix} M_{00} & M_{01} & M_{02} & \cdots \\ M_{10} & M_{11} & M_{12} & \cdots \\ M_{20} & M_{21} & M_{22} & \cdots \\ \vdots & \vdots & \vdots & \ddots \end{pmatrix}$





Impulse response of **C** to date 0 (unanticipated) increase in income Z

What is V?

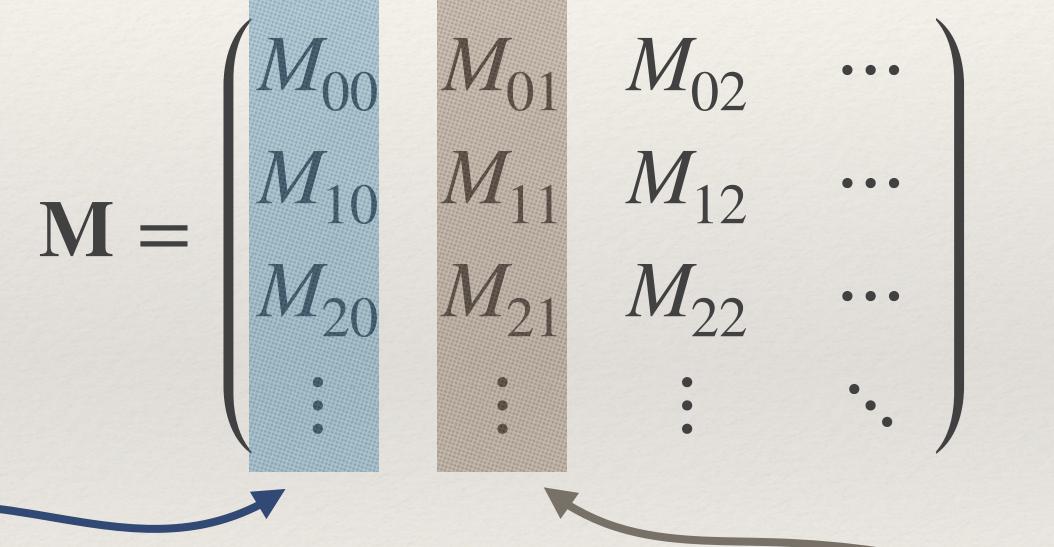
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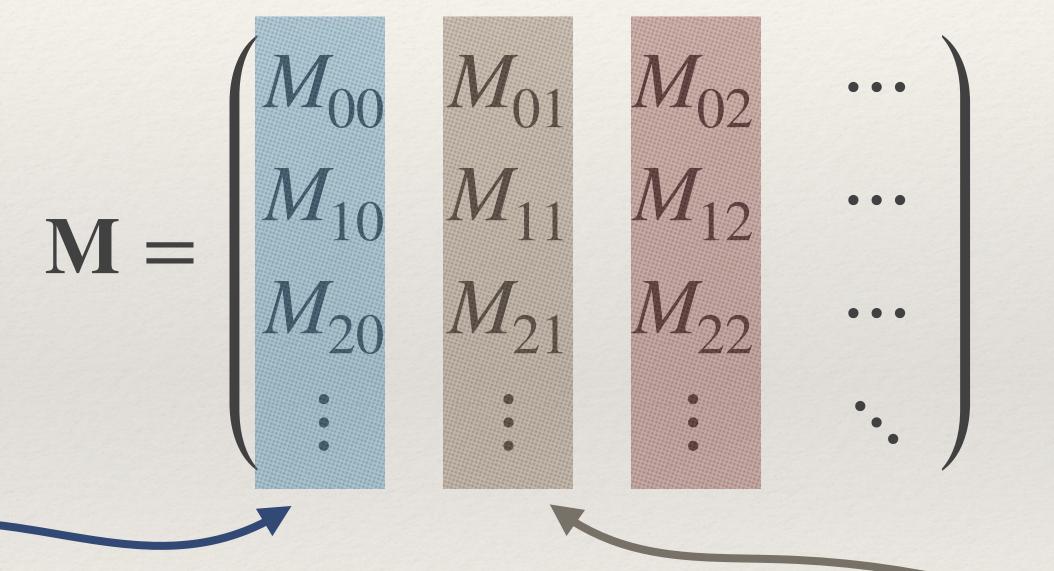
Impulse response of C to date 1 (anticipated) increase in income Z





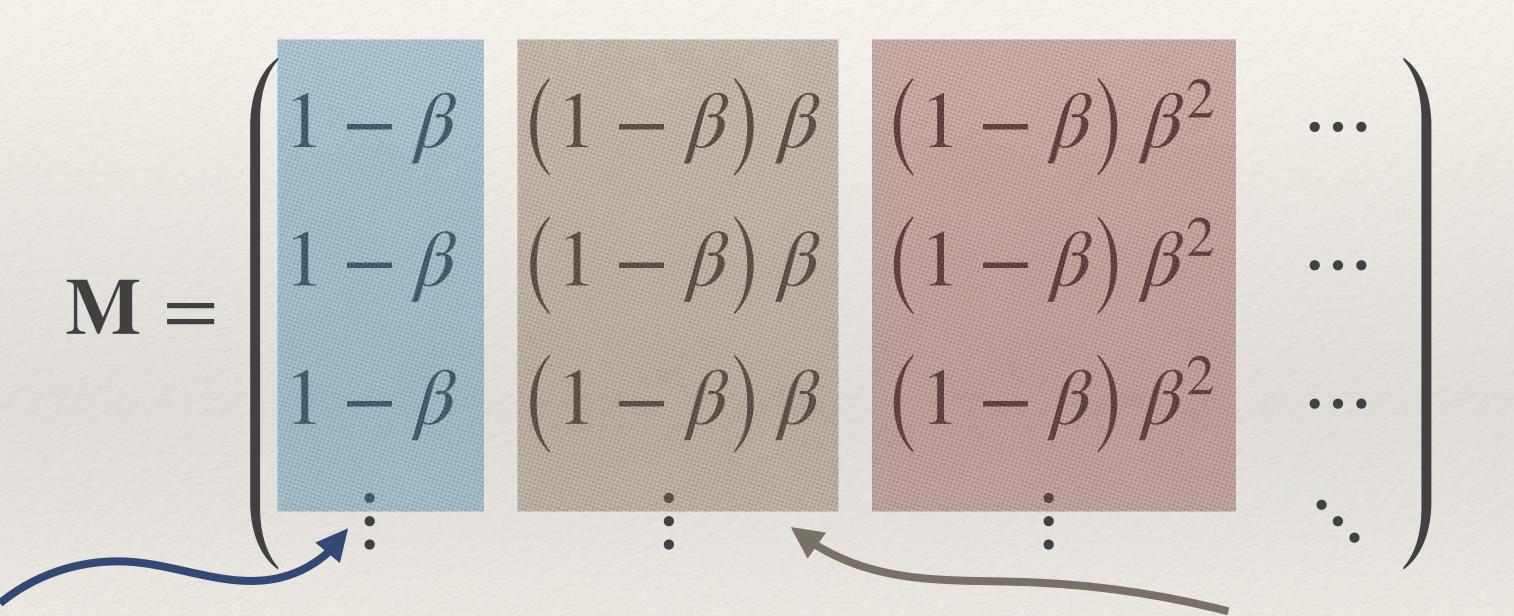
Impulse response of **C** to date 0 (unanticipated) increase in income Z

What is M?



Impulse response of C to date 1 (anticipated) increase in income Z

What is M for a representative agent? * **M** is the matrix derivative (Jacobian) of the cons. function $\mathscr{C}_t \left(\left\{ \frac{Y_s - T_s}{S} \right\} \right)$

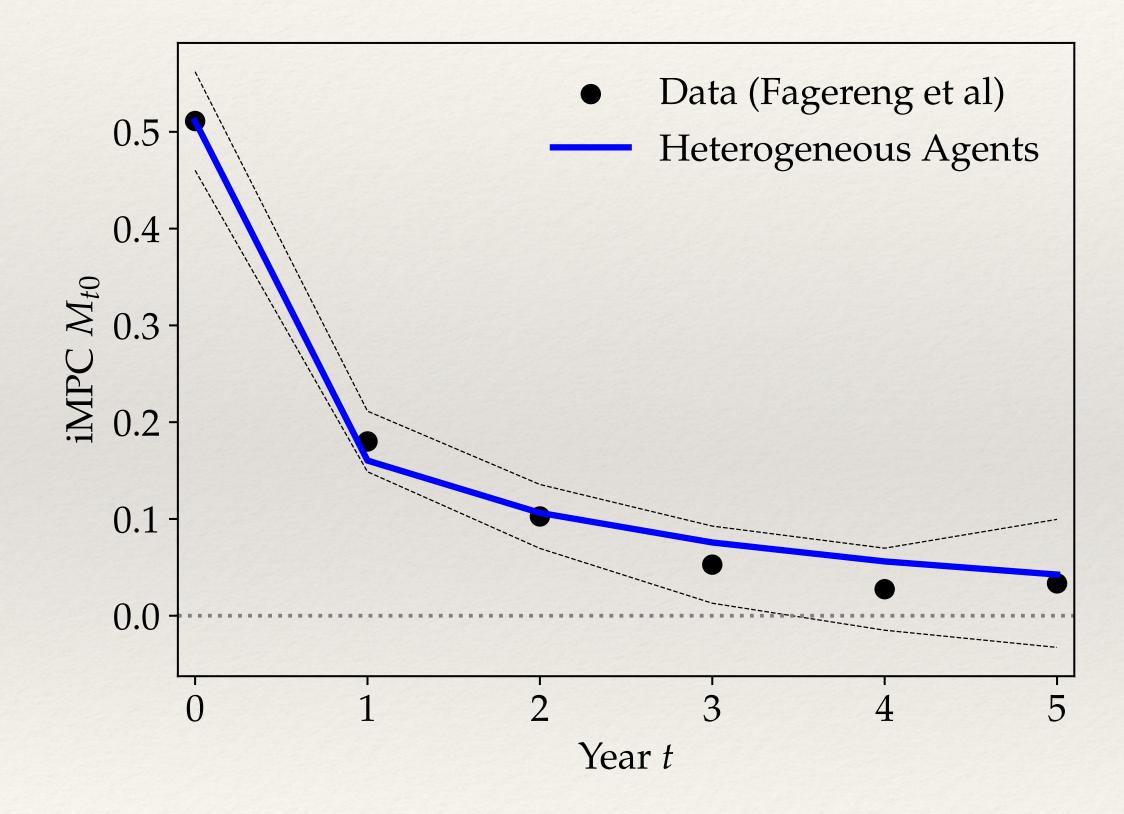


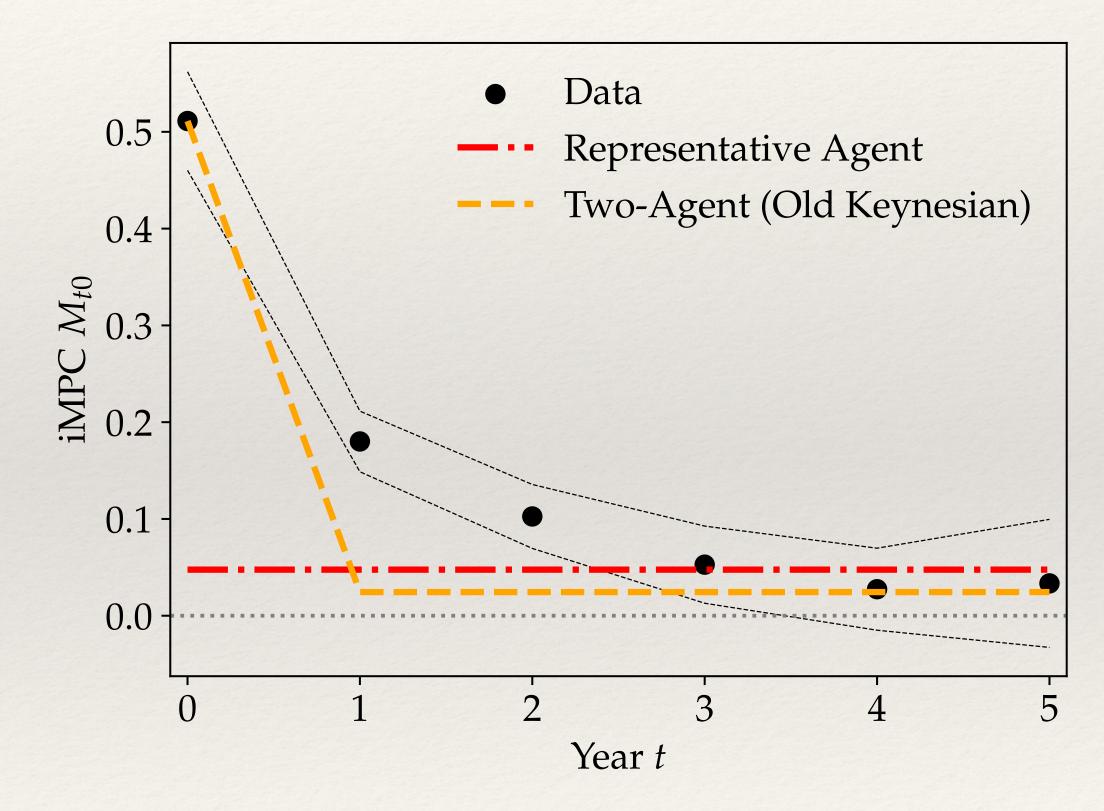
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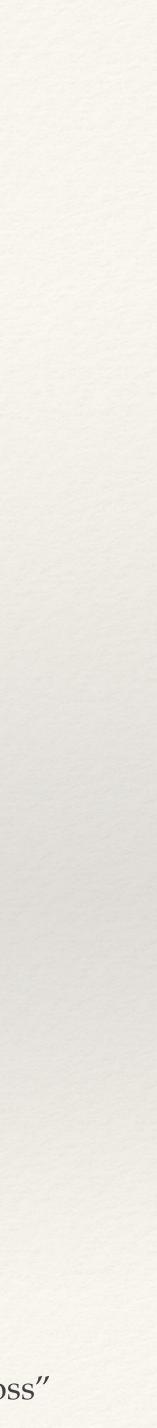
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Min models and the data

* Can compare first column with the data from Fagereng-Holm-Natvik:

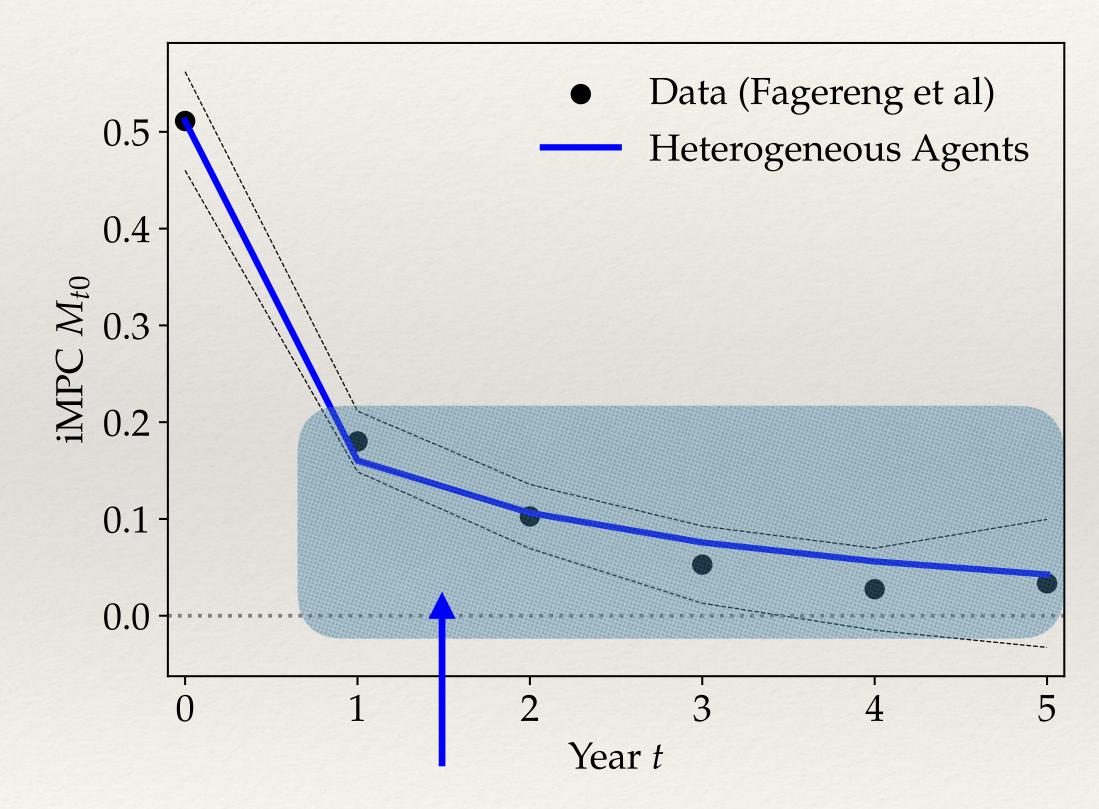




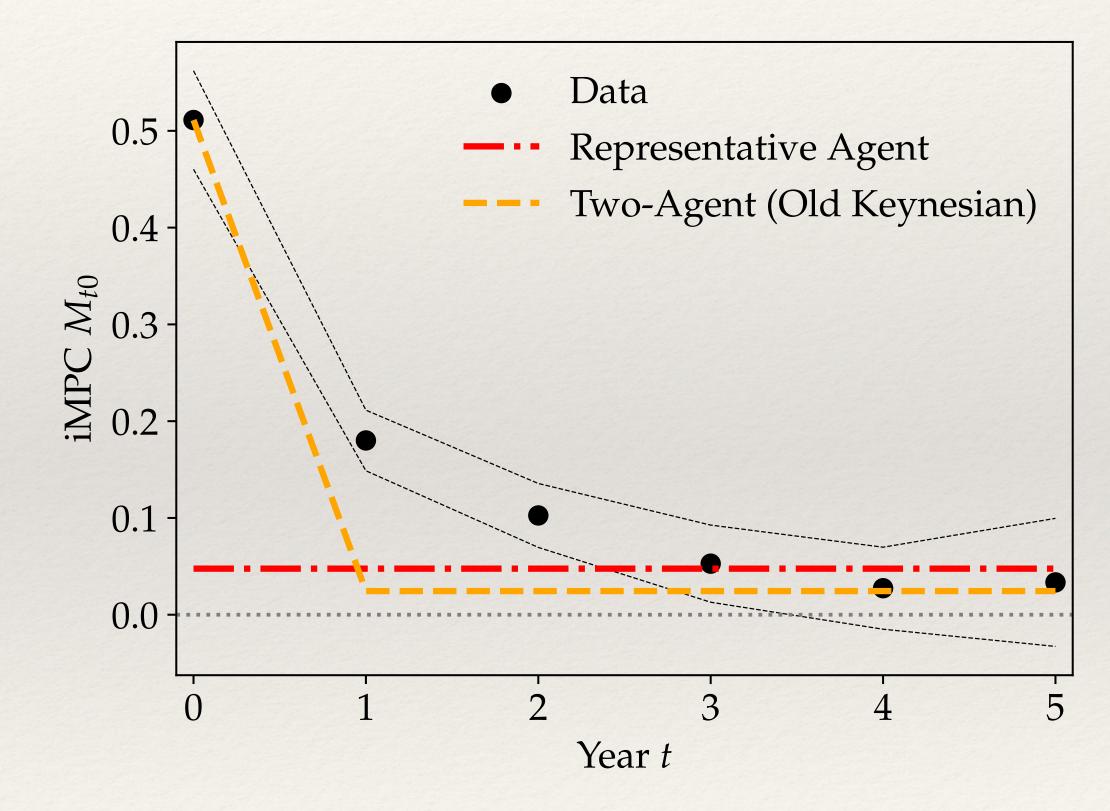


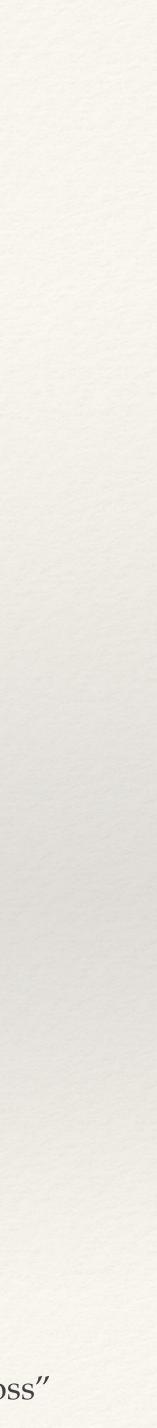
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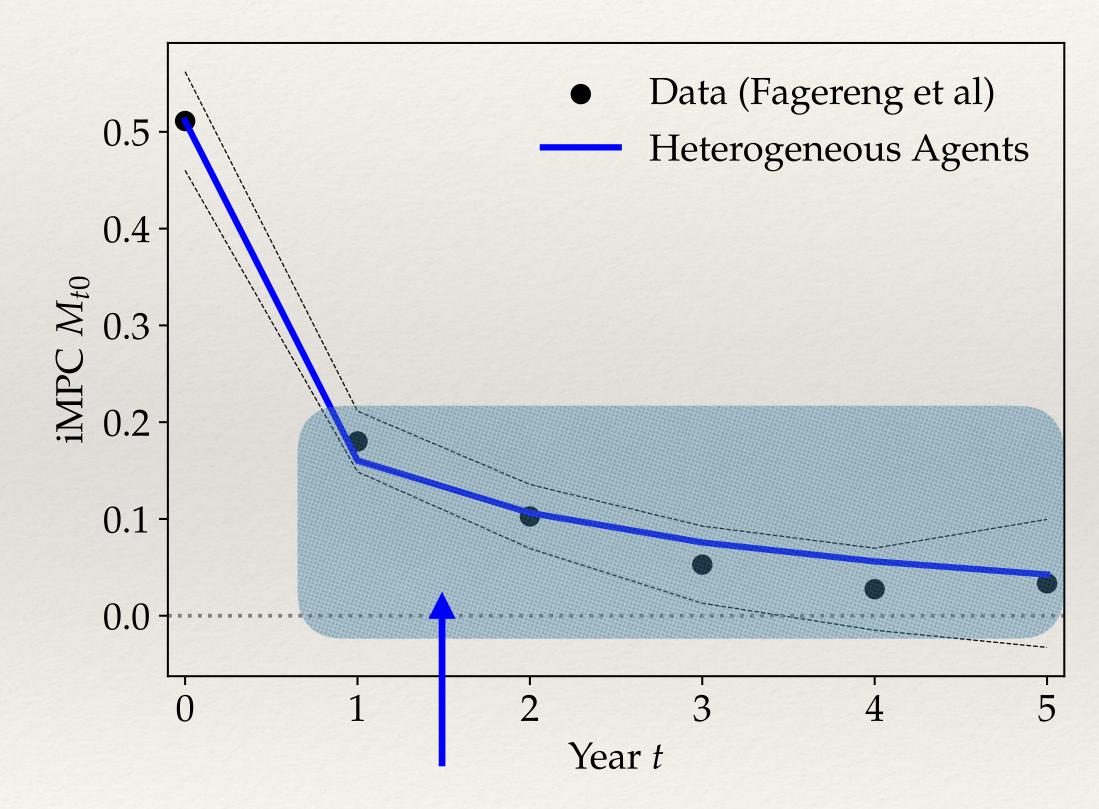
HA: Households spend down transfer relatively slowly



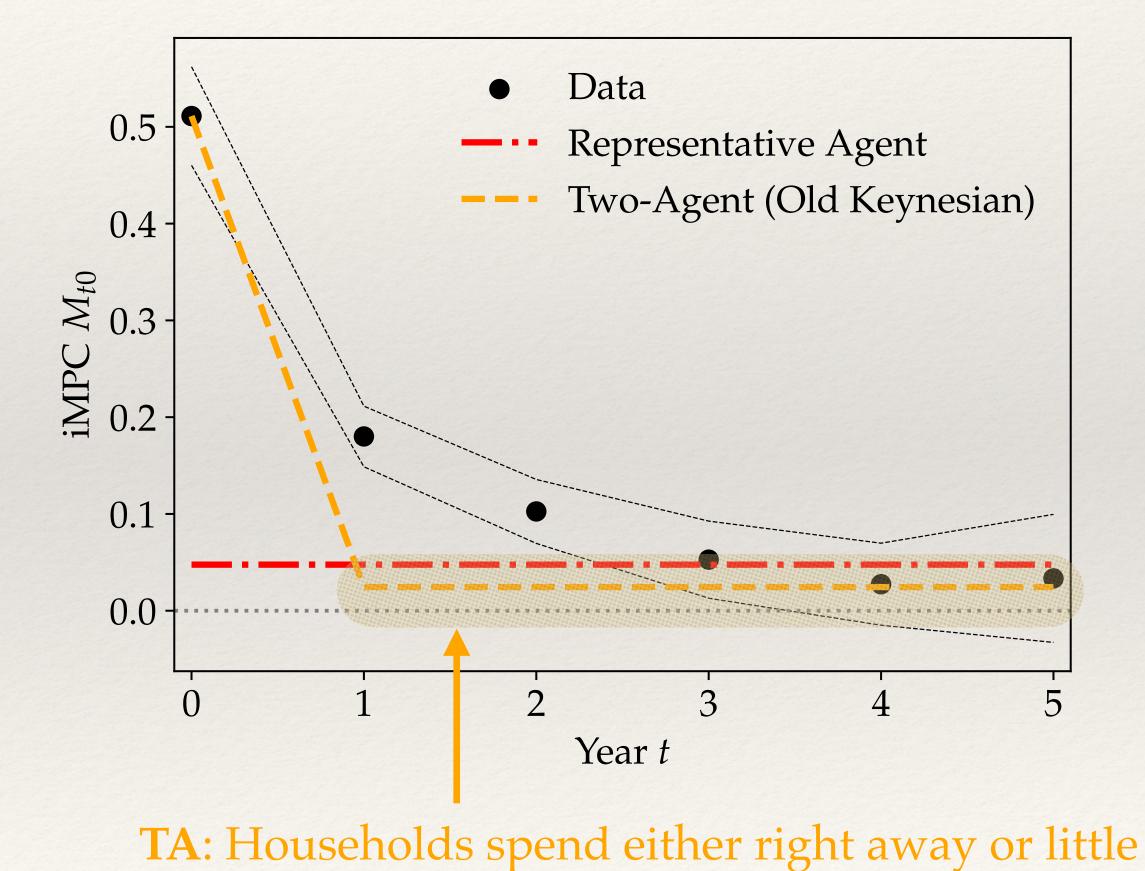


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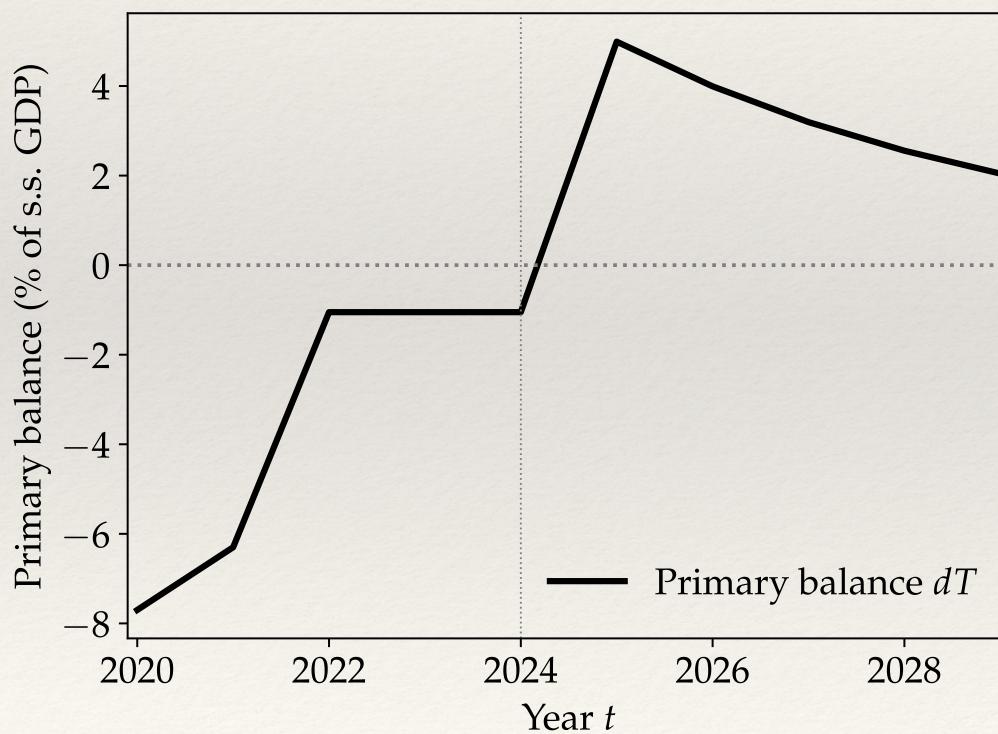
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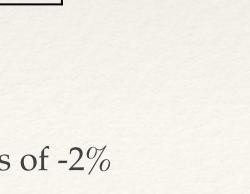
The long shadow of Covid stimulus

* Feed in Covid stimulus and solve for consumption and inflation.



Tax change

Constructed as 70% of observed primary balance beyond pre-Covid surplus of -2%

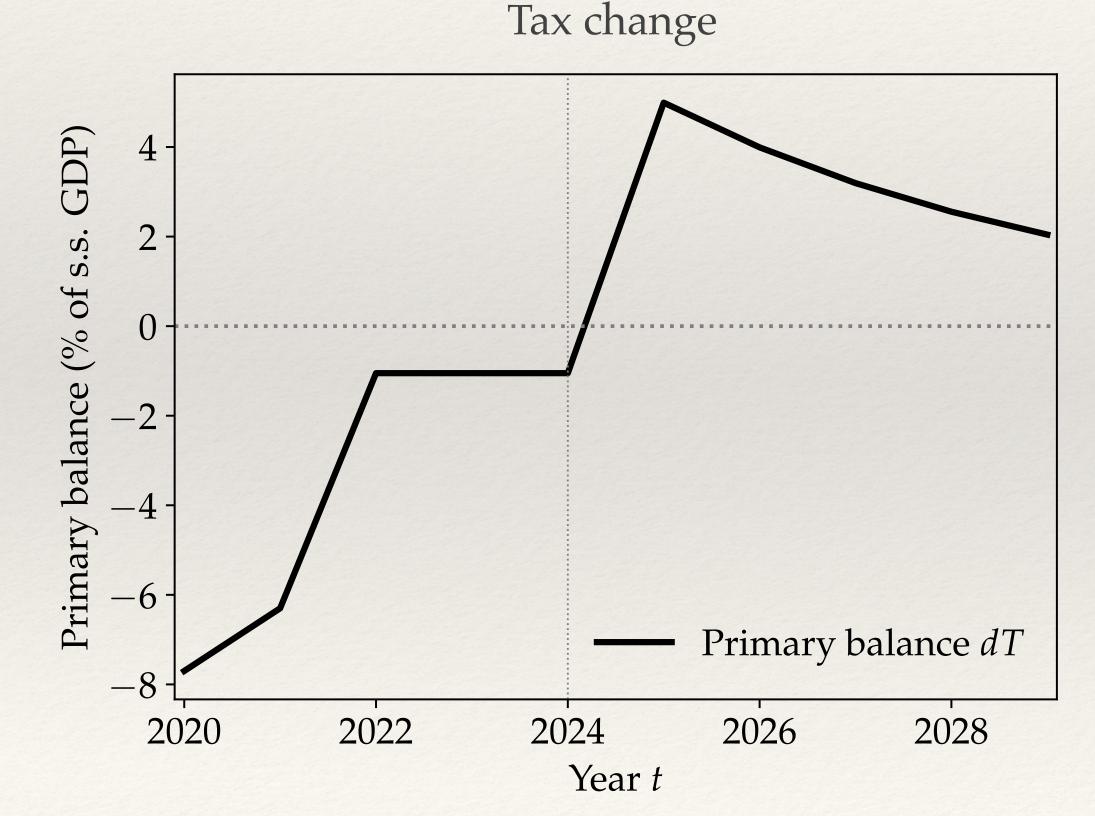


See also Bayer Born Luetticke Müller

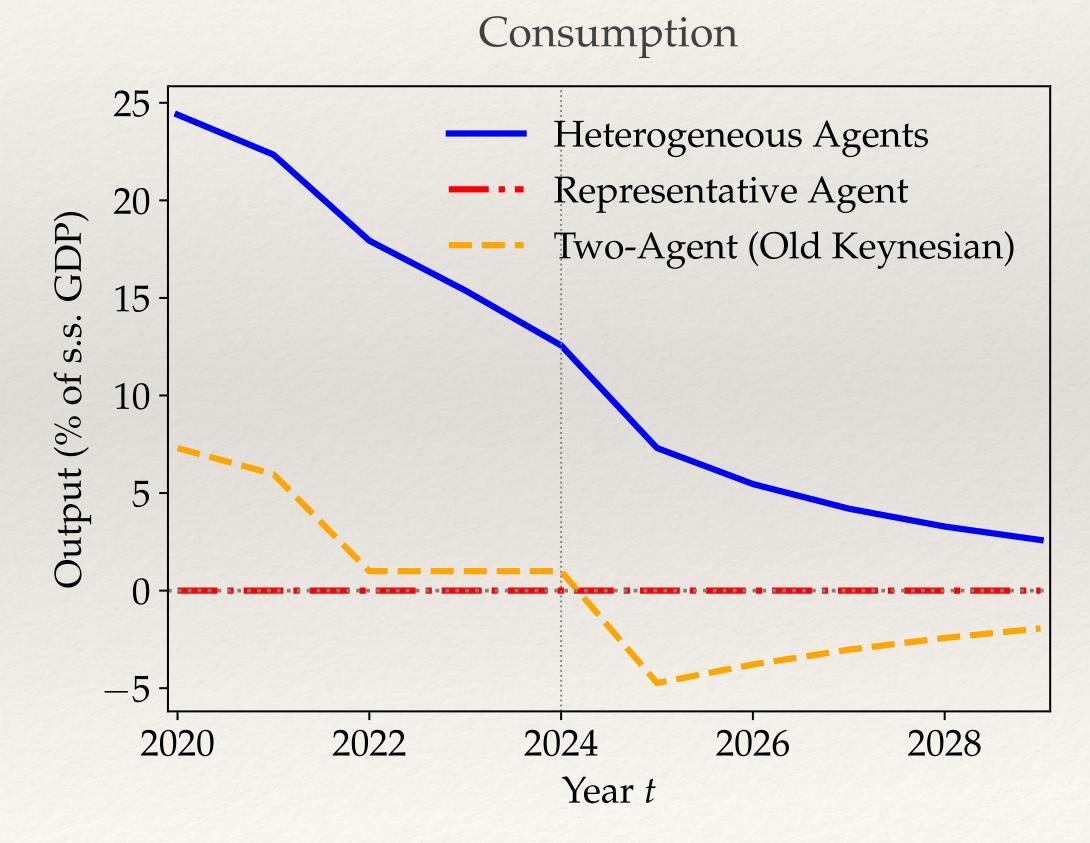


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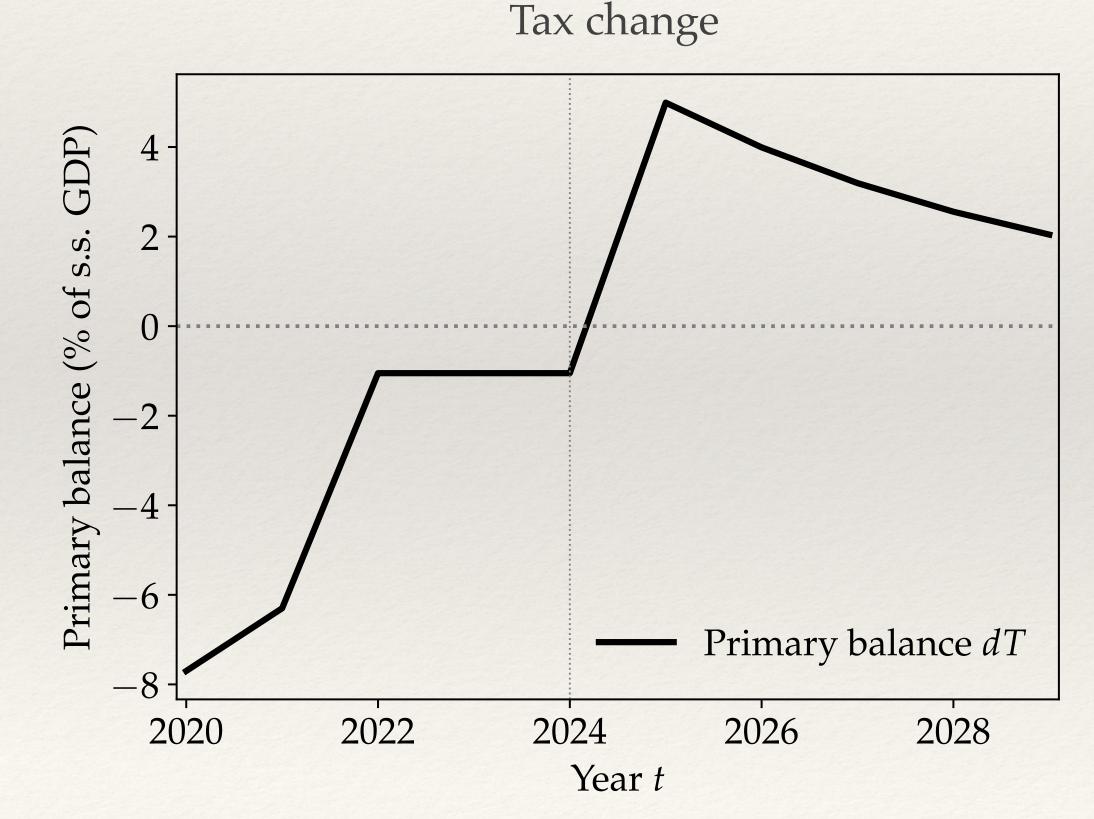


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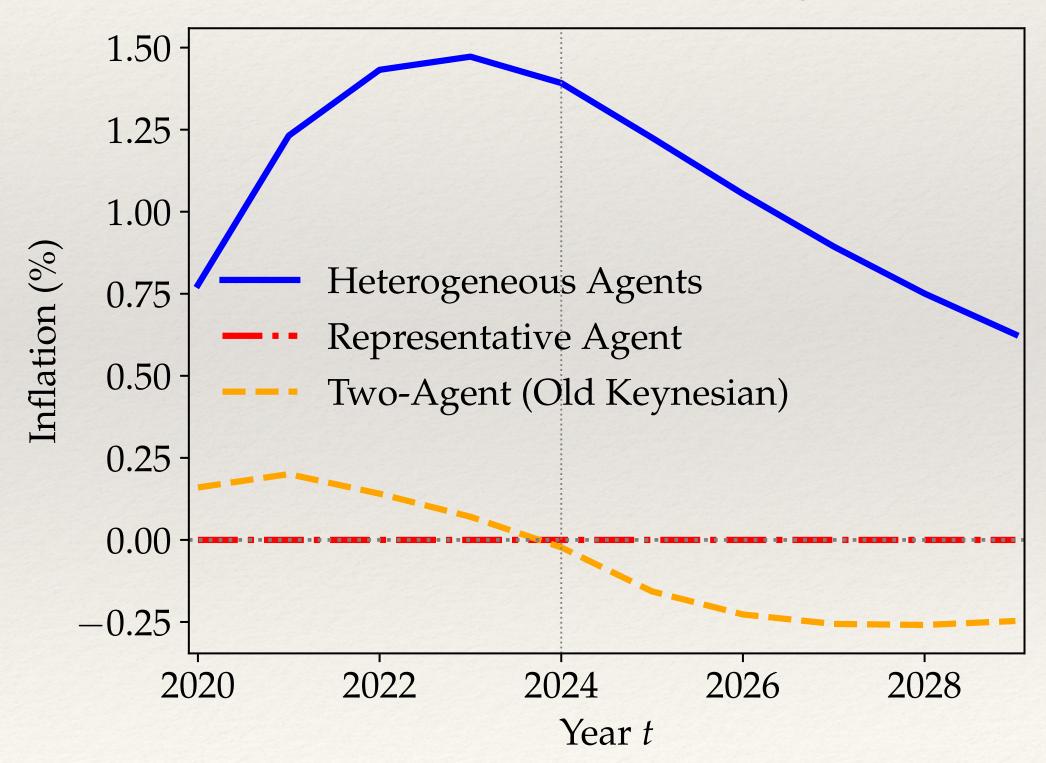
The long shadow of Covid stimulus

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Inflation (relative to target)

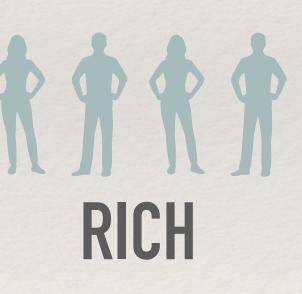


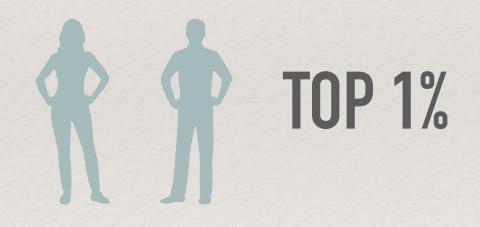
Standard hybrid NKPC with 50% weight on lagged inflation, $\kappa = 0.01$



POOR AND MIDDLE CLASS

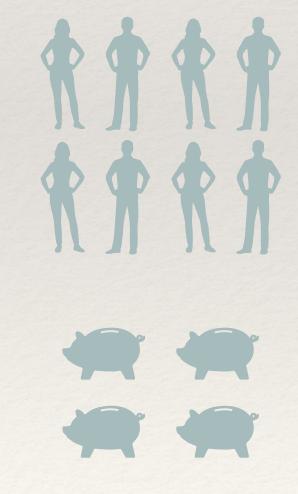
AGGREGATE DEMAND



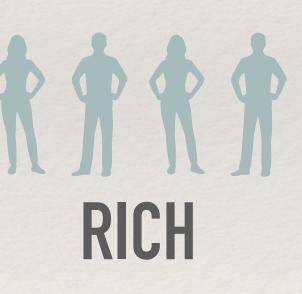


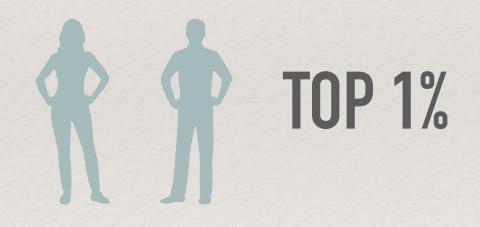


POOR AND MIDDLE CLASS



AGGREGATE DEMAND





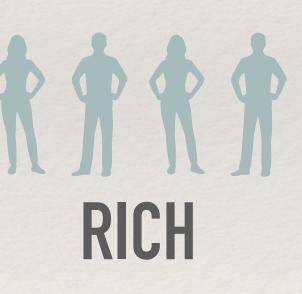


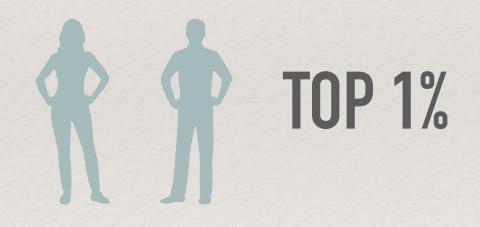
Poor & middle class spend down the fastest



POOR AND MIDDLE CLASS

AGGREGATE DEMAND



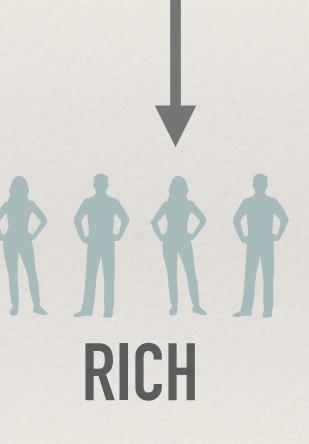


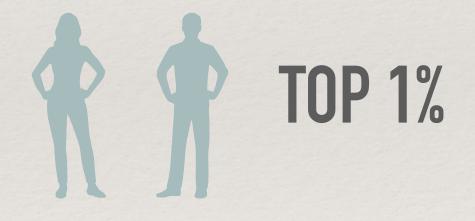


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POOR AND MIDDLE CLASS

AGGREGATE DEMAND



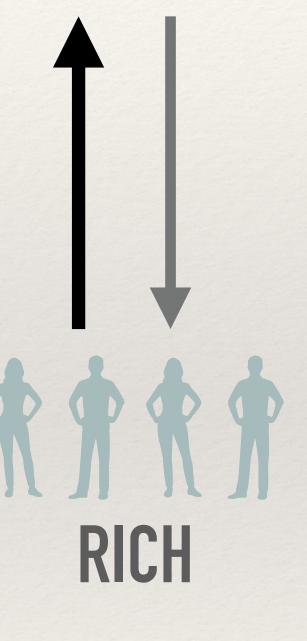


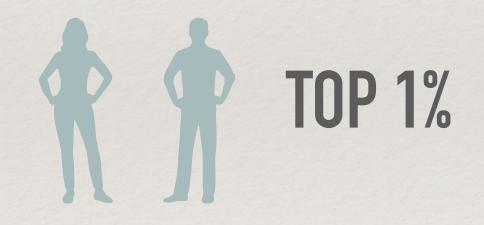


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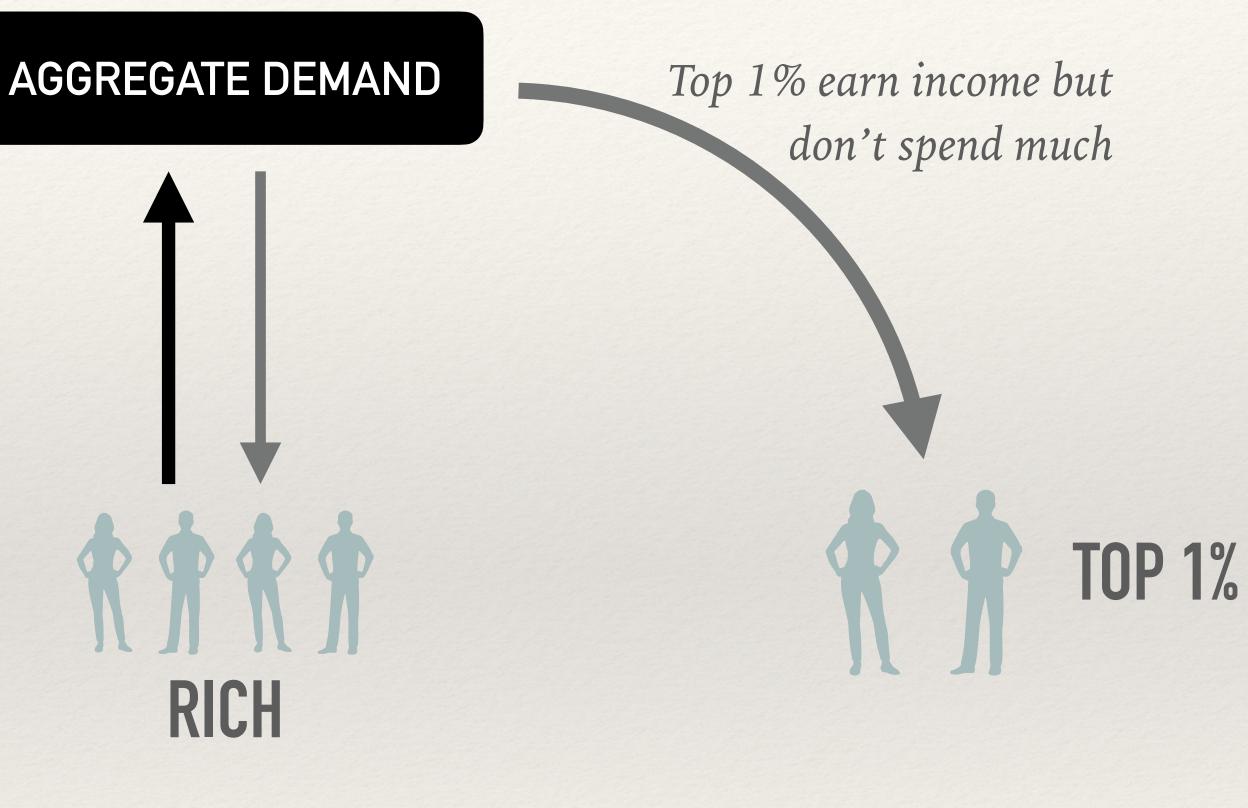






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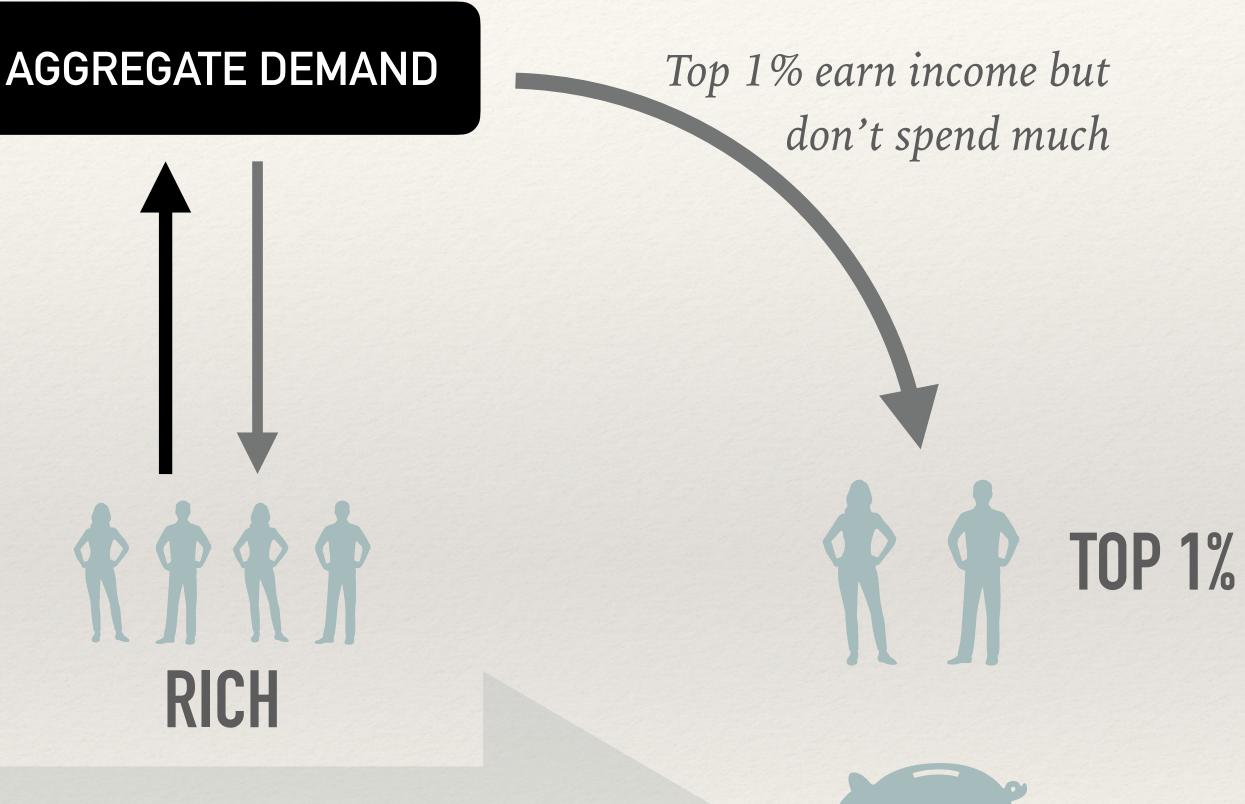




Poor & middle class spend down the fastest

POOR AND MIDDLE CLASS

Excess savings slowly "trickle up" towards the top 1%









- * Allow for central bank to shock the real interest rate $\{r_{s}\}$
- * Assume gov. keeps debt repayment $(1 + r_{t-1})B_t$ constant and adjusts T_t $\mathbf{Y}_{t} = G_{t} + \mathscr{C}_{t} \left(\left\{ r_{s}, \mathbf{Y}_{s} - T_{s} \right\} \right) \qquad T_{t} = (1+r)B + G - \frac{(1+r)B}{1+r_{t}}$

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 $d\mathbf{Y} = \mathbf{M}^r \frac{d\mathbf{r}}{1+r} - \mathbf{M}B \frac{d\mathbf{r}}{1+r} + \mathbf{M}d\mathbf{Y}$

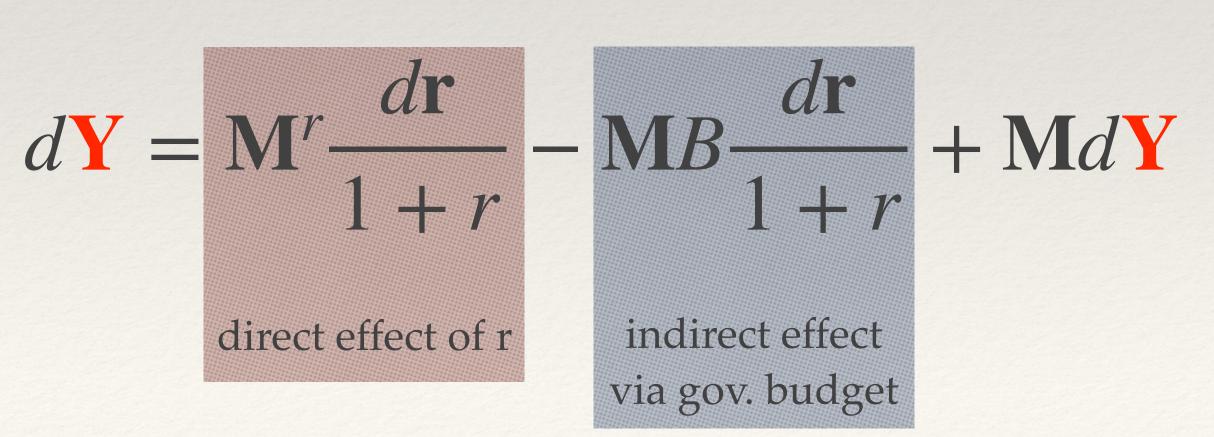
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direct effect of r

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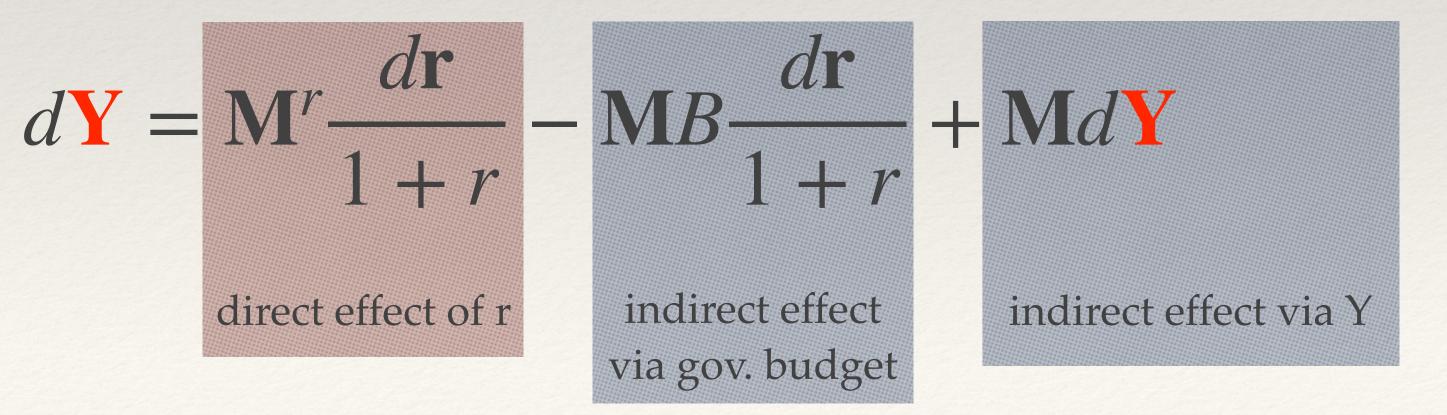
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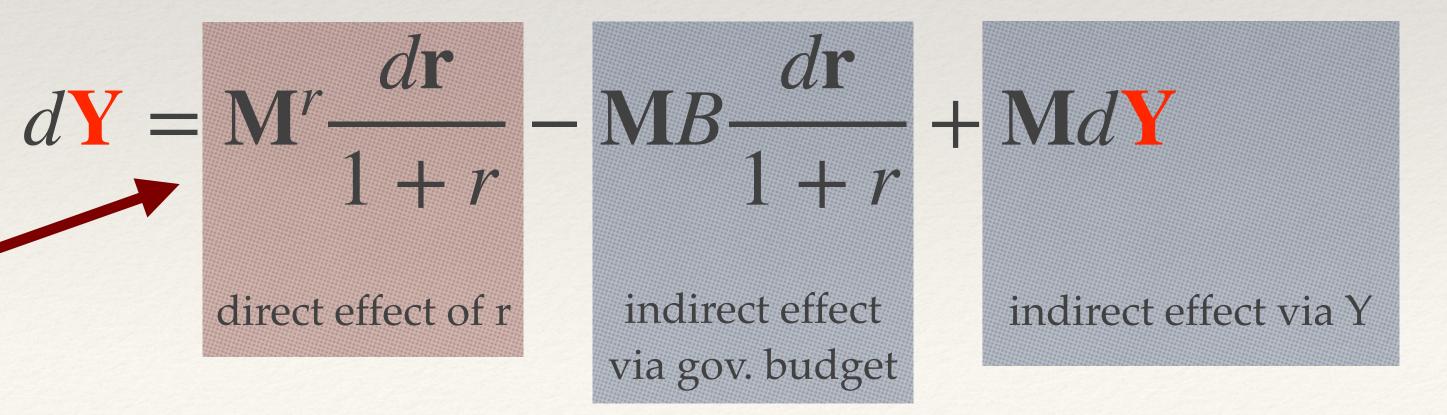
direct effect of r



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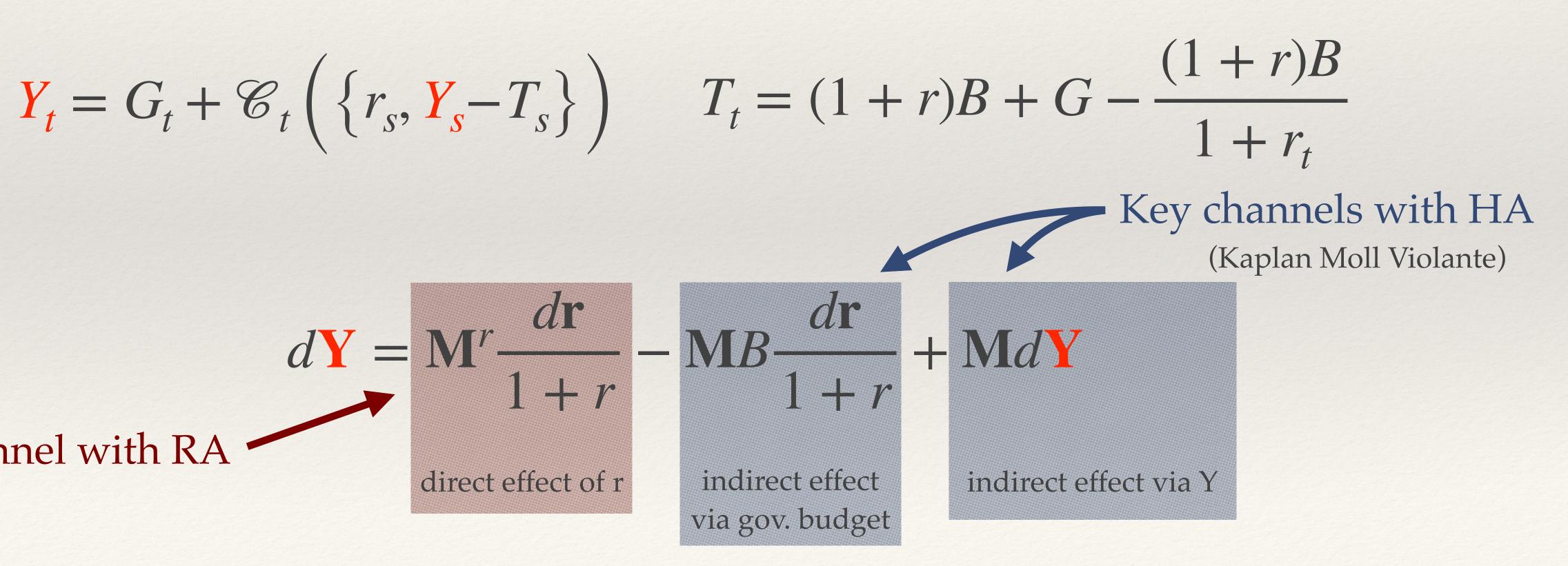
direct effect of r

Key channel with RA



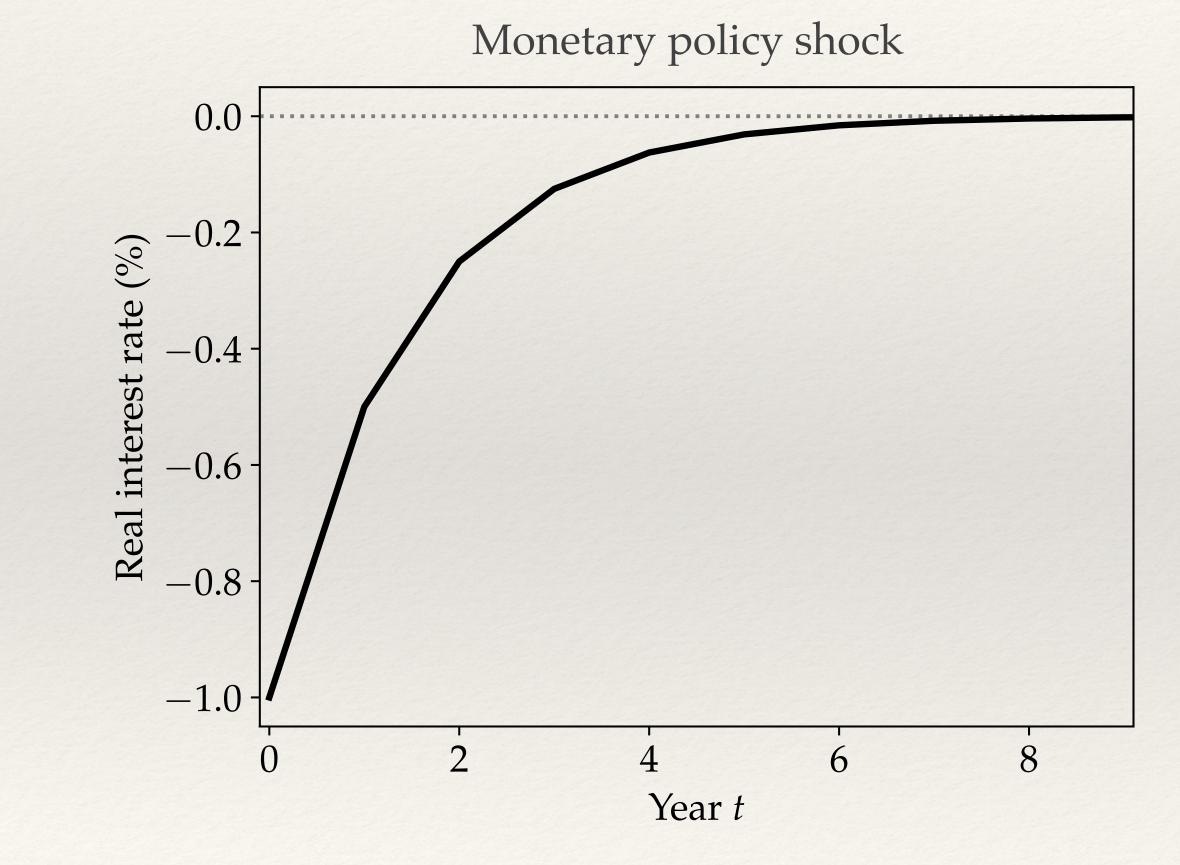
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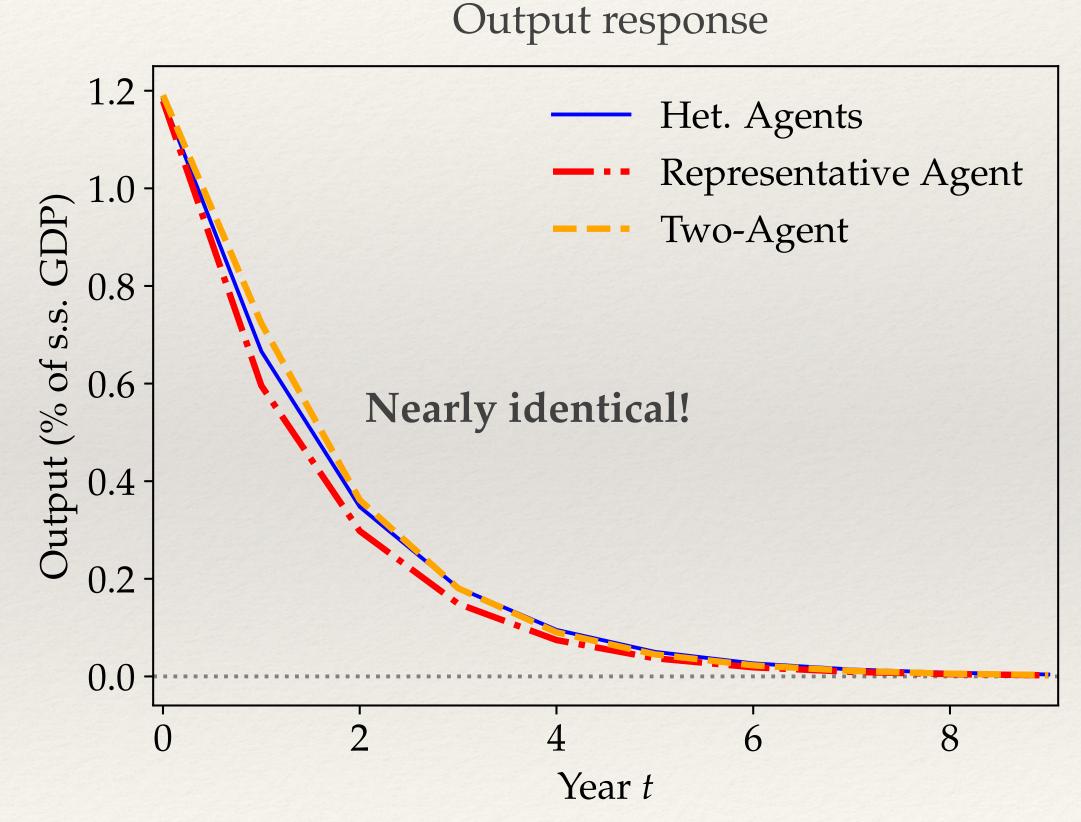
Key channel with RA



Aggregate effects of monetary policy * Does HANK matter for aggregate effects of monetary policy?

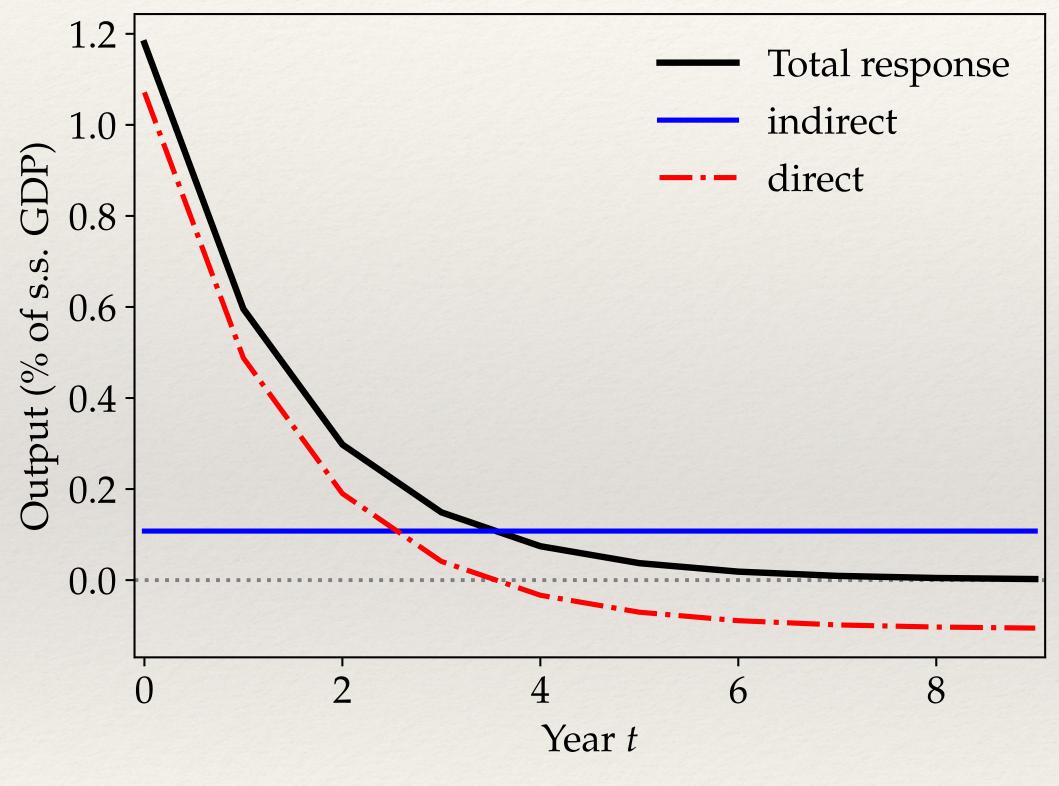
Aggregate effects of monetary policy * Does HANK matter for aggregate effects of monetary policy?





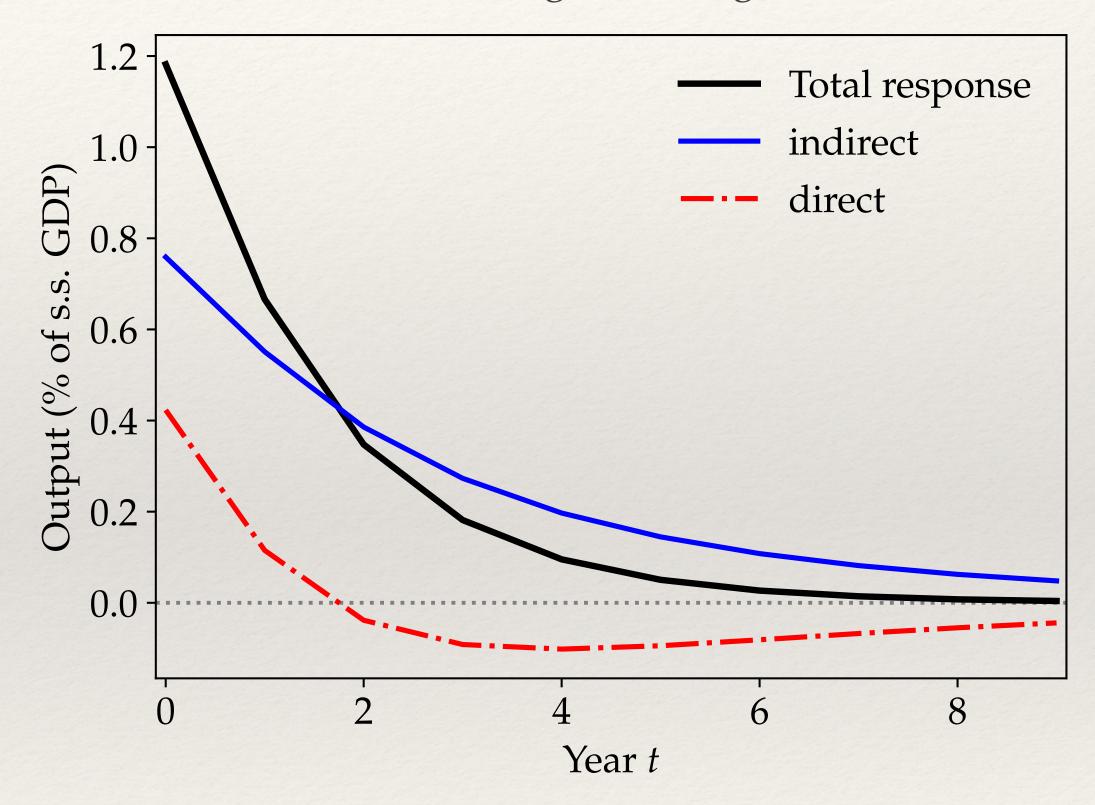
Direct and indirect effects

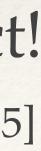
Representative agent



* HANK similar to RANK because stronger indirect offsets weaker direct effect! [Werning 2015]

Heterogeneous agents

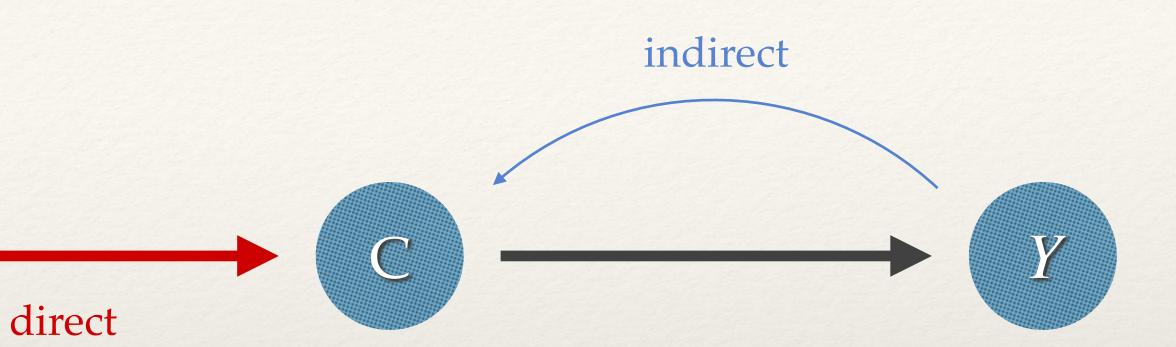


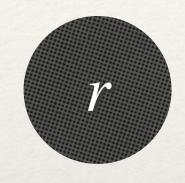






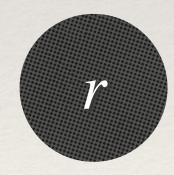




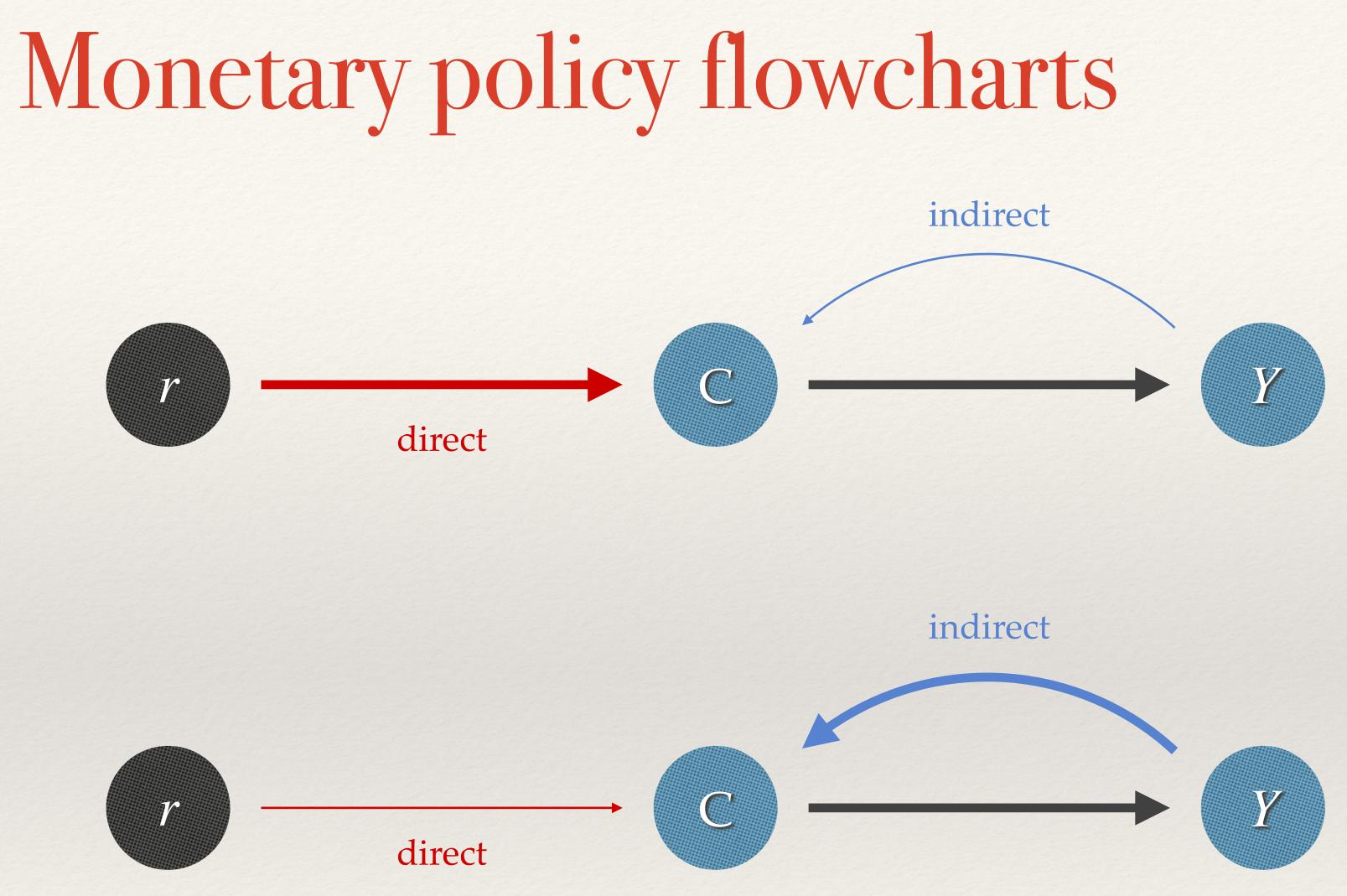


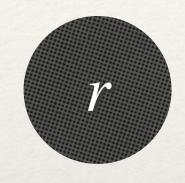






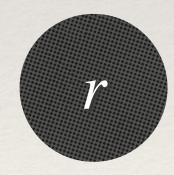
direct





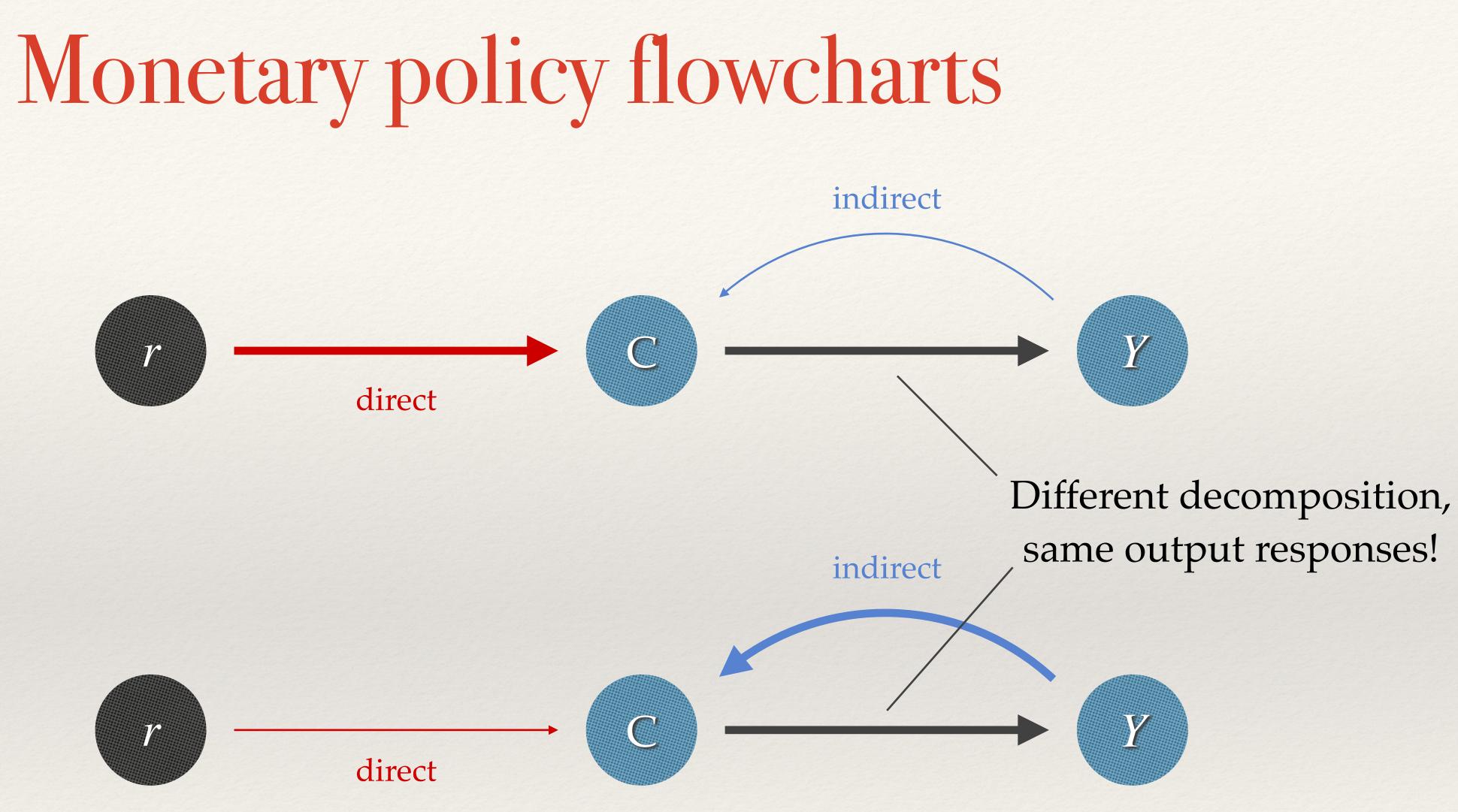


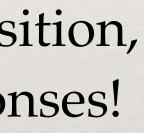




direct

direct



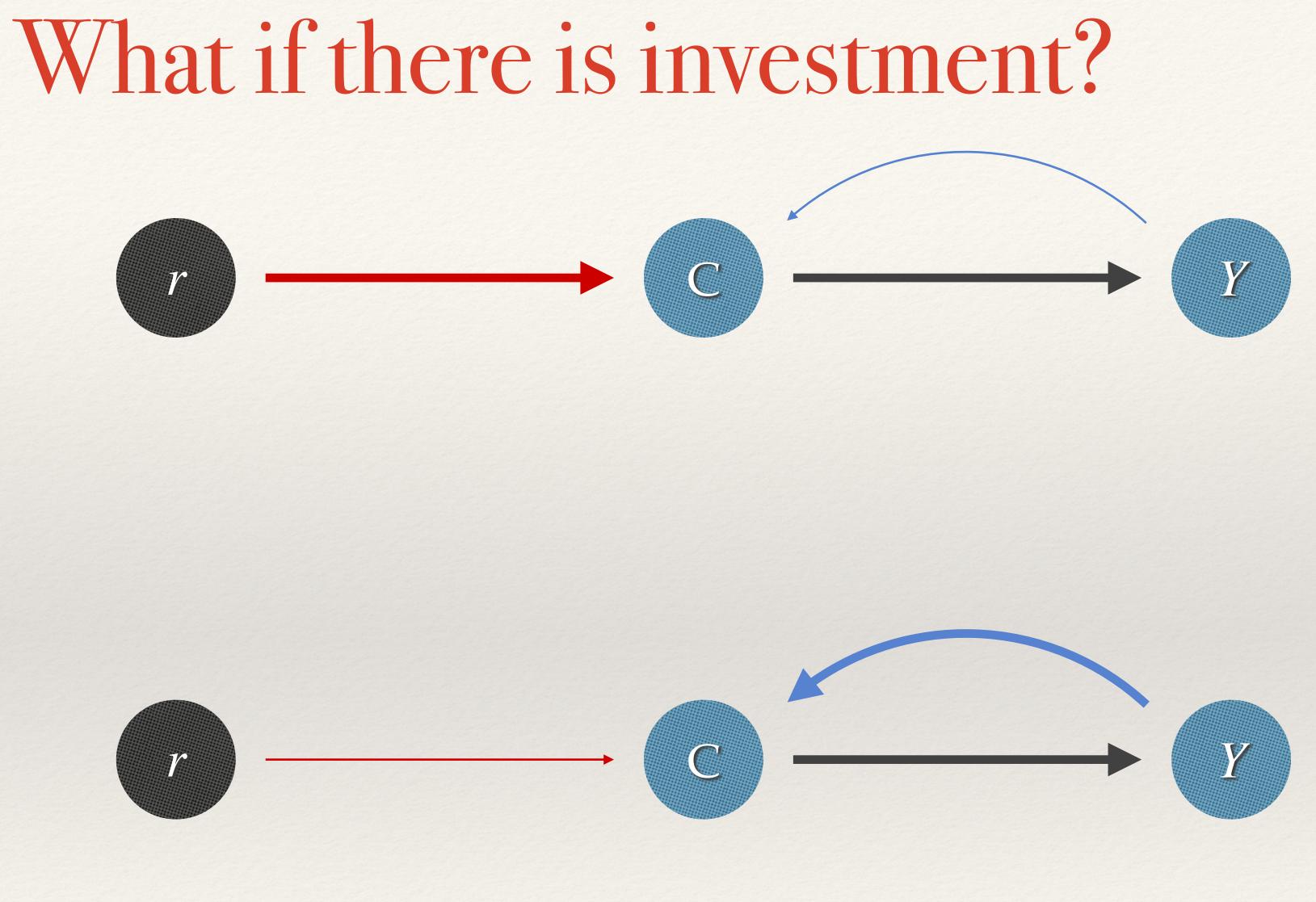


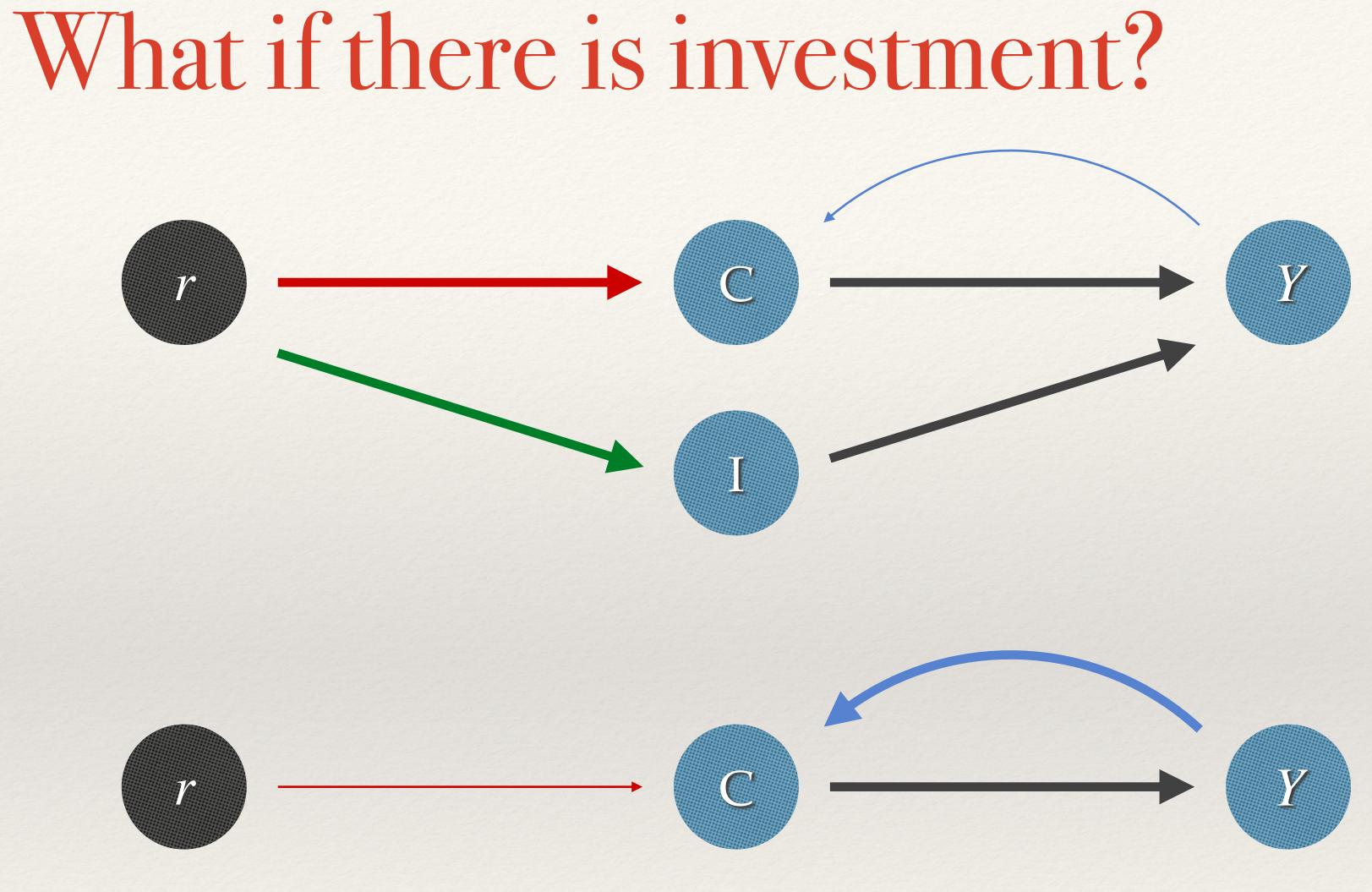


RANK





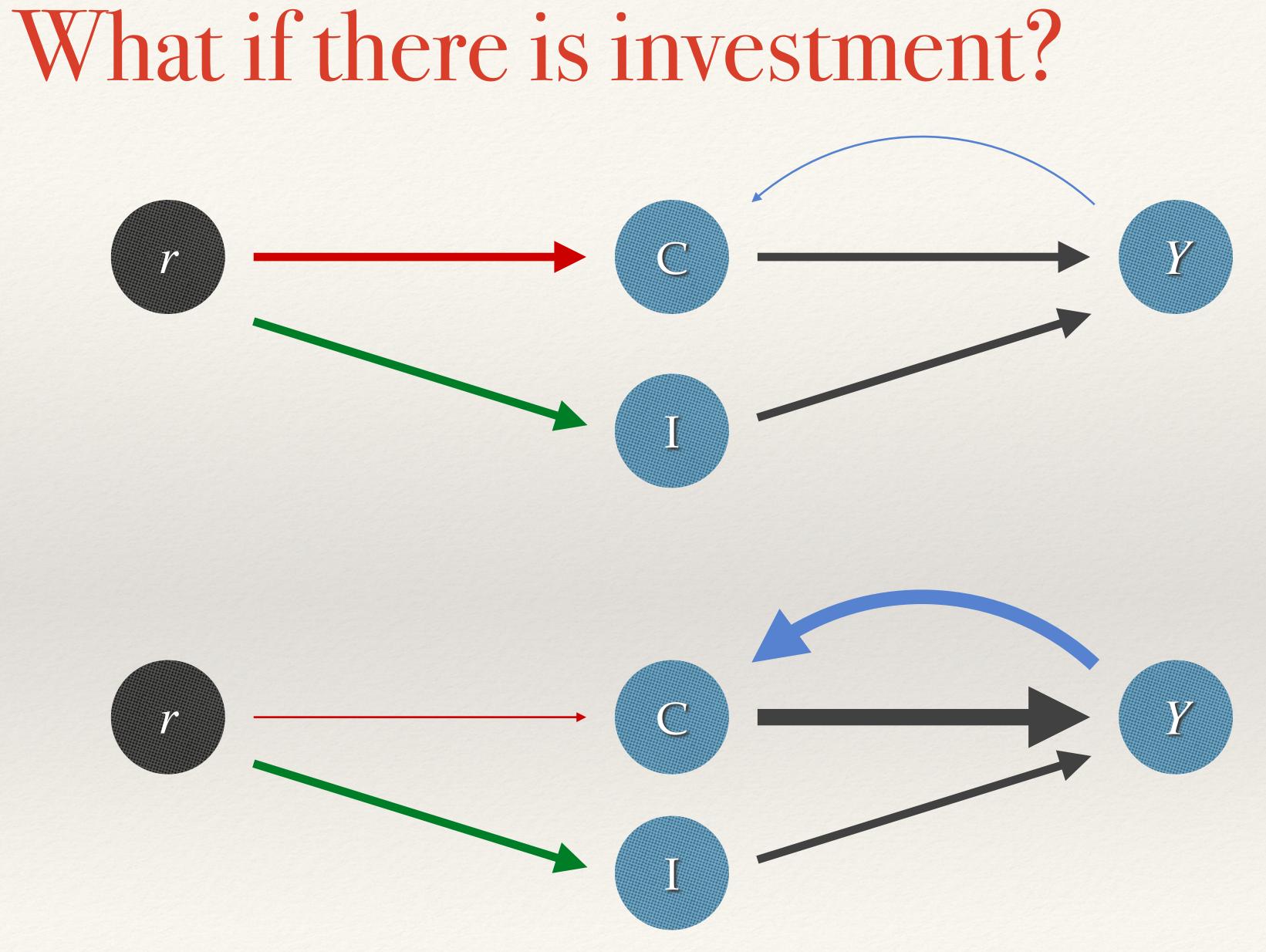




RANK

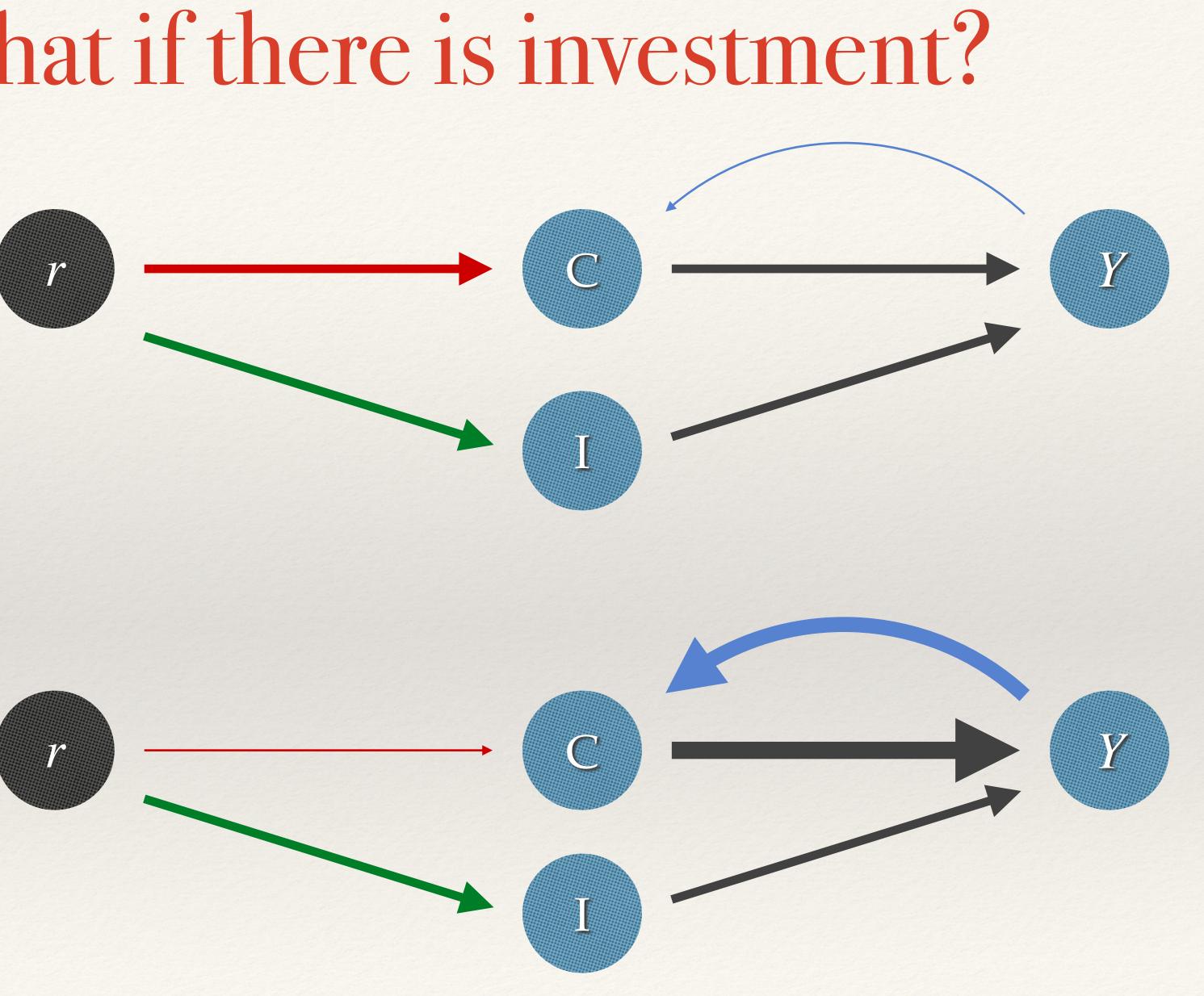


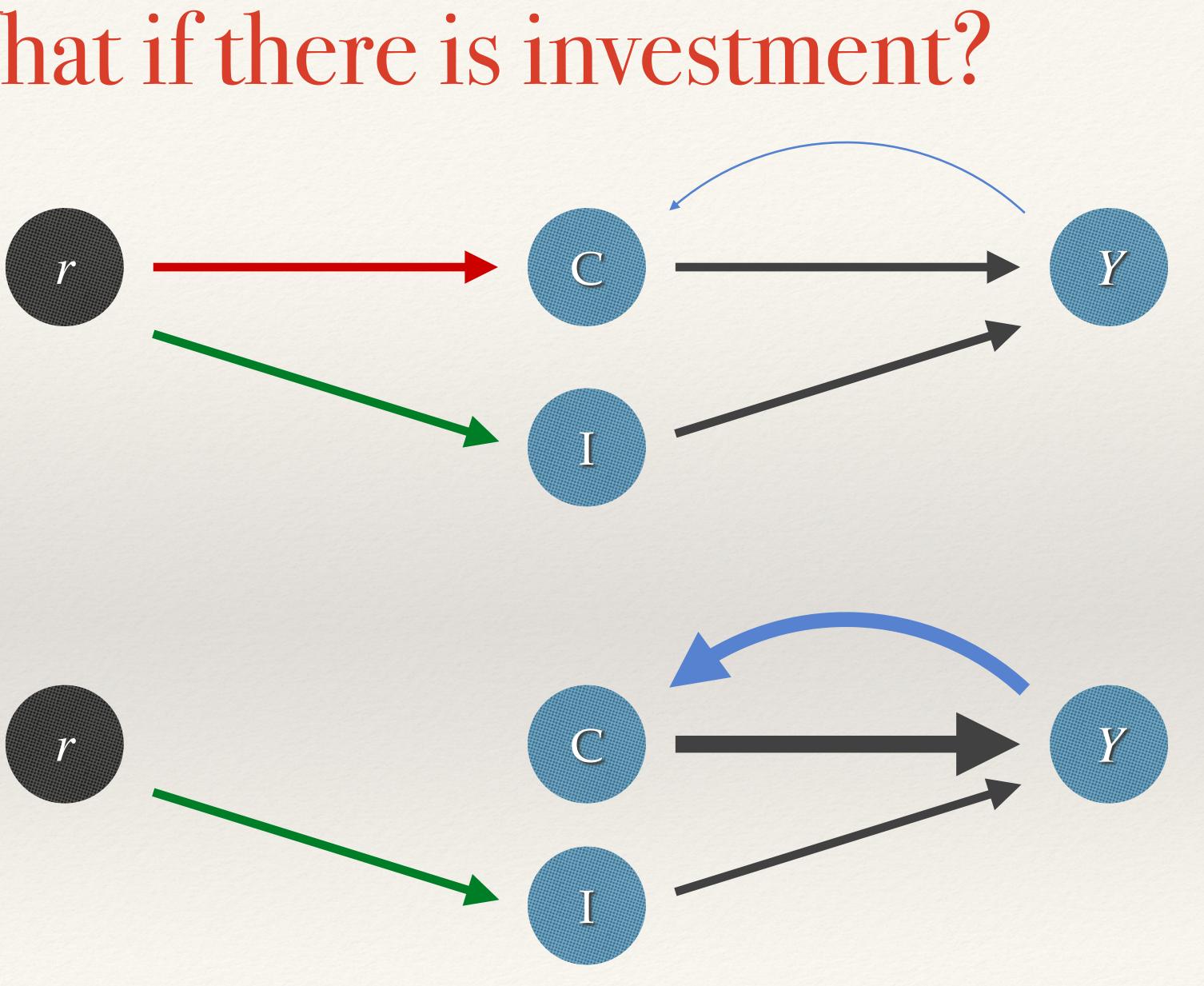




RANK

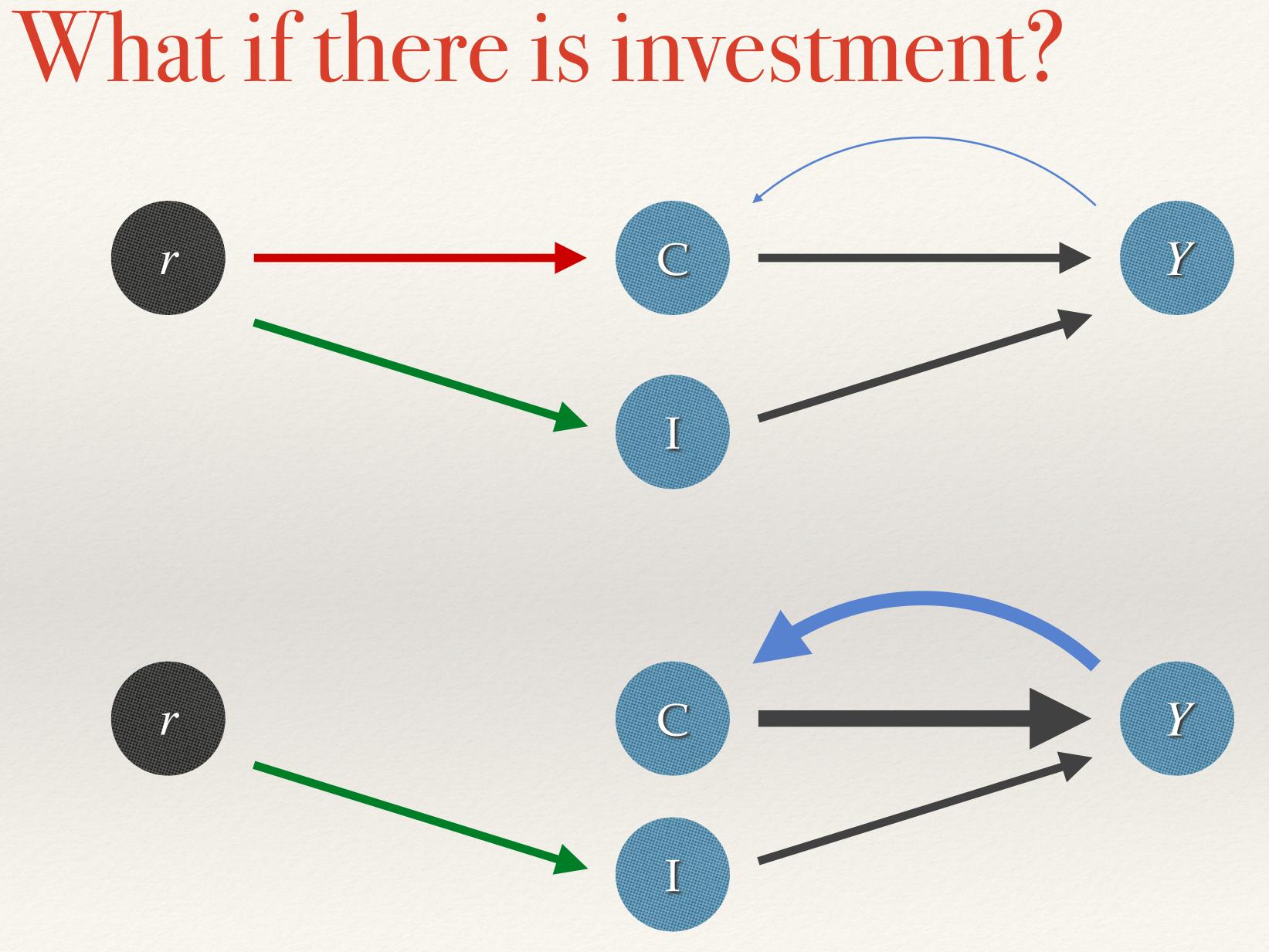


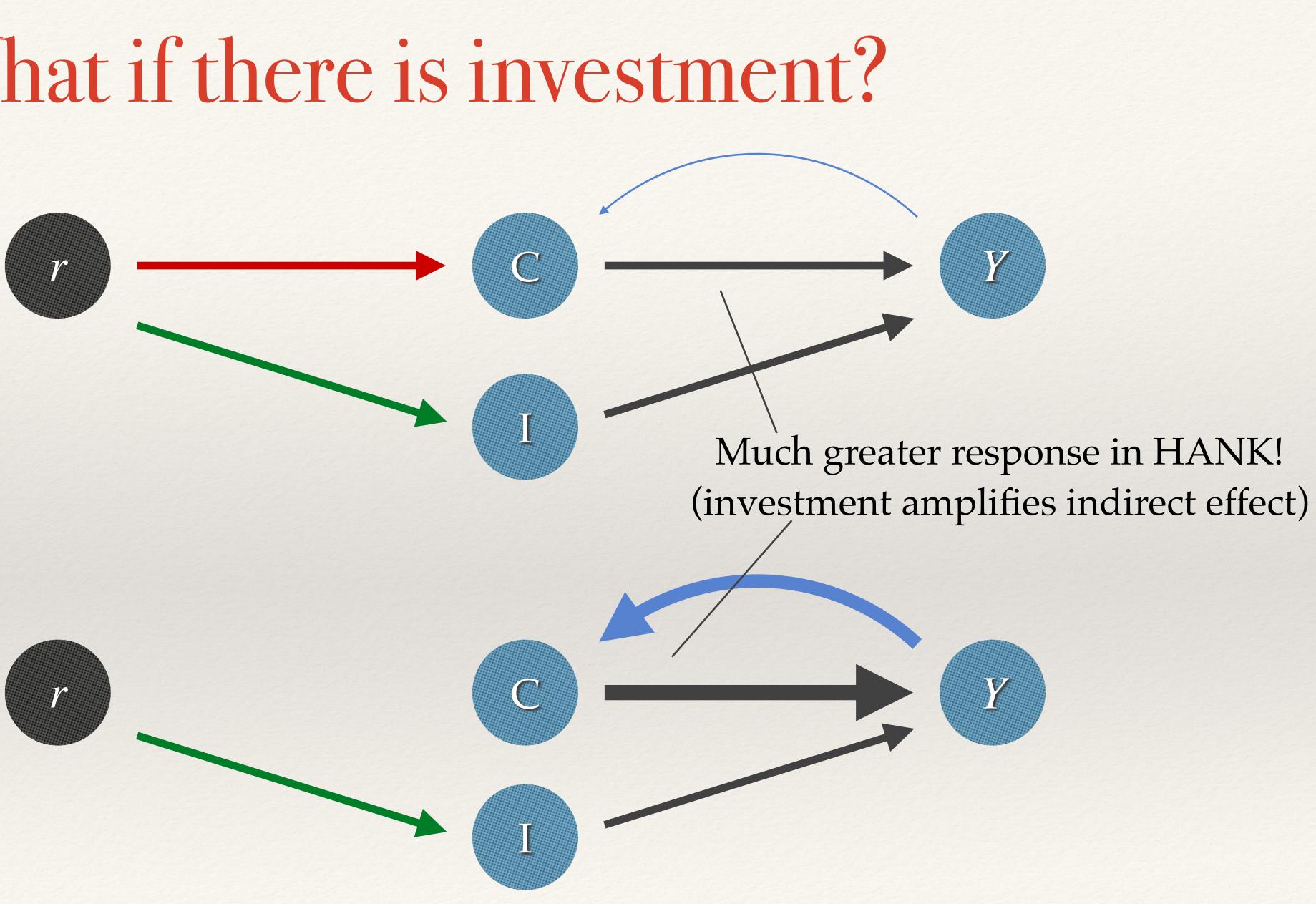




RANK

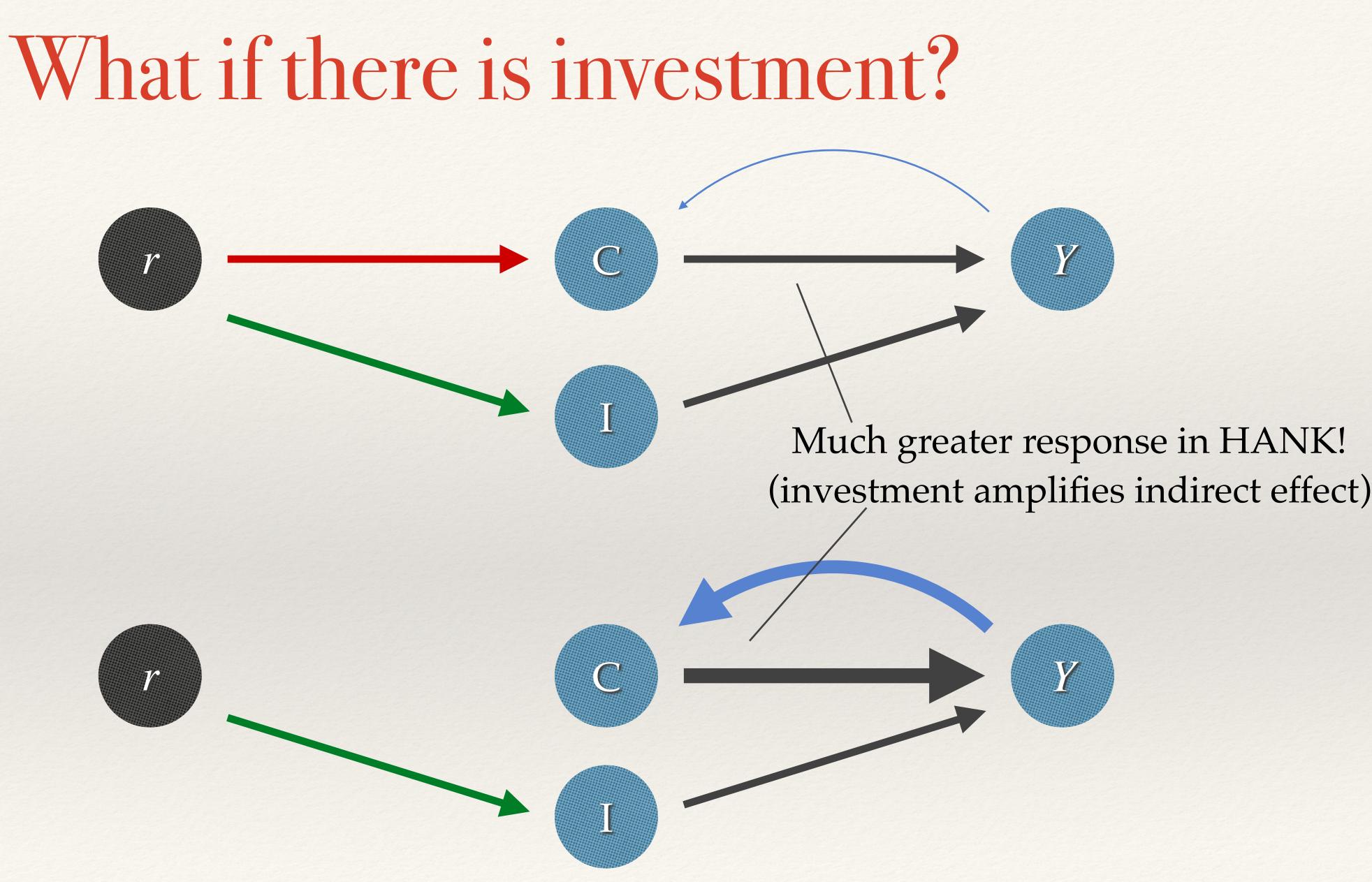




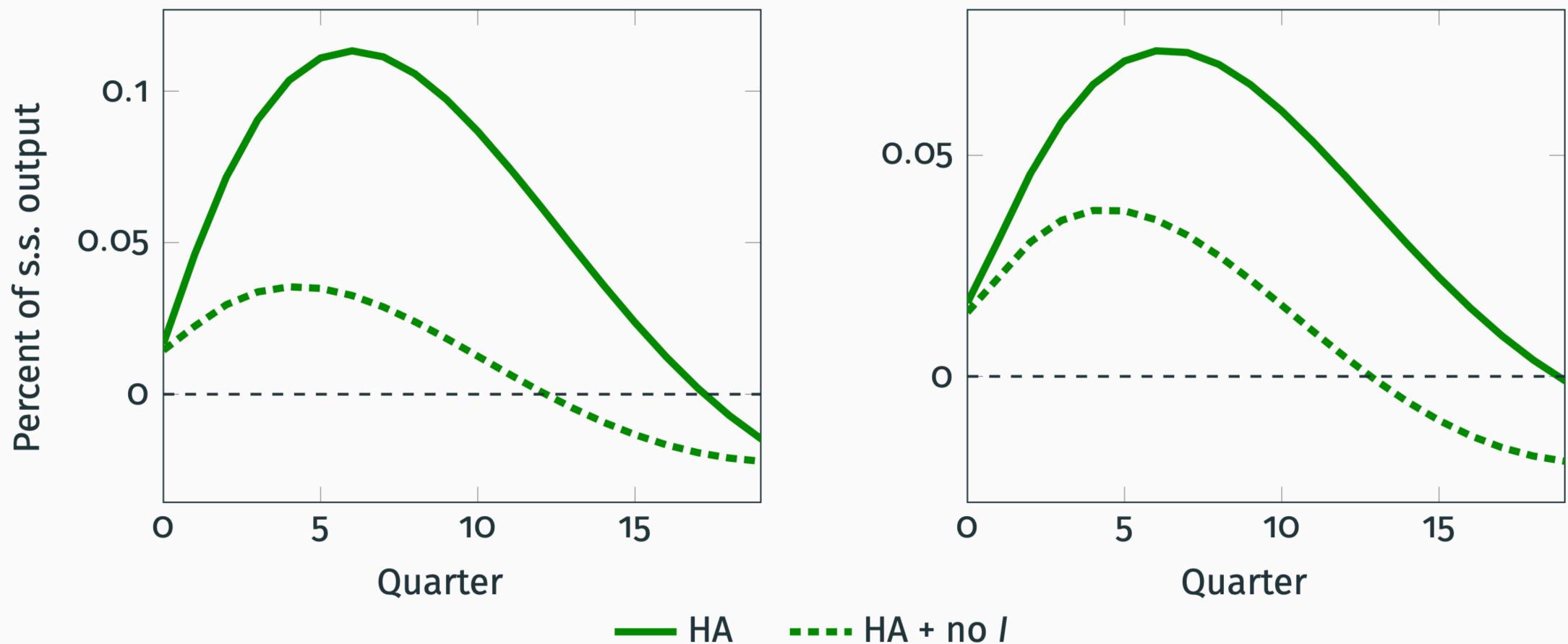


RANK





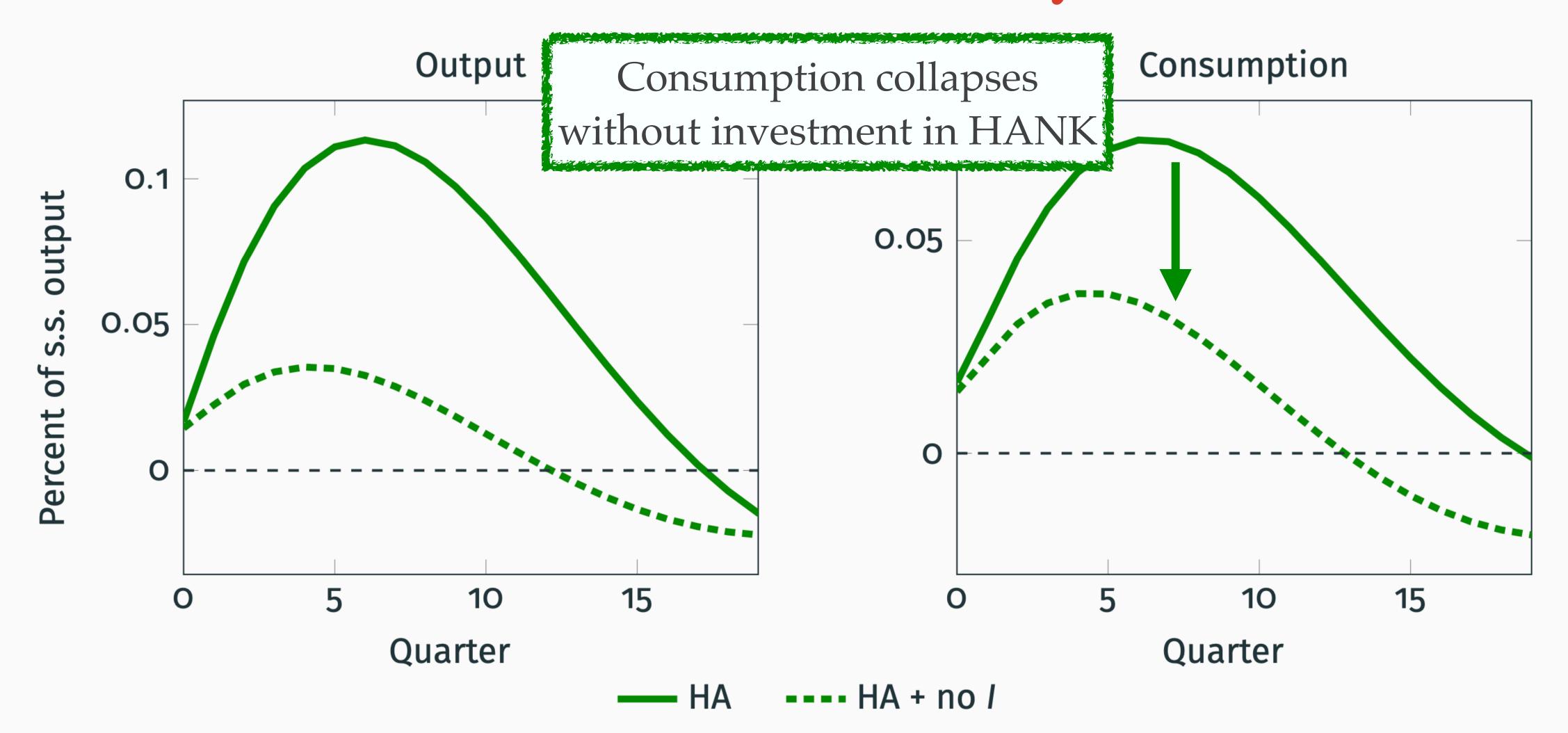
Output



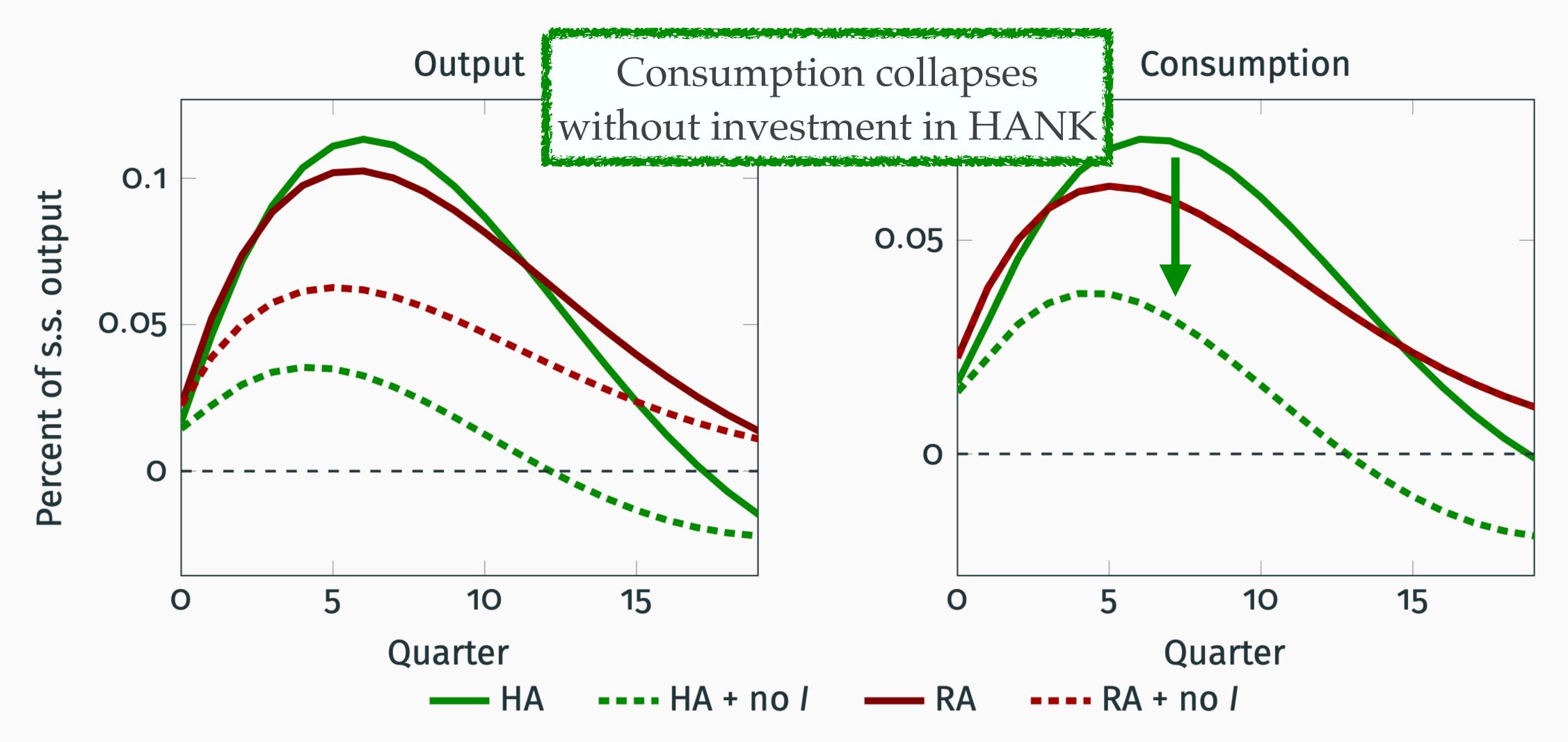
HA

Consumption

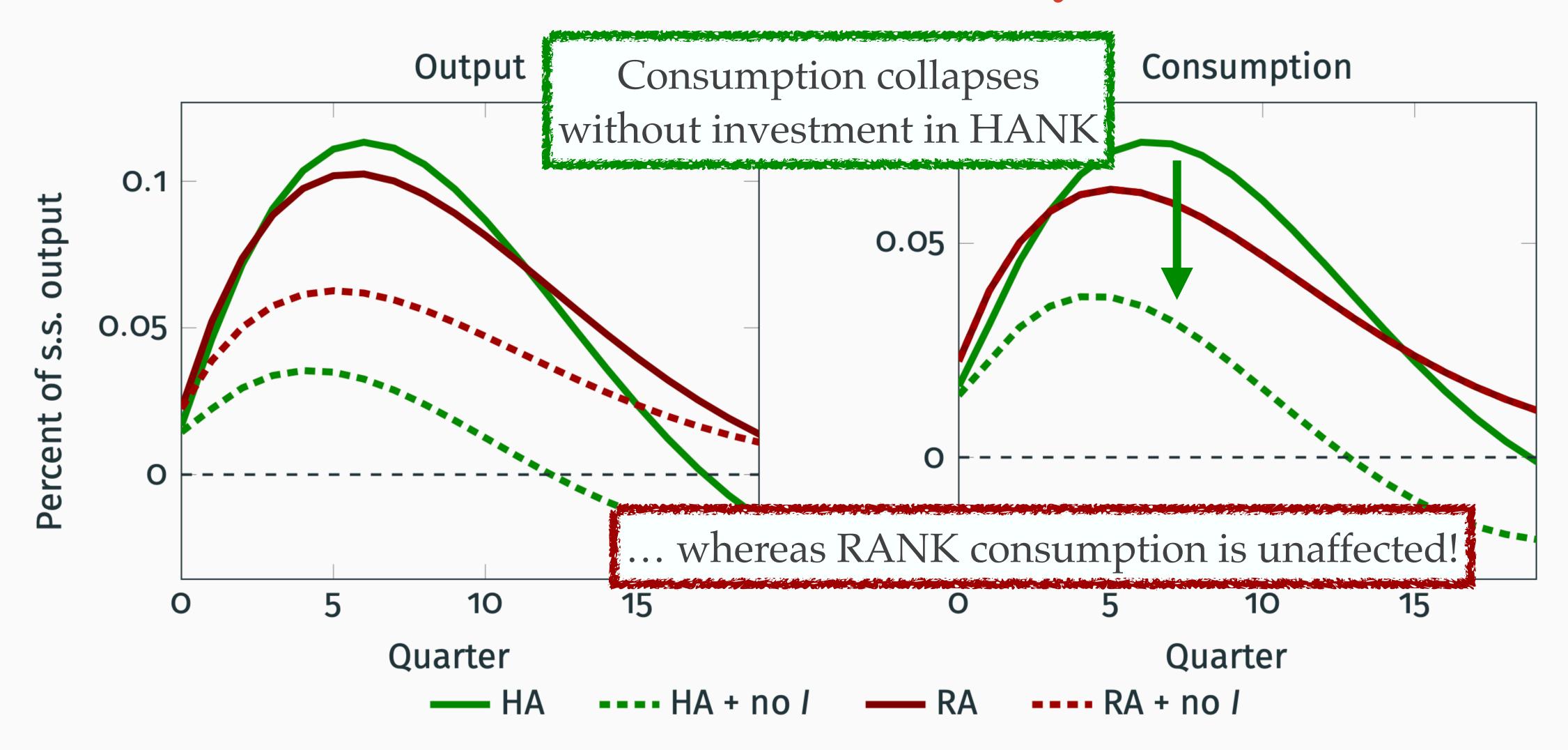














Broader implications of investment in HANK

- Limited response to monetary policy tightening
 if house prices & residential investment doesn't respond much!
- Investment stimulus (e.g. CHIPS, IRA) spills over into consumption!
 Generates outsized positive effect on aggregate demand



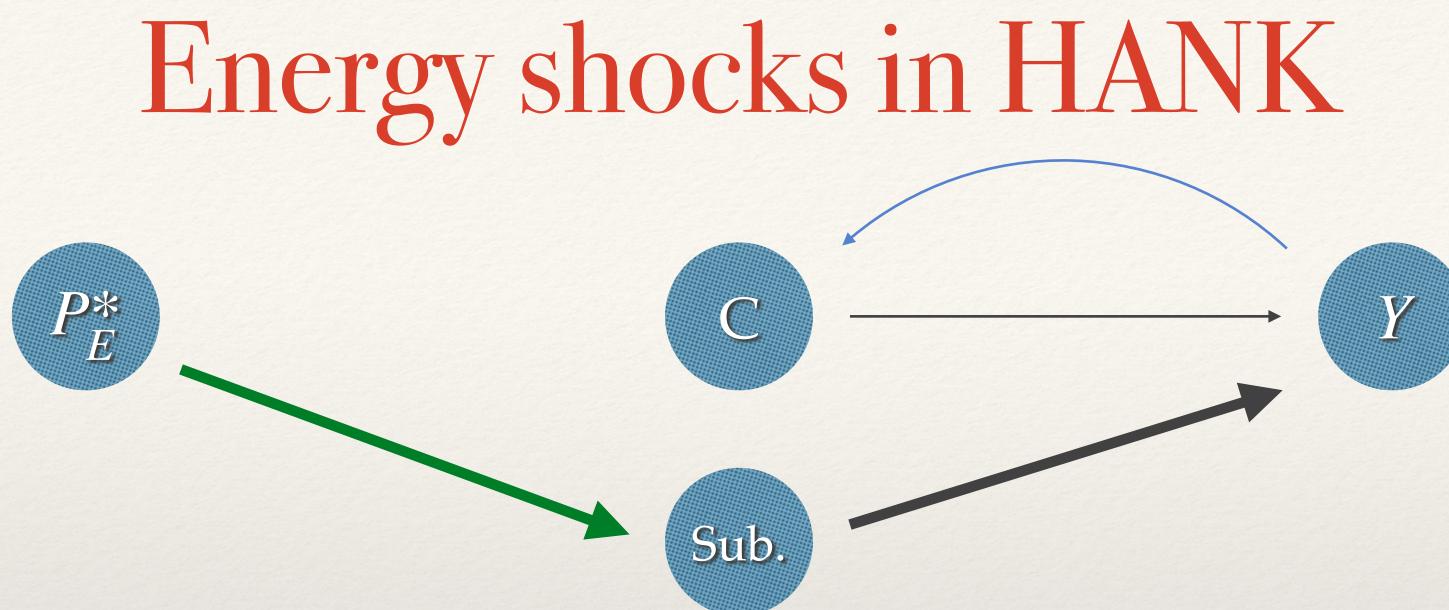
Extending the model

- * Small open economy
- * Produces "home" goods, imports "foreign" and "energy"
- * Exogenous shock to world price of energy $P_{E_t}^*$
- * Two forces:
 - * Higher relative price for energy \rightarrow substitution towards home
 - * Lower real income of households \rightarrow households cut spending

foreign" and "energy" energy P_{Et}^*

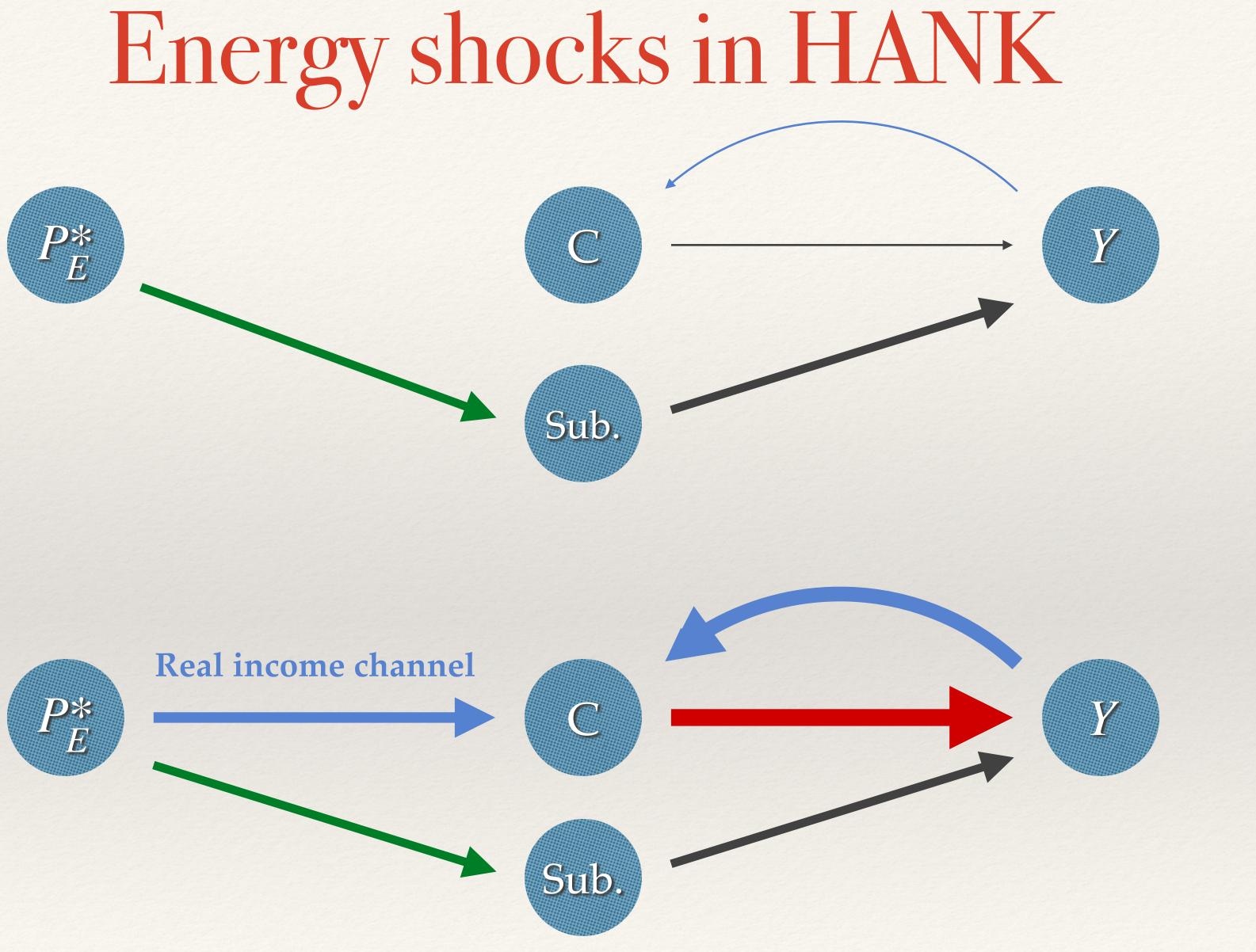
 \rightarrow substitution towards home s \rightarrow households cut spending



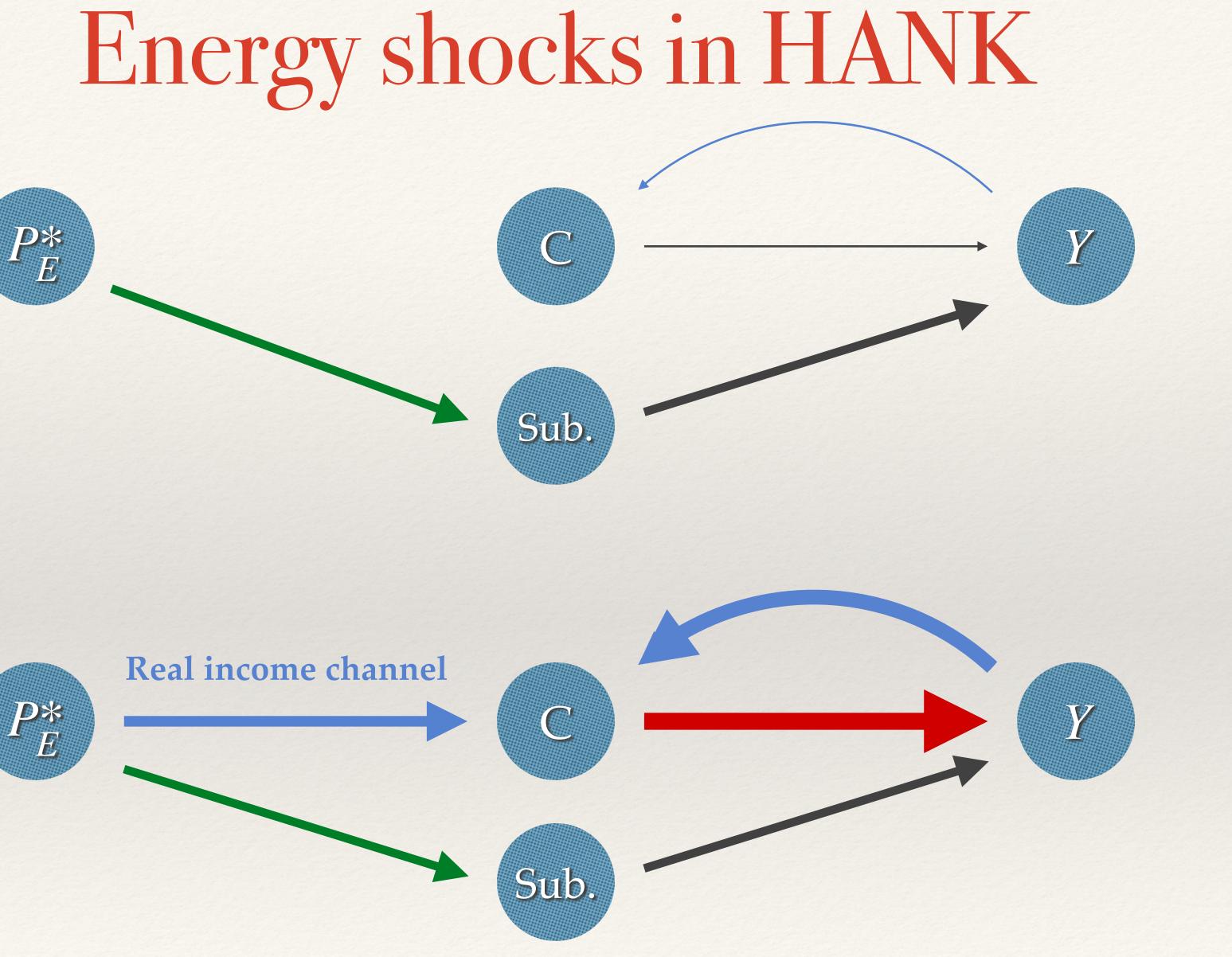


Real income channel









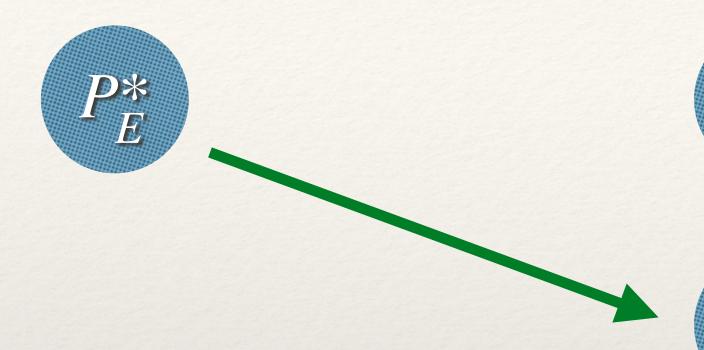
Energy shocks in HANK

C

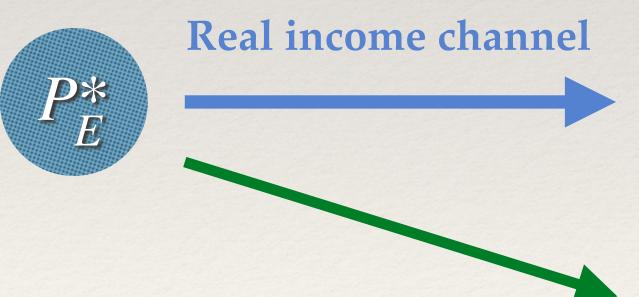
Sub.

Sub.







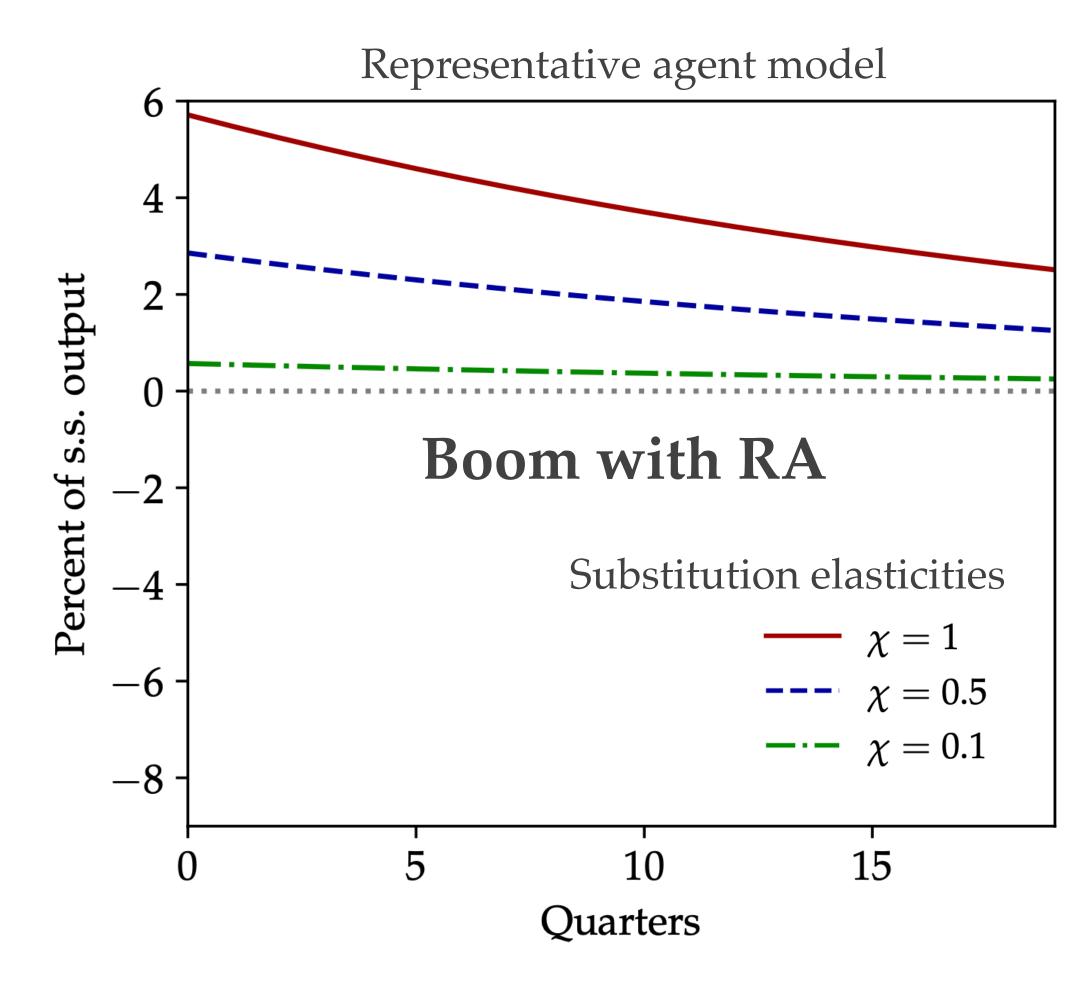


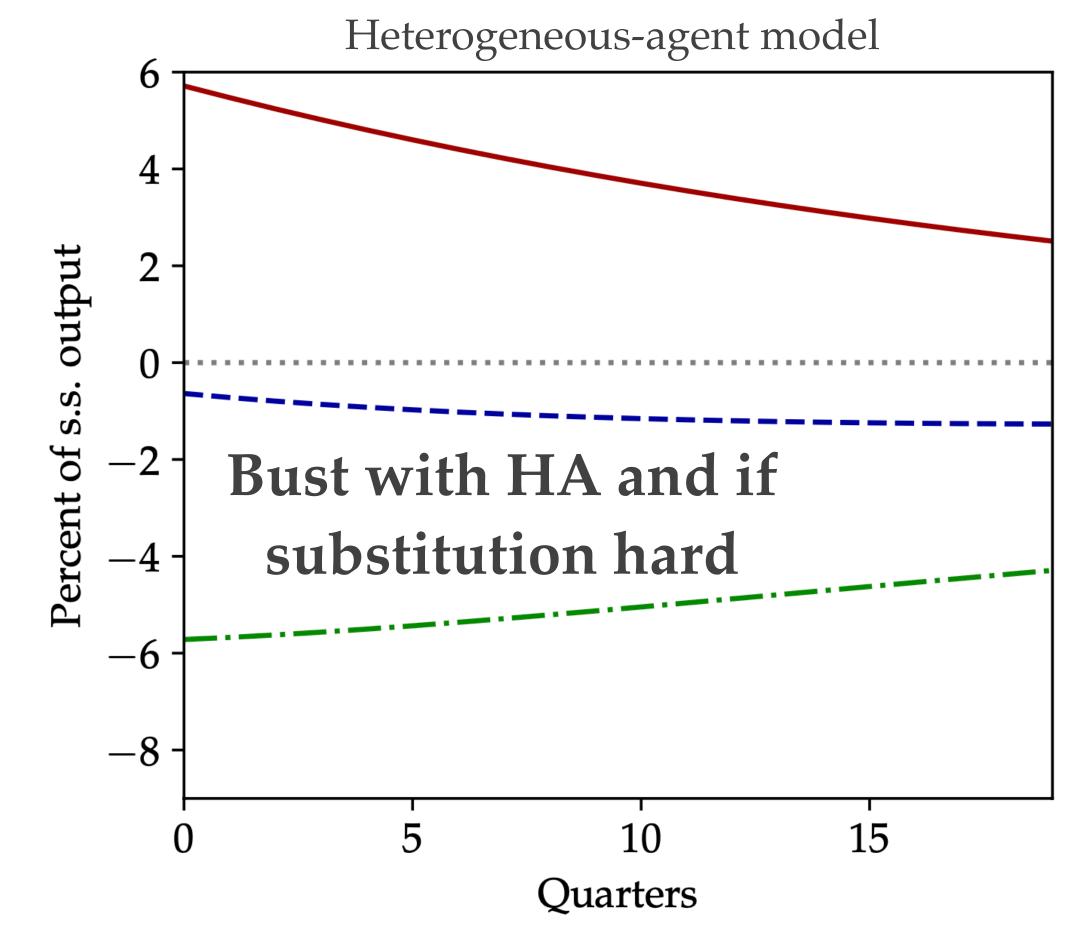
Boom in GDP in RANK! Contraction in HANK

Y

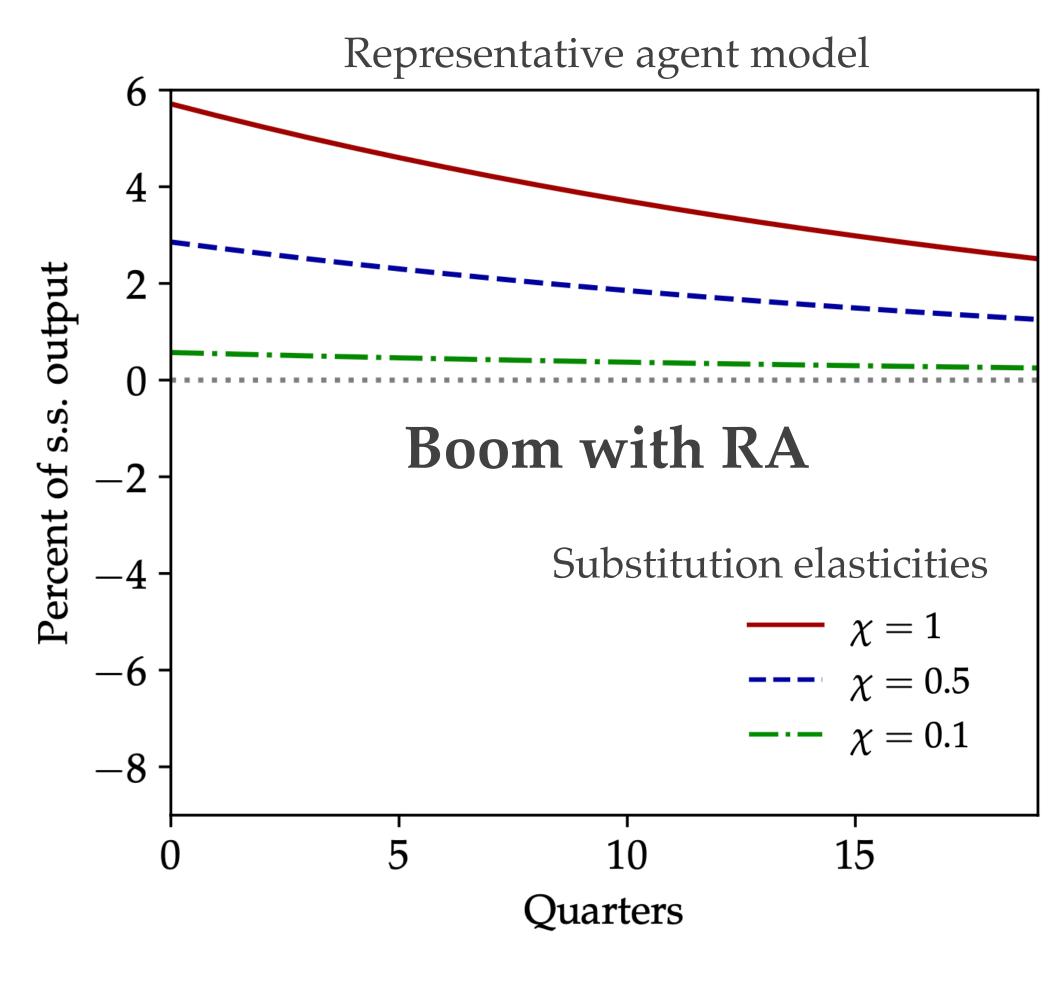
Y

Output responses to energy shock

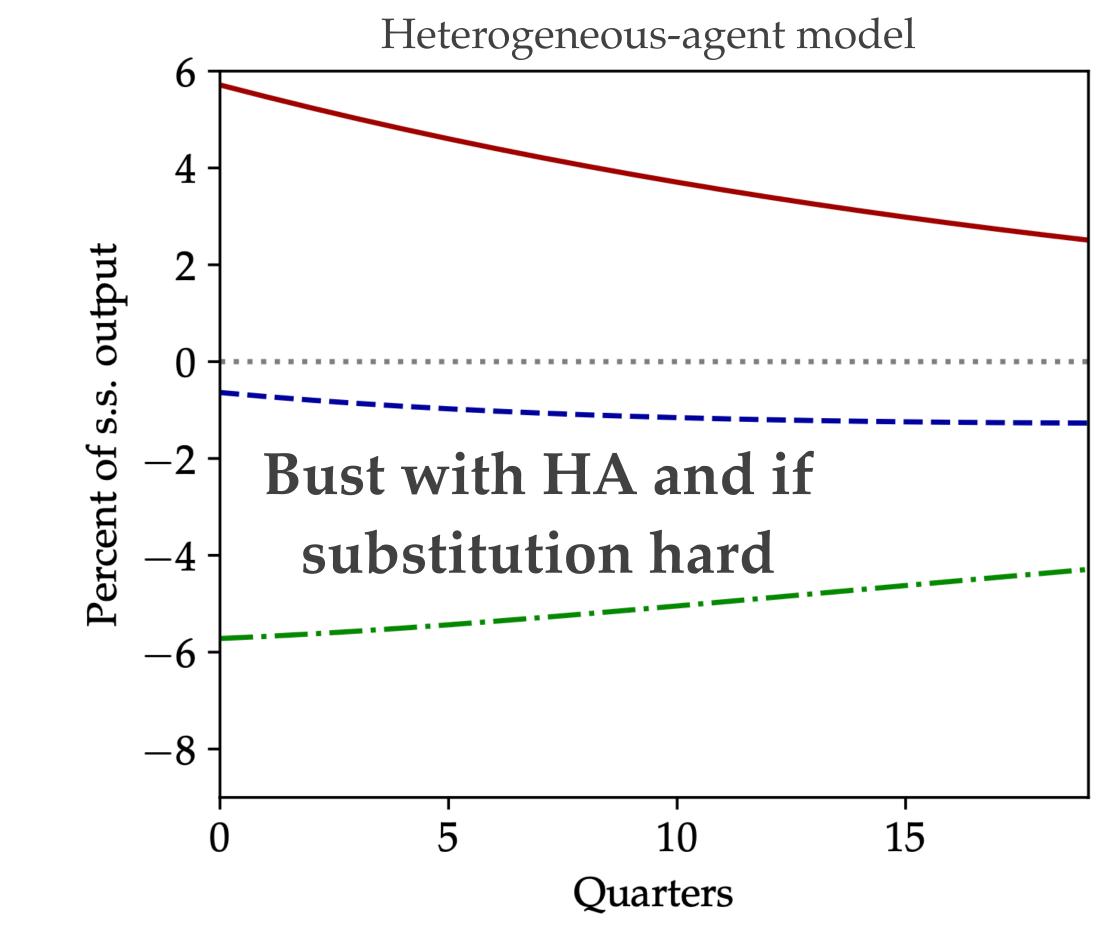




Output responses to energy shock



This result holds whether energy is used in production or not !





Conclusion: Three takeaways

- * HANK implies that consumption depends more on income than interest rates
- * Natural to organize and analyze HANK models in the sequence space
- * Three lessons:
 - * deficit-financed fiscal stimulus is persistent
 - * monetary policy only works if investment responds
 - Energy shocks are stag-flationary
- * Lots of work to do!

